

Looking Behind* the Standard Model

with Lattice Gauge Theory

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* *BSM: Behind, Beyond, ... ?*

A MATTER OF PREPOSITIONS ...

Beyond the SM

- **Expt:** New particles?
- Flavor physics anomalies?
- Matter–antimatter asymmetry
- Dark matter
- Dark energy
- Inflation
- Gravity

Behind the SM

- $SU(3) \times SU(2) \times U(1)$
- 3 families
- Quark & lepton masses & angles (hierarchies)
- Neutrino masses & angles (more hierarchies)
- The Higgs

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- **The Higgs**

The Higgs boson: not just another number to explain

THE HIGGS BOSON — THEORISTS' *BÊTE NOIRE*

As a **fundamental** scalar: *unnatural*

$$m_H^2 = m_0^2 + \text{const} \cdot M_{\text{Pl}}^2$$

$(125 \text{ GeV})^2$ vs. $(10^{19} \text{ GeV})^2$

Tamed by **supersymmetry**: quadratic divergence \implies log divergence
but the **LHC** sees no superpartners

General approach to a “UV completion”:

- Make the Higgs (multiplet) emerge as **composite** states: integrals cut off by compositeness scale $\Lambda \gtrsim 5 \text{ TeV}$ — but why is $m_H \ll \Lambda$??
- The fundamental theory is an **asymptotically free** gauge theory with spin-1/2 matter \implies again, only log divergences

In general, **COMPOSITE STATES** emerge from **strong dynamics** —

⇒ enter **Lattice Gauge Theory**

Don't bite off too much:

- Look at a specific phenomenon
- ... in a class of model
- ... that explains something but not everything.

corresponding to modern phenomenology:*

- Connect sub-LHC physics (e.g. $m_H = 125 \text{ GeV}$)
- ... to a super-LHC model ($\Lambda \gtrsim 5 \text{ TeV}$)
- ... without trying to explain everything.

*usually *without* a UV completion!

A MATTER OF PREPOSITIONS ...



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Lattice gauge theory: *Beneath* the Standard Model

THIS LECTURE:

Follows excellent reviews by

- C. Pica at Lattice 2016 [1701.07782](#)
- T. DeGrand in Rev. Mod. Phys. [1510.05018](#)
- D. Negradi and A. Patella IJMPA [1607.07638](#)

Covers recent work on

- Technicolor — “Dilatonic Higgs” (most of the recent lattice work)
- Higgs as a pseudo-Goldstone boson — “Composite Higgs”
(time permitting)

Whatever the UV theory is, it's not QCD.

QCD's lightest scalar σ (or f_0):

$$m_\sigma = 400\text{--}500 \text{ MeV}$$

vs. typical scale

$$m_\rho = 770 \text{ MeV},$$

and

$$\Gamma_\sigma = 400\text{--}700 \text{ MeV}$$

because of $\sigma \rightarrow \pi\pi$. But the Higgs boson:

$$m_H = 125 \text{ GeV} \ll \Lambda \gtrsim 5 \text{ TeV},$$

$$\Gamma_H = 4 \text{ MeV} \quad (\text{SM})$$

$$\lesssim 2\text{--}5 \text{ GeV} \quad (\text{expt})$$

TECHNICOLOR:

Break the Standard Model's $SU(2)_L \times U(1)$ dynamically, without a scalar field

Original prototype: a copy of QCD with $\Lambda \sim f_\pi \sim v \simeq 245 \text{ GeV}$

- Chiral symmetry $SU(2)_L \times SU(2)_R \rightarrow SU(2)_V$
- ... leaving 3 Nambu–Goldstone bosons π^\pm, π^0
- ... which get eaten to give mass to W^\pm, Z^0 .

Only 3/4 of the Higgs multiplet:

NO HIGGS PARTICLE

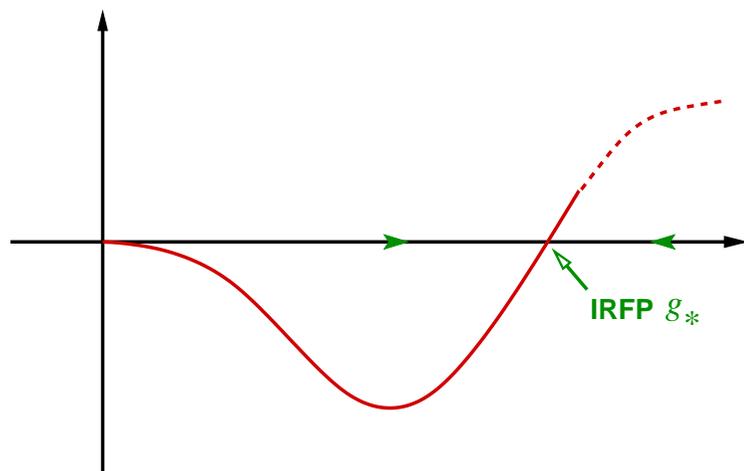
(like QCD!)

Technicolor:
Higgsless since 1976!

For a light scalar — suppose **APPROXIMATE SCALE INVARIANCE**

In the **Conformal Window**:

$$N_f > N_f^*$$

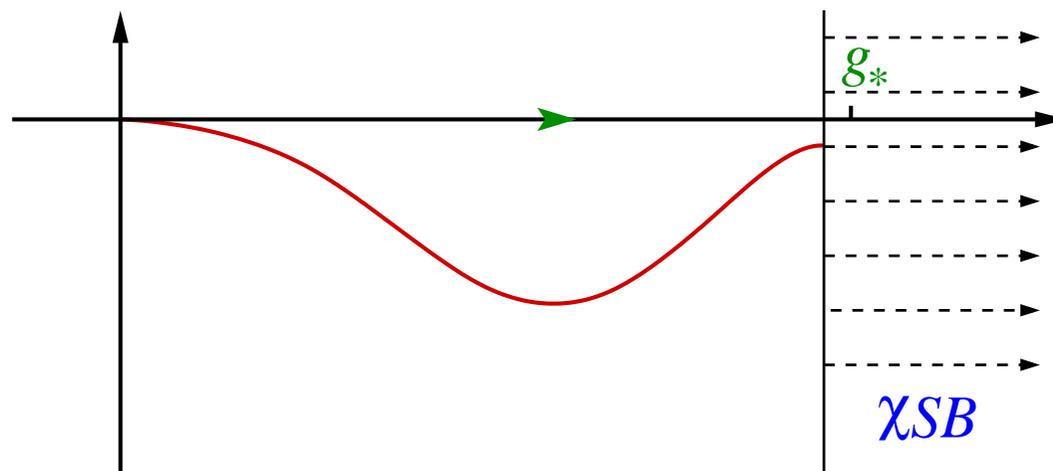


IR fixed point \Rightarrow scale invariance

Below the **sill**:

$$N_f \text{ slightly } < N_f^*$$

(“**WALKING** technicolor”)



approximate scale invariance

- Guess: **Light scalar** emerges as pseudo-Goldstone boson of approximate dilatation symmetry.
 $\Rightarrow m_H$ is protected from UV, like any PGB (and Yukawa couplings $\propto m_q$)

QUESTIONS FOR DIRECT CALCULATIONS:

1. Where is the sill N_f^* ? (for given gauge group & fermion rep)
2. Is there a light scalar in theories below the sill?

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ANSWERS:

1. It might not matter too much — as long as we confirm $N_f < N_f^*$.
2. Yes.

FINDING N_f^* — SU(3)/fund

2 loops: $N_f^* = 8.05$

- $N_f = 4n$ popular because of staggered fermions*
- $N_f = 12$ — a long-running controversy
- many approaches: scaling of spectrum, finite- T transition, Dirac eigenvalues — point (mostly) towards conformality of $N_f = 12$
- **Danger:** *slow* running (spontaneous χ SB) is very similar to *no* running (fixed point)
 - possible fixed point at IR scale L would be at strong coupling
slow (or no) running \implies strong coupling at scale a as well,
i.e. far from continuum limit in UV
- **RG** was born for this purpose — compare L_1 to L_2 and obtain β fn
- no scale Λ ($1/L < \Lambda < 1/a$) \implies everything is a function of a/L
 \implies continuum extrap equivalent to $L \rightarrow \infty$

*watch for taste breaking

LATEST on $N_f = 12$ — β function from gradient flow

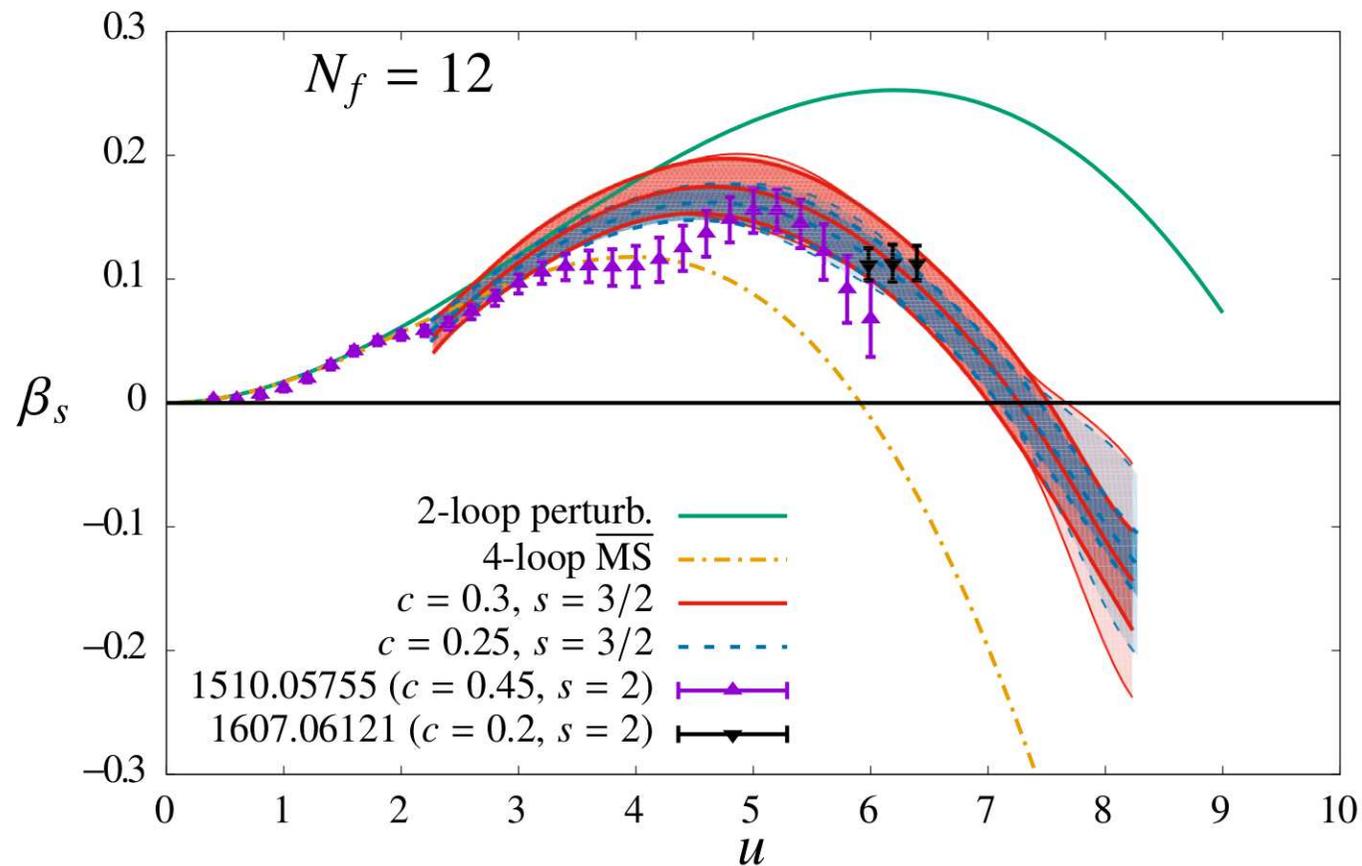
(Hasenfratz & Schaich 1610.10004, LatHiggs Fodor *et al.* 1607.06121,
Lin, Ogawa, Ramos 1510.05755)

- **Existence** (or not) of fixed point g_* is universal
- **Location** is not. Neither is the β function.
 - Varies with **scheme** for defining g : Schrödinger functional vs. gradient flow; parameter c in gradient flow

$$g_{\text{GF}}^2 = \frac{128\pi^2}{3(N^2 - 1)} \langle t^2 E(t) \rangle \quad \text{at scale } \sqrt{8t} = cL$$

- **Shouldn't** depend on: discretization/improvement of action (extrap. $a \rightarrow 0$); disc./imp. of E ; scale factor $s \equiv L_2/L_1$

FIXED POINT from Hasenfratz & Schaich, consistent with previous work,
but go to stronger couplings (nHYP action)



- The controversy continues (recent LatHiggs)...

[Note $N_f = 10$ is conformal (Chiu 1603.08854 DWF)]

DOES $N_f = 8$ DELIVER THE GOODS?

(LSD Appelquist *et al.* 1601.04027 + recent)

(LatKMI Y. Aoki *et al.* 1610.07011)

Recall two-loops: $N_f^* = 8.05$. The claim is that $N_f = 8$ **walks**.

Study m_f dependence of various quantities:

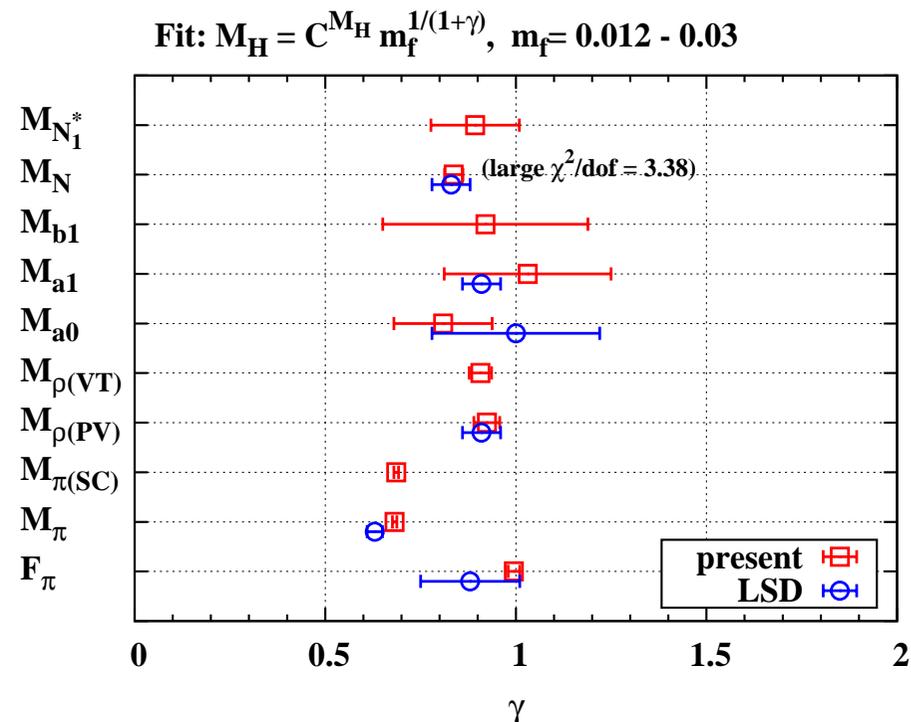
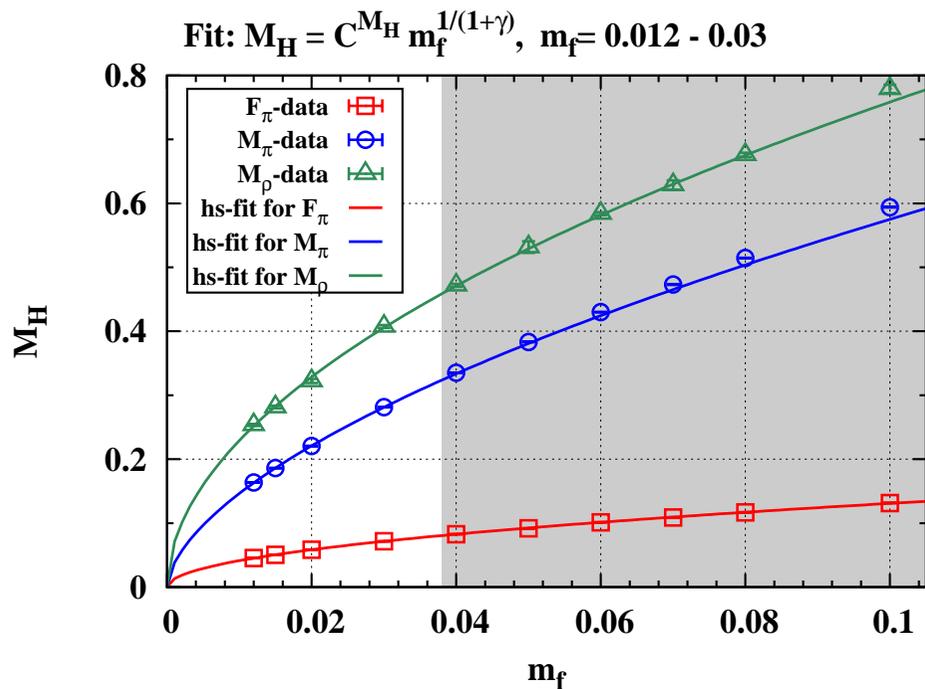
- As $m_f \rightarrow 0$, find χ SB: $f_\pi \rightarrow \text{const}$ and massless π
- Hyperscaling of all masses (*except the π*) for a large range of m_f :

$$M_H \sim m_f^{1/(1+\gamma)}, \quad \gamma \simeq 1$$

\implies nearby fixed point

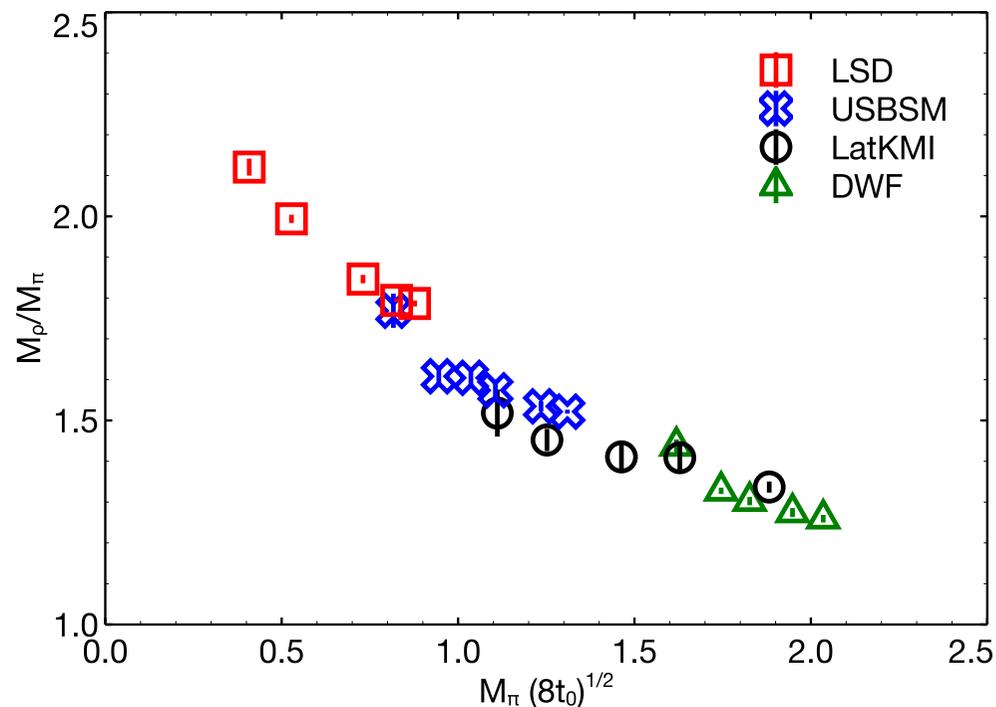
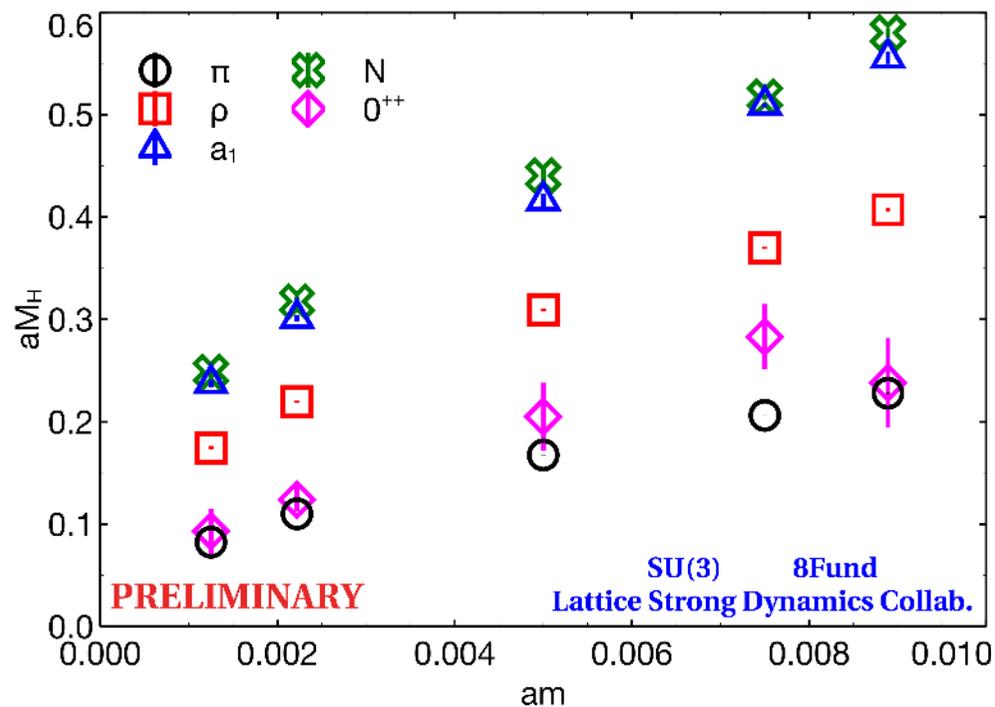
- Light scalar — degenerate with π over large range of m_f
As $m_\pi \rightarrow 0$, where does the scalar end up?

HYPERSCALING — LatKMI [cf. LSD 1405.4752 (DWF)]



- Exponent γ common to all hadrons except π (and σ)
- Note: single value of $\beta = 6/g_0^2$ — not the same thing as a single lattice spacing

LIGHT SCALAR — updated LSD (D. Schaich)



- $M_\pi \rightarrow 0$ with m_f
- So far, $m_\sigma \simeq m_\pi$

- Edinburgh plot: M_ρ stays finite as $M_\pi \rightarrow 0$: χ SB
- LSD's min $M_\pi \ll$ LatKMI, older work

FORCING A THEORY TO WALK: $N_f = 4\ell + 8h$

$N_f = 8$ has 63 Goldstone bosons. 3 are eaten. 36 are neutral under EW interactions! (& S parameter ...)

⇒ Give them a mass *explicitly*, but preserve near-conformality. Example:

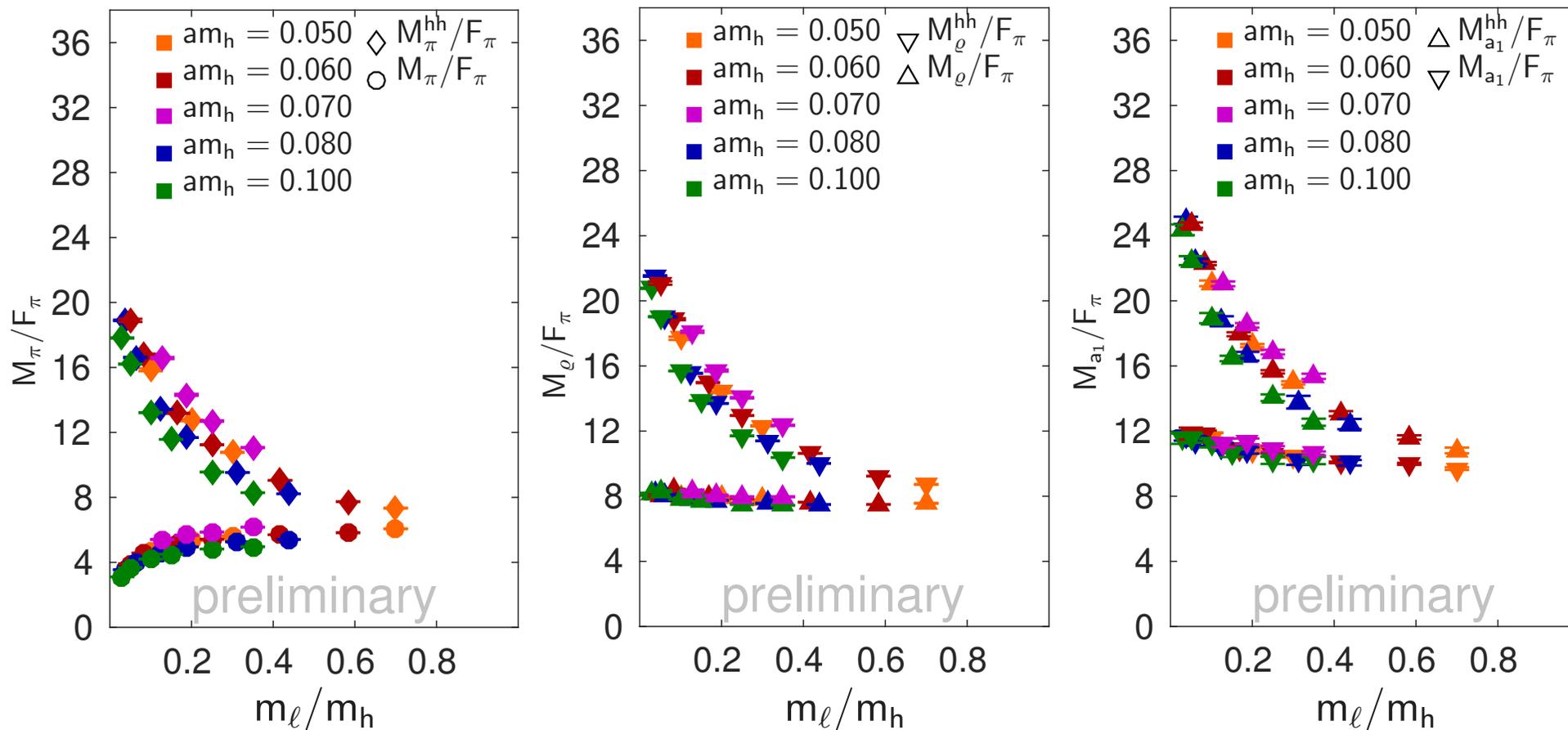
(Hasenfratz, Rebbi, Witzel 1609.01401 + recent,
following Brower *et al.* 1512.02576)

- SU(3) with $N_f = 12$, nearly conformal at scale Λ .
- Lift 8 flavors with $m_h < \Lambda$.
- Low-energy theory sees 4 flavors with $m_\ell \rightarrow 0$.
- Appeal to near-conformality to give light Higgs as above.

Note m_h has to come from somewhere.

Extra Goldstones ($N_f = 4$) still have to go somewhere. Better for *composite Higgs* (Ma & Cacciapaglia).

HYPERSCALING in $N_f = 4\ell + 8h - 0$. Witzel (updated)



- Mass ratios depend only on ratio m_ℓ/m_h , even for hh mesons; β is irrelevant. Light $\pi \Rightarrow \chi$ SB, $m_\sigma \simeq m_\pi$ (not shown).

IS THE LIGHT SCALAR A (pseudo-)DILATON? Compare to effective action.

Dilatation current $S_\mu = x_\nu T_{\mu\nu}$ is anomalous,

$$\partial_\mu S_\mu = T_{\mu\mu} = -\frac{\beta(g^2)}{4g^2} F^2 - (1 + \gamma_m) m \bar{\psi} \psi$$

⇒ partially conserved if m and $\beta(g^2(\Lambda))$ are small.

- **Conceptual question:** What is the unperturbed theory? If $\beta = m = 0$ then the theory is conformal, *i.e.*, there are **no GB's!**
- Cf. broken chiral symmetry: $m_\pi^2 f_\pi^2 = m_q \langle \bar{\psi} \psi \rangle$, expansion around $m_q = 0$.

⇒ Construct an **effective action** for SSB of chiral & dilatation symmetries

(Golterman & Shamir 1603.04575, 1610.01752)

$$p^2/\Lambda^2 \sim m/\Lambda \sim 1/N_c \sim |N_f - N_f^*|/N_c \sim \delta$$

Dilaton action

$$\mathcal{L}_\tau = \frac{f_\tau^2}{2} V_\tau(\tau) e^{2\tau} (\partial_\mu \tau)^2 + f_\tau^2 B_\tau V_d(\tau) e^{4\tau} + \text{coupling to } \pi$$

Expand potential $V_d = \sum c_n \tau^n$, $c_n = O(\delta^n)$: fix constants (including m_τ) from correlators in gauge theory.

See also: Kasai, Okumura, Suzuki 1609.02264; Golterman & Shamir 1611.04275

Fit to LSD $SU(3)/N_f = 8$ data

(Appelquist, Ingoldby, Piai 1702.04410)

- Not \mathcal{L}_τ above but *ad hoc* dilaton potential

$$V_1 = \frac{m_\tau^2}{8f_\tau^2} (\chi^2 - f_\tau^2)^2, \quad \chi \equiv f_\tau e^\tau$$

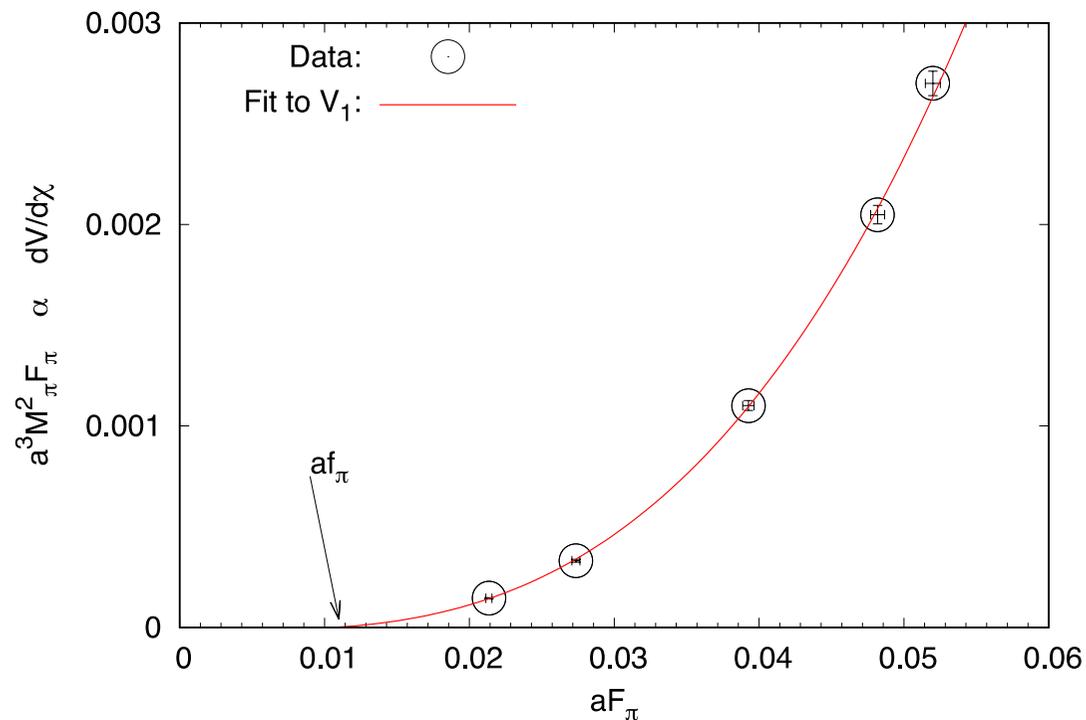
- Fit to LO \mathcal{L}_τ is indistinguishable.

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$$V_1 = \frac{m_\tau^2}{8f_\tau^2} (\chi^2 - f_\tau^2)^2, \quad \chi \equiv f_\tau e^\tau$$

- F_π has substantial m dependence, due to dilaton. Successful fit (in lattice units) shows how $v \sim F_\pi$ might be $\ll \Lambda$:



SIMILAR PHYSICS in OTHER GAUGE THEORIES

- $SU(2)/\text{fund}$, $N_f = 8$ — in the conformal window

Leino et al. 1701.04666

- $SU(2)/\text{adj}$, $N_f = 1, 2$ — straddling the sill

Athenodorou et al. 1605.04298; *Bergner et al.* 1610.01576

- $SU(2)/\text{adj}$, $N_f = 2 + \text{NJL}$ — induce walking with NJL term

Rantaharju, Pica, Sannino 1704.03977

- $SU(3)/\text{sextet}$, $N_f = 2$ — may walk, with light Higgs

Fodor et al. 1506.06599, 1601.03302 (staggered)

Hansen, Drach, Pica 1705.11010 (unimp. Wilson)

OTHER ISSUES: anomalous dimension γ_m , precision tests (e.g. S parameter)

COMPOSITE HIGGS

(Georgi & Kaplan 1984)

- **Hypercolor** theory (with scale $f \gg v$) has spontaneous symmetry breaking with $SU(2)_L \times U(1)$ *unbroken*.
Higgs multiplet $h \subset$ Goldstone bosons so $m_h = 0$ and in fact $V(h) = 0$

- Couple to gauge bosons/fermions of SM, generate

$$V_{\text{eff}}(h) = \alpha \cos(2h/f) - \beta \sin^2(2h/f)$$

1st term: $\alpha = -\frac{1}{2}(3g^2 + g'^2)C_{LR} + \text{top loops}^*$

2nd term: $\beta = \text{top loops}^*$

- If $\alpha + 2\beta > 0$ then $h = 0$ is unstable, $v = \sqrt{2} \langle h \rangle$ given by
 $\cos(\sqrt{2}v/f) = -\alpha/(2\beta) \implies (v/f)^2 \approx 1 + \alpha/(2\beta)$
- $C_{LR} = \# \int_0^\infty dq^2 q^2 \Pi_{LR}(q^2) = \text{current correlator}$

* Golterman & Shamir, in preparation

REALISTIC MODELS

Narrowed down by [Ferretti & Karateev 1312.5330](#) to add
the possibility of **PARTIALLY COMPOSITE TOP QUARK**.



([Kaplan 1991](#))



For example:

$SU(4)$ gauge theory with **sextet** fermions  — a **real** representation.

5 Majorana fermions give the global symmetry $SU(5) \rightarrow SO(5)$
— a good embedding for the Higgs multiplet

For a **top partner**, add **fund rep** fermions  (**3** × Dirac)

Note: Technicolor is *silent* on the top quark — much too heavy for ETC

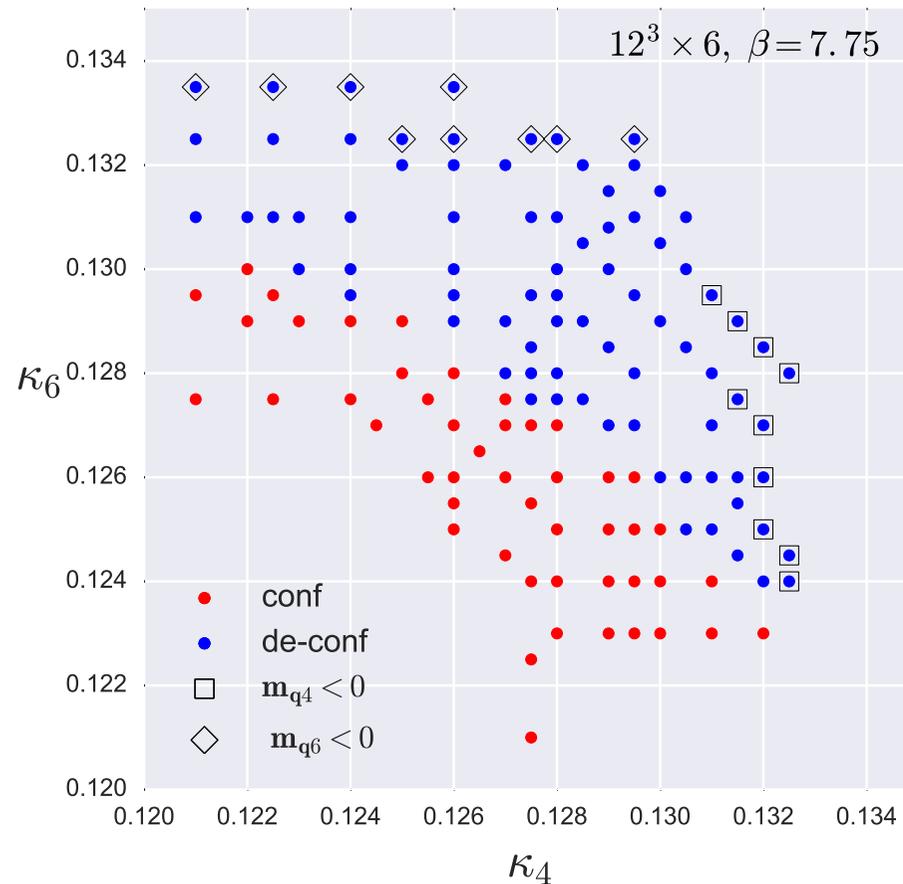
CURRENT WORK on Composite Higgs / Partially Composite Top



TACO (DeGrand et al.): $SU(4)$ gauge with $\{N_f = 2 \times 6 \text{ and } 2 \times 4\}$

— on the way to The Real Thing: $\{5 \times 6 \text{ (Majorana) and } 3 \times 4\}$

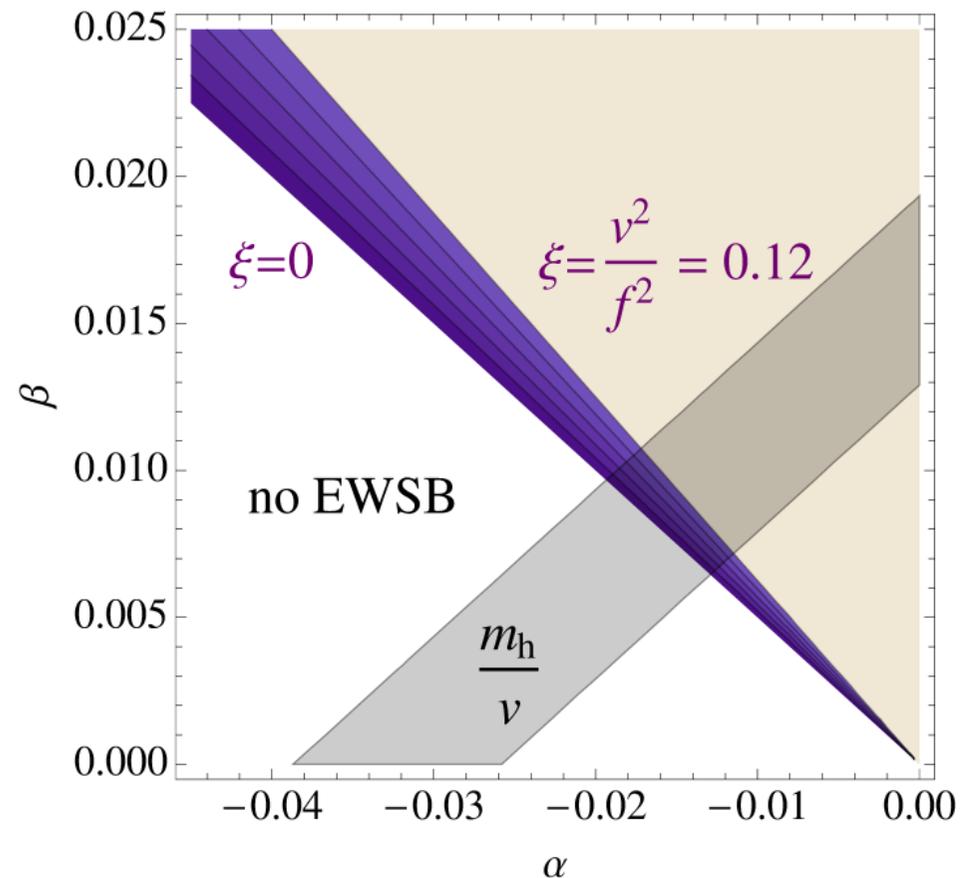
(V. Ayyar)



LHC CONSTRAINTS listed by DeI Debbio, Englert, Zwicky 1703.06064

⇒ E.g., Higgs potential $V_{\text{eff}}(h) = \alpha \cos(2h/f) - \beta \sin^2(2h/f)$ constrained by

- $\alpha + 2\beta > 0$ for SSB
- $8(2\beta - \alpha) = m_h^2/v^2$
Higgs mass
- Future limits on exotic
Goldstone bosons



N.B. *Problems with the model:* e.g., coupling of extra Goldstone fields to Higgs field

SUMMARY

TECHNICOLOR

1. Looking for the sill of the conformal window — $SU(3) : N_f^* < 12 ?$
2. Looking for *walking* just below the sill ($N_f = 8$)
... or *forcing* a conformal theory to walk ($N_f = 4\ell + 8h$)
3. Checking that this yields a light ($m_h > 0!$), dilatonic Higgs — via low-energy effective action

COMPOSITE HIGGS & partially composite top

1. Many opportunities for lattice in calculating low-energy constants
($SU(4) + 2$ reps)
2. Constraints from LHC data may be premature — models aren't perfect

