



THE UNIVERSITY
of ADELAIDE

ISOSPIN BREAKING EFFECTS ON NUCLEON STRUCTURE FROM FULLY DYNAMICAL QCD+QED

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The University of Adelaide*

QCDSF Collaboration

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Granada, Spain*

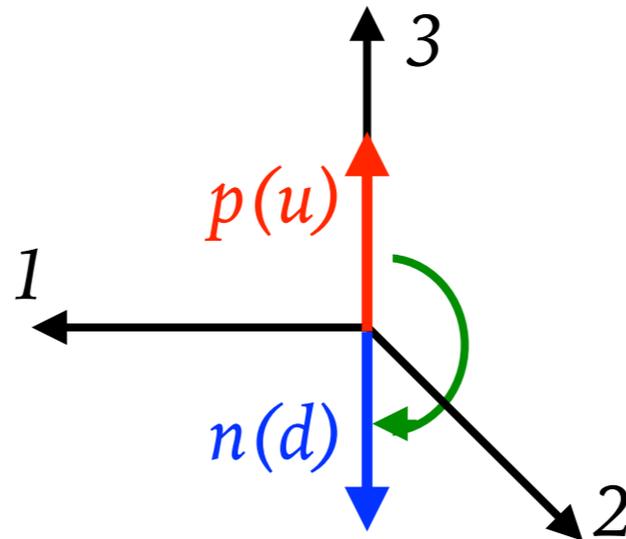
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CHARGE SYMMETRY

u quarks in the proton \equiv d quarks in the neutron

- Explicitly: *invariance of strong interaction under a rotation of 180° about the '2' axis in isospin space.*



- For form factors:

$$G_{E/M}^{p,u} = G_{E/M}^{n,d}$$

$$G_{E/M}^{p,d} = G_{E/M}^{n,u}$$

CHARGE SYMMETRY

Decompose form factors into their flavour contributions

$$p = e^u u^p + e^d d^p + \mathcal{O}_N$$

$$n = e^d d^n + e^u u^n + \mathcal{O}_N$$

total p/n form factor

connected d -quark
contribution to n FF

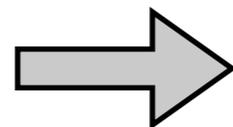
total disconnected
contribution

$$\mathcal{O}_N = \frac{2}{3} \ell G^u - \frac{1}{3} \ell G^d - \frac{1}{3} \ell G^s$$

Under charge symmetry:

$$u \longleftrightarrow d$$

$$p \longleftrightarrow n$$



$$p = e^u u^p + e^d d^p + \mathcal{O}_N$$

$$n = e^d u^p + e^u d^p + \mathcal{O}_N$$

CHARGE SYMMETRY

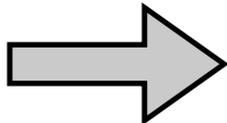
u quarks in the proton \equiv d quarks in the neutron

- ▶ Experimental determinations of $G_{E,M}^s(Q^2)$ rely on charge symmetry
- ▶ (As does the inclusion of neutron data for Qweak)
- ▶ EM and weak interactions give access to different combinations of $G^{p,(u/d/s)}$

$$G^{p,\gamma} = \frac{2}{3}G^{p,u} - \frac{1}{3}(G^{p,d} + G^{p,s})$$

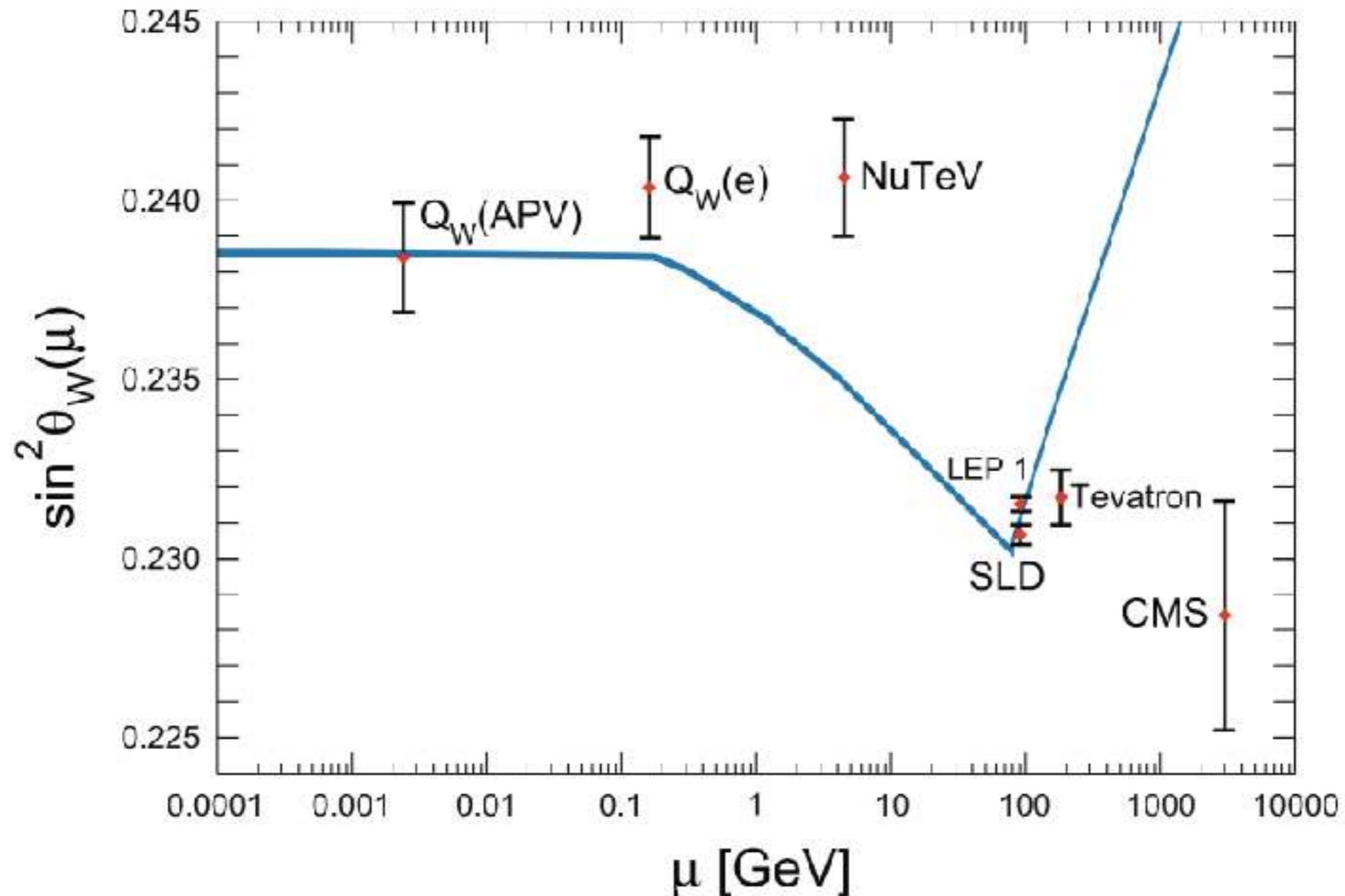
$$G^{p,Z} = \left(1 - \frac{8}{3}\sin^2\theta_W\right)G^{p,u} - \left(1 - \frac{4}{3}\sin^2\theta_W\right)(G^{p,d} + G^{p,s})$$

- ▶ Assume charge symmetry ($G^{p,u} = G^{n,d}$, $G^{p,d} = G^{n,u}$, $G^{p,s} = G^{n,s}$)

 $G_{E/M}^{p,s} = (1 - 4\sin^2\theta_W)G_{E/M}^{p,\gamma} - G_{E/M}^{n,\gamma} - G_{E/M}^{p,Z}$

NUTEV & $\sin^2\Theta_W$

- NuTeV report a 3-sigma discrepancy from the Standard Model



Relies on assumption that CSV is negligible

CSV IN PDFS

- Under charge symmetry $u^p(x) = d^n(x)$
- Many experiments make this assumption (e.g. NuTeV)
- Use Lattice simulations to constrain the violation of charge symmetry

$$\delta u(x) = u^p(x) - d^n(x)$$

$$\delta d(x) = d^p(x) - u^n(x)$$

- Lattice, however, can only access (the lowest couple of) moments

$$\langle x^{m-1} \rangle = \int_0^1 dx x^{m-1} [q(x) + (-1)^m \bar{q}(x)]$$

- E.g. second moment of spin-independent

$$\delta u = \langle x \rangle_u^p - \langle x \rangle_d^n$$

$$\delta d = \langle x \rangle_d^p - \langle x \rangle_u^n$$

- or first moment of spin-dependent

$$\delta \Delta u = \Delta u_p - \Delta d_n$$

$$\delta \Delta d = \Delta d_p - \Delta u_n$$

LATTICE QCD SET-UP

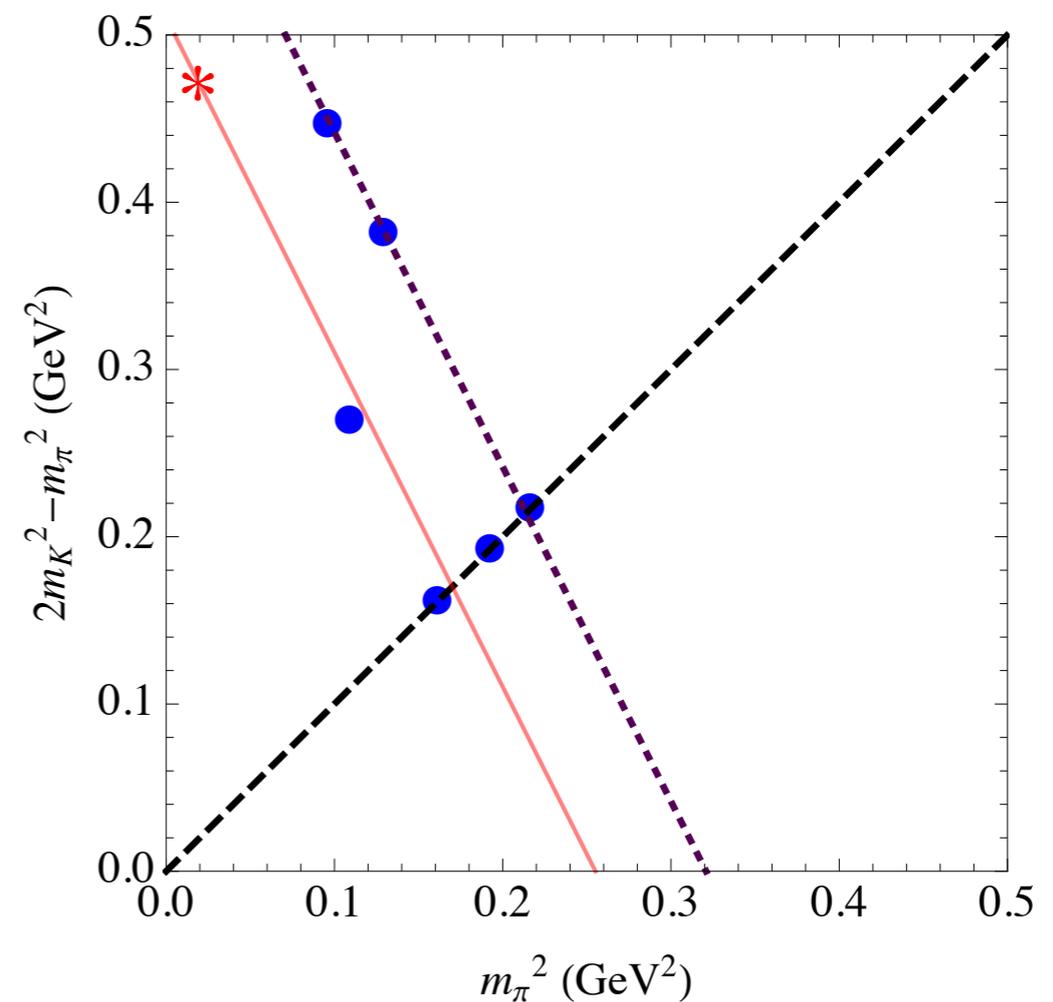
- $N_f = 2 + 1$ $O(a)$ -improved Clover fermions (“SLiNC” action)
- Tree-level Symanzik gluon action (plaq + rect)
- Novel method for tuning the quark masses

- keep the singlet quark mass fixed

$$\bar{m}^R = \frac{1}{3}(2m_l^R + m_s^R)$$

- at its physical value \bar{m}^{R*}

- Multiple V, a, m_q



FORM FACTOR CSV

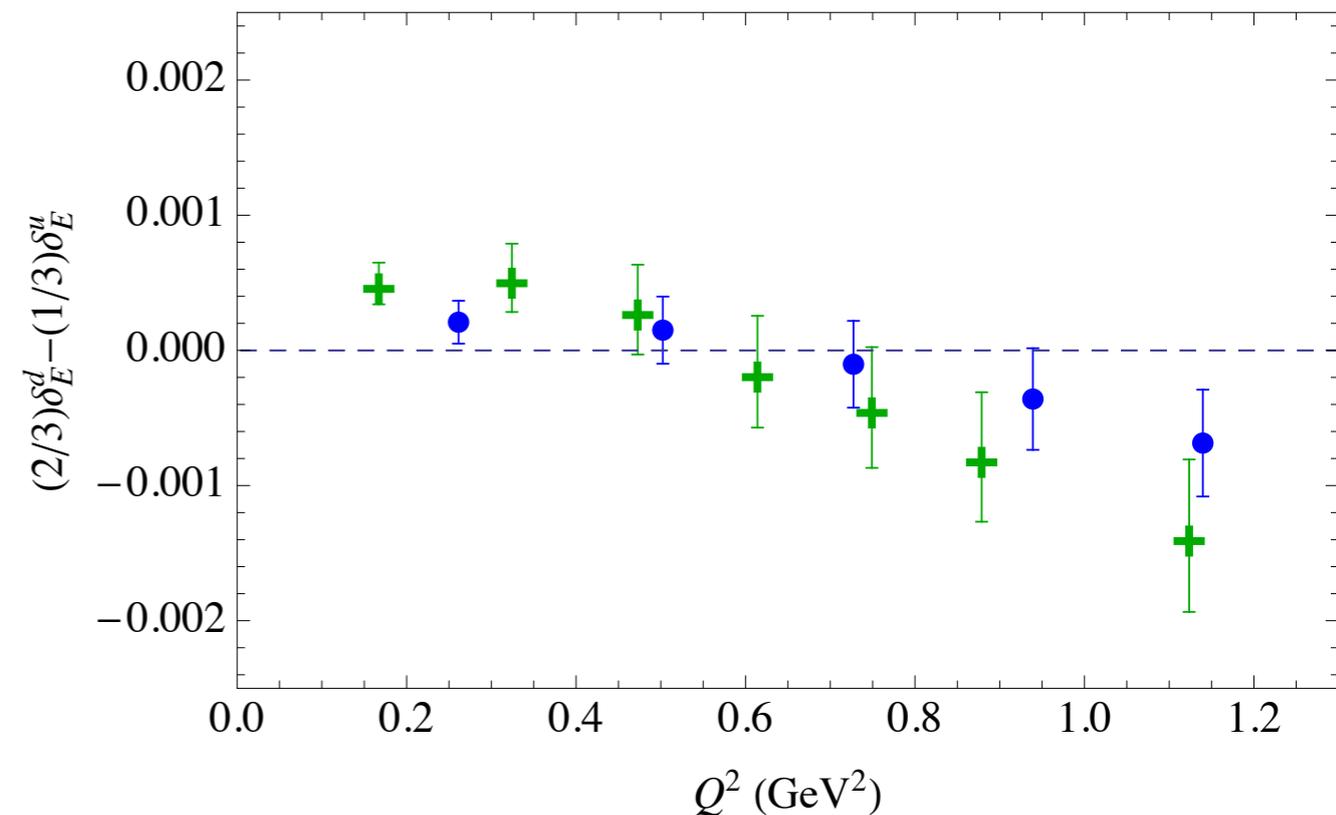
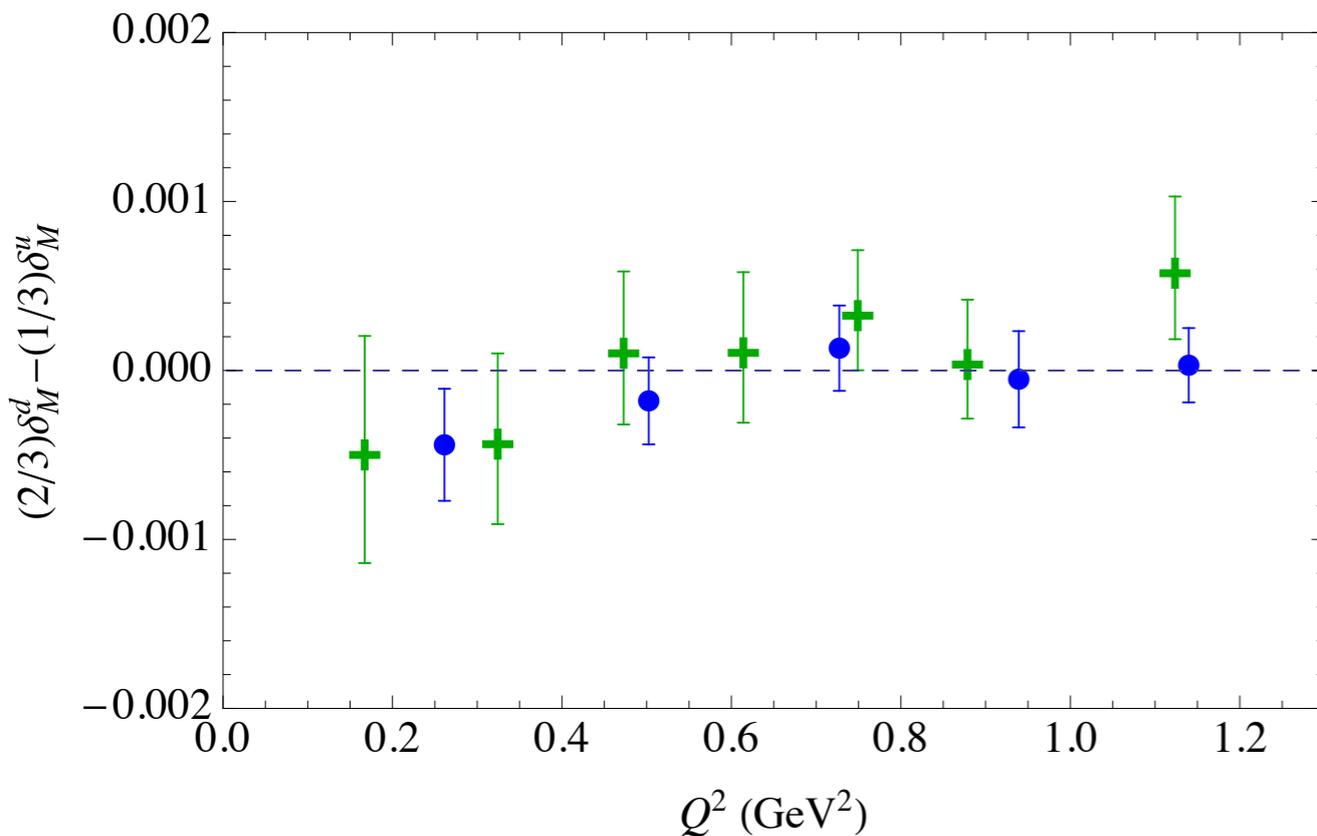
[CSSM/QCDSF PRD91 (2015) 113006]

- Determine the degree to which charge symmetry is violated in EM form factors by:
 - Combining χ PT fits to isospin-averaged Lattice QCD hyperon FFs
 - Input m_u/m_d from experiment (or FLAG)

FORM FACTOR CSV

[CSSM/QCDSF PRD91 (2015) 113006]

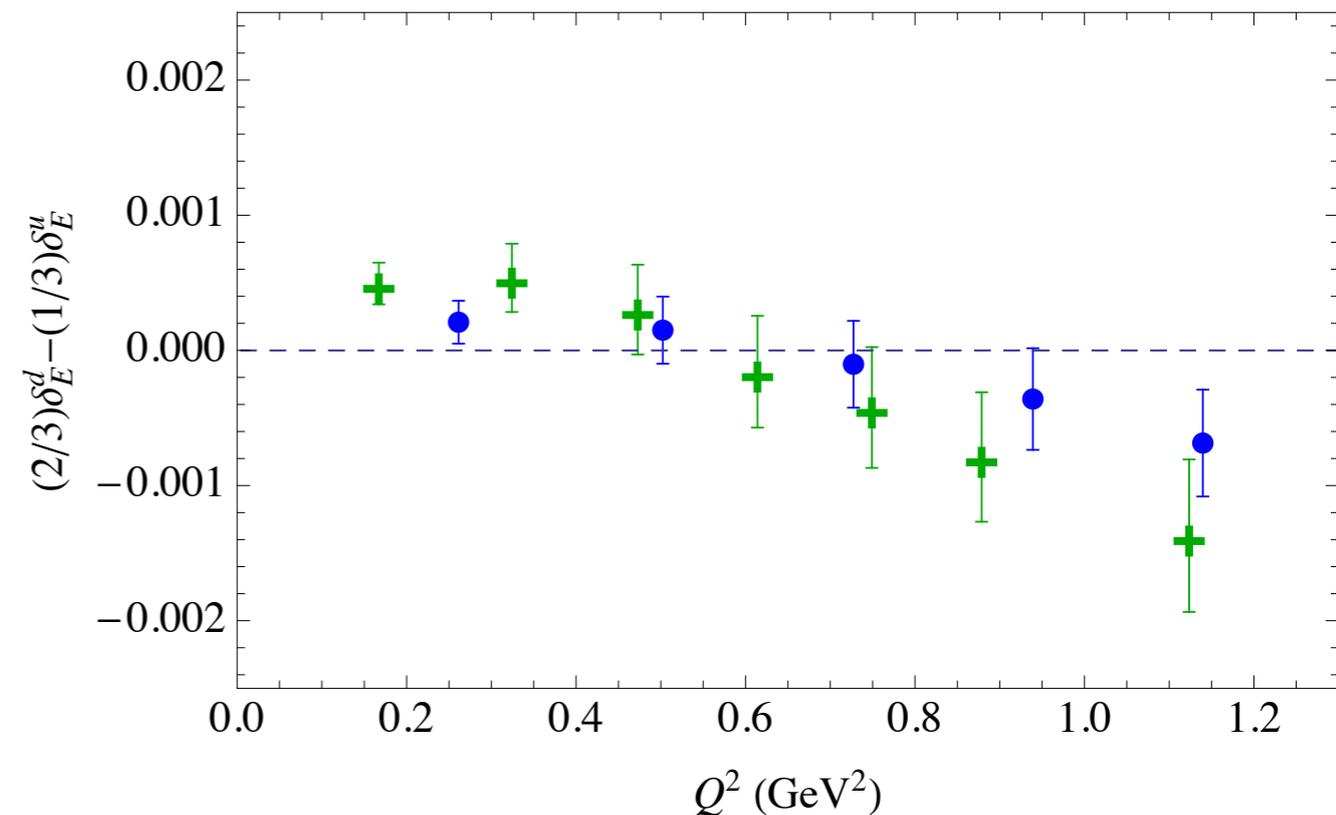
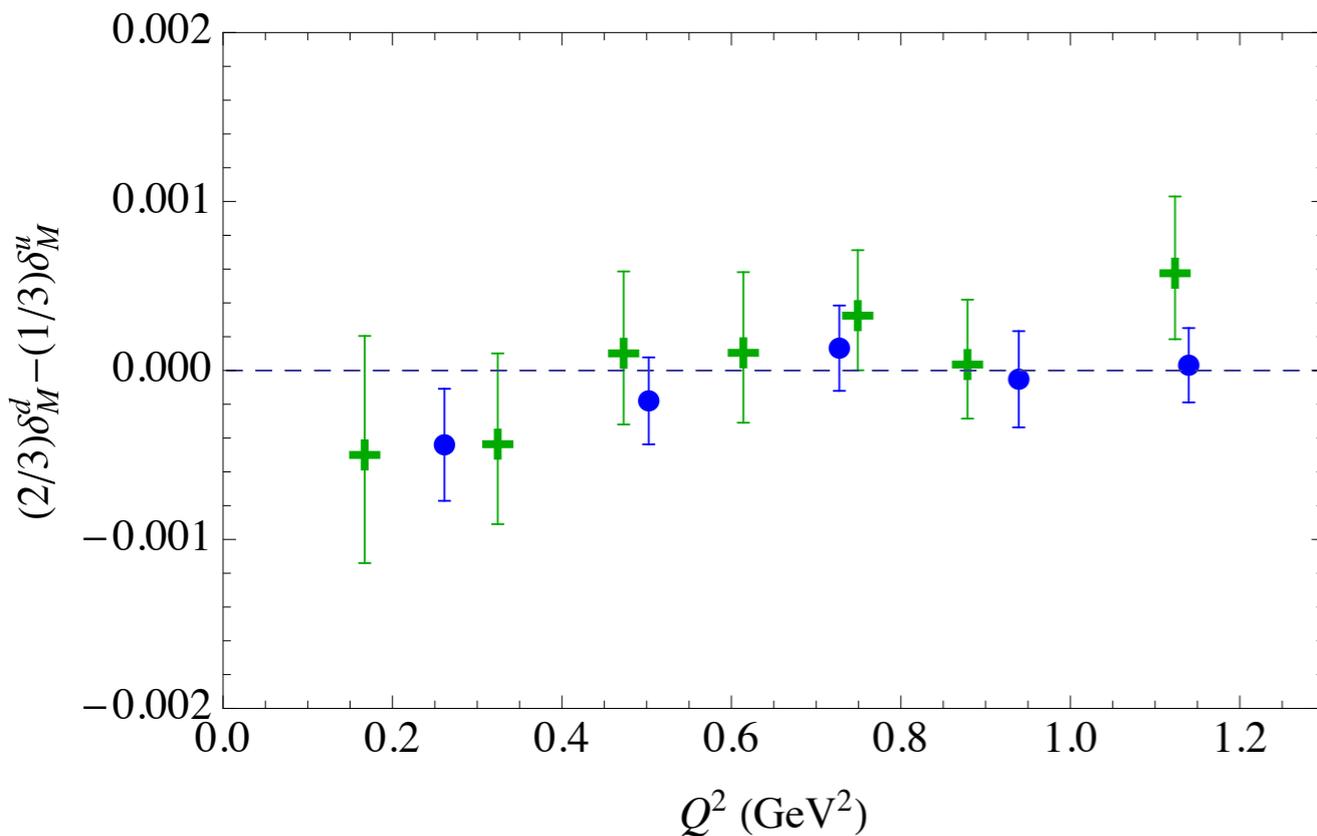
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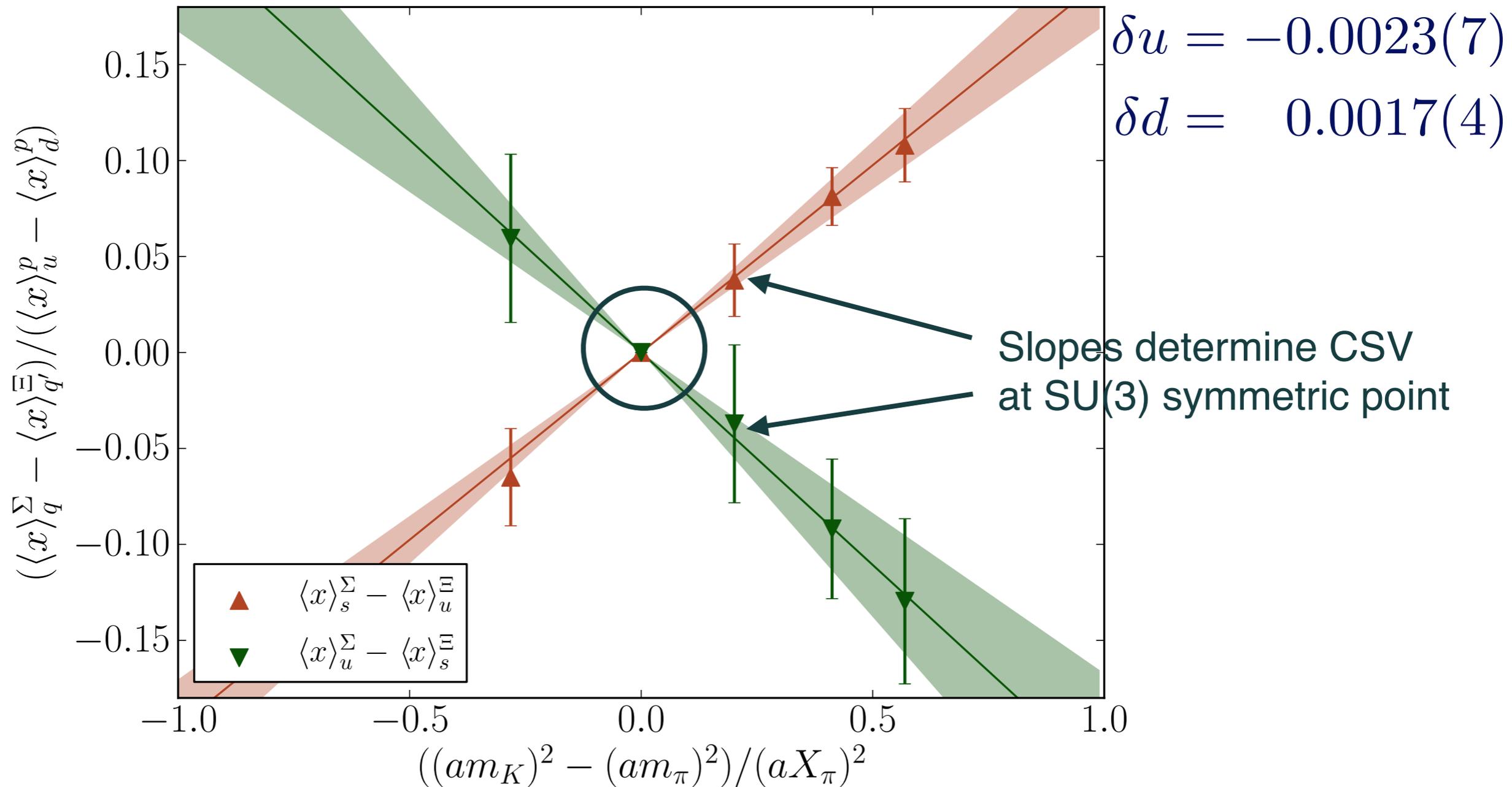
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Charge symmetry satisfied to better than **0.2% (QCD)**

Violations due to **QED?**

Chiral corrections in **Shanahan, Thomas & Young, PRD(2013)094515**



- Reduce NuTeV Standard Model discrepancy by ~ 1 sigma

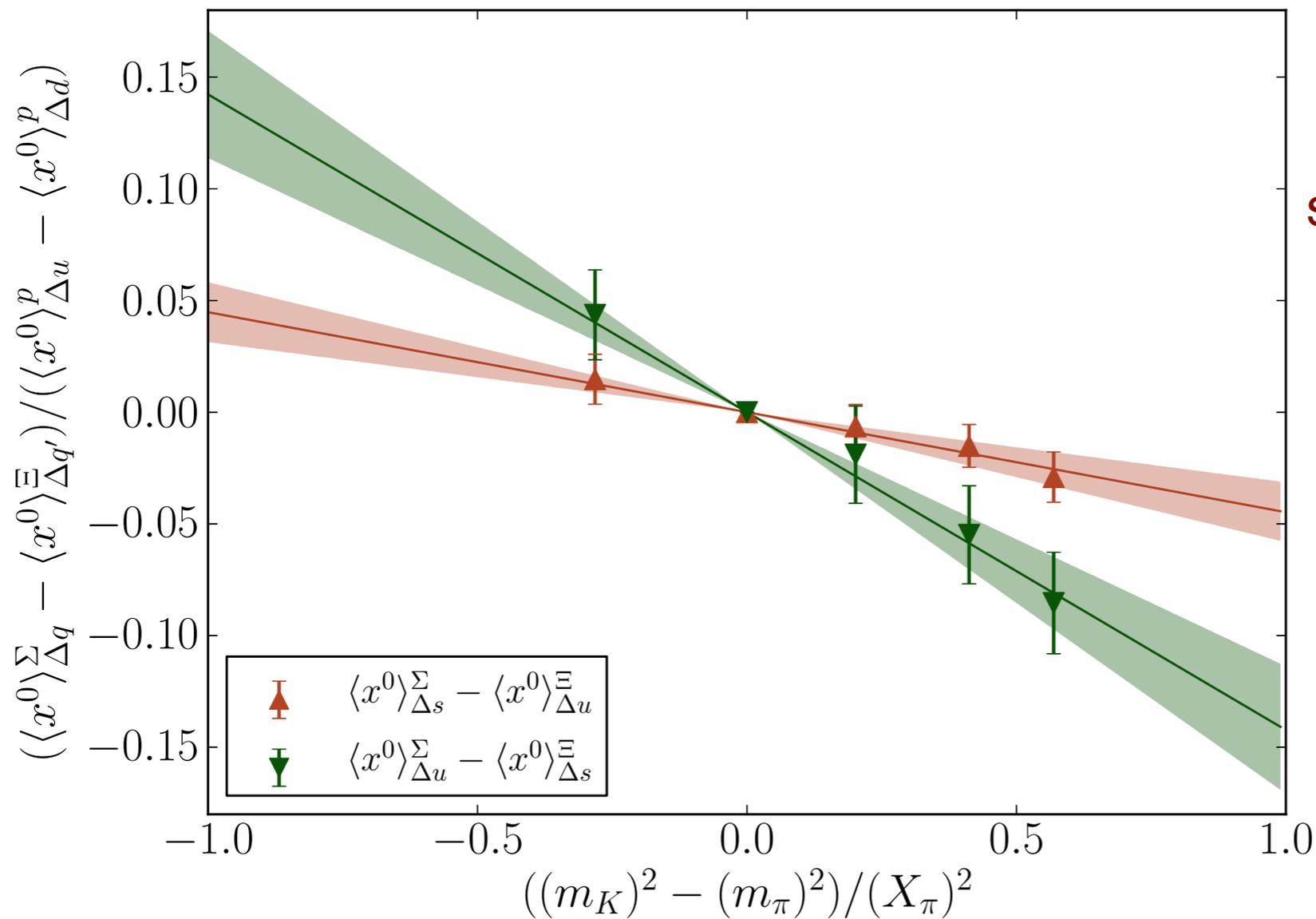
SPIN DEPENDENT CSV

[QCDSF, 1204.3492 (PLB)]

► Repeat procedure for

$$\delta\Delta u^m = \int_0^1 dx x^m [\Delta u^p(x) - \Delta d^n(x)]$$

$$\delta\Delta d^m = \int_0^1 dx x^m [\Delta d^p(x) - \Delta u^n(x)]$$



same sign for $\delta\Delta u$ and $\delta\Delta d$



~1% correction to Bjorken sum rule

LATTICE QCD+QED SET-UP

JHEP 1604, 093 (2016);
J.Phys. G43 no.10, 10LT02 (2016)

- Non-compact QED
- Gauge coupling corresponding to $\alpha_{QED}=0.1$
- Quark masses tuned to $SU(3)_{\text{sym}}$ point via the “Daschen Scheme”

$$m_{\pi}^{u\bar{u}} = m_{\pi}^{d\bar{d}} = m_{\pi}^{s\bar{s}}$$

- Zero modes?

LATTICE QCD+QED SET-UP

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- ▶ Zero modes?



- ▶ Eliminated by additional gauge-fixing of Uno & Hayakawa (2008) — on valence quarks
- ▶ Finite volume effects? Not yet

LATTICE QCD+QED SET-UP

$$V=32^3 \times 64, a=0.068 \text{ fm}$$

- Simulate with 3 different valence quark charges

- $u : +2/3$ $m_{\pi}^{n\bar{n}} = 408(3) \text{ MeV}$

- $d : -1/3$ $m_{\pi}^{d\bar{d}} = 409(1) \text{ MeV}$

- $n : 0$ $m_{\pi}^{u\bar{u}} = 407(3) \text{ MeV}$

Daschen:

$$m_{\pi}^{u\bar{u}} = m_{\pi}^{d\bar{d}} = m_{\pi}^{n\bar{n}}$$

- Construct baryons

flavour	Q	flavour	Q	flavour	Q
uuu	+2	ddu	0	nnu	+2/3
uud	+1	ddd	-1	nnd	-1/3
uun	+4/3	ddn	-2/3	nnn	0

- Isolate individual quark contributions, e.g.

u^{uud} u quark in (uud)

d^{ddn} n quark in (ddn)

FORM FACTORS

[Unrenormalised]

- Z_V depends on the charge of the active quark

[Also observed in Boyle et al., 1706.05293 (today!)]

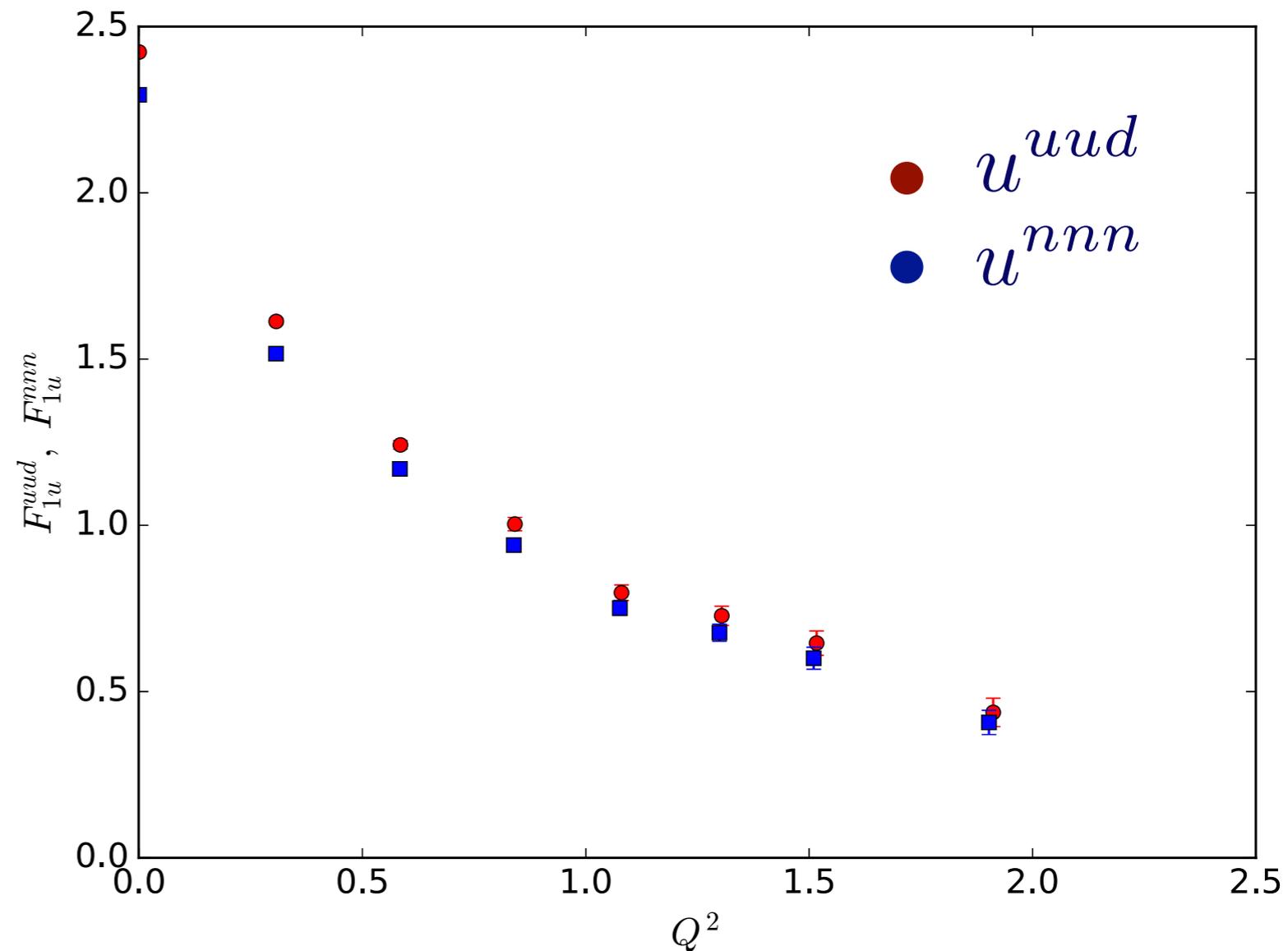
- From dipole fits

$$r_{1u}^{nnn} = 0.575(6)$$

$$r_{1u}^{uud} = 0.570(6)$$

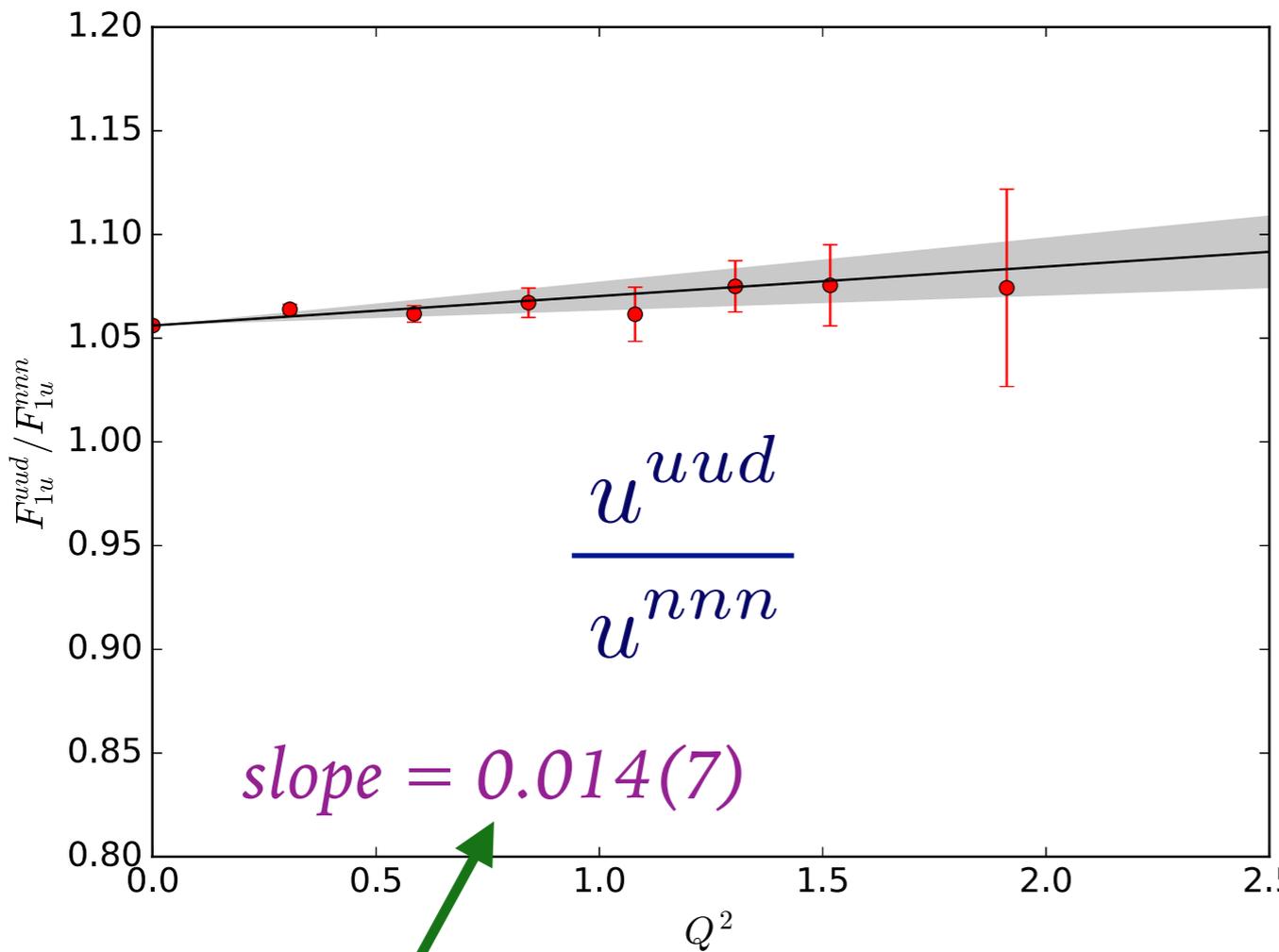
- Form factor shapes similar

➔ distinguish via ratios

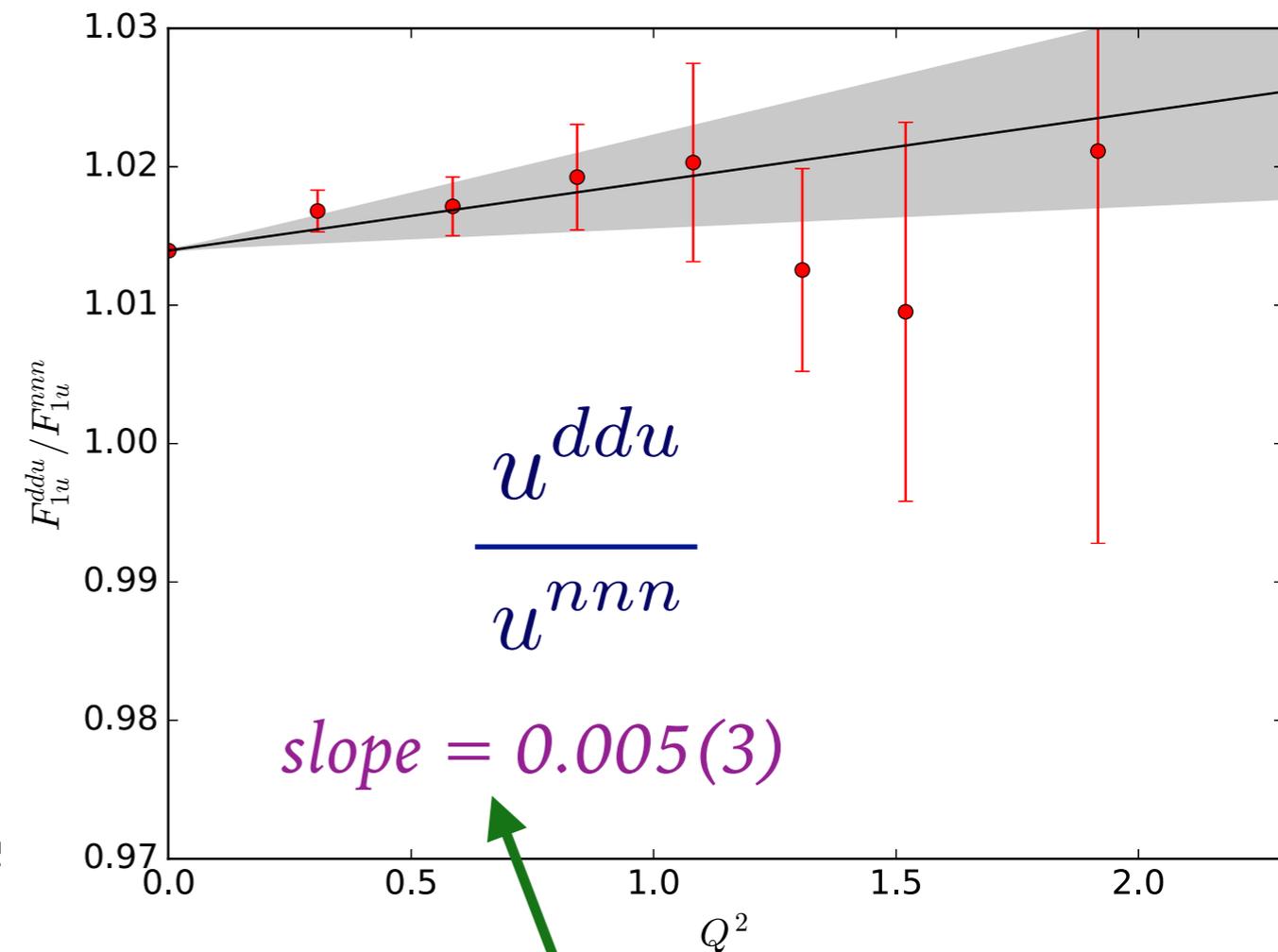


FORM FACTORS – DOUBLY REPRESENTED QUARK

- Coulomb attraction/repulsion, expect smaller/faster fall-off with Q^2



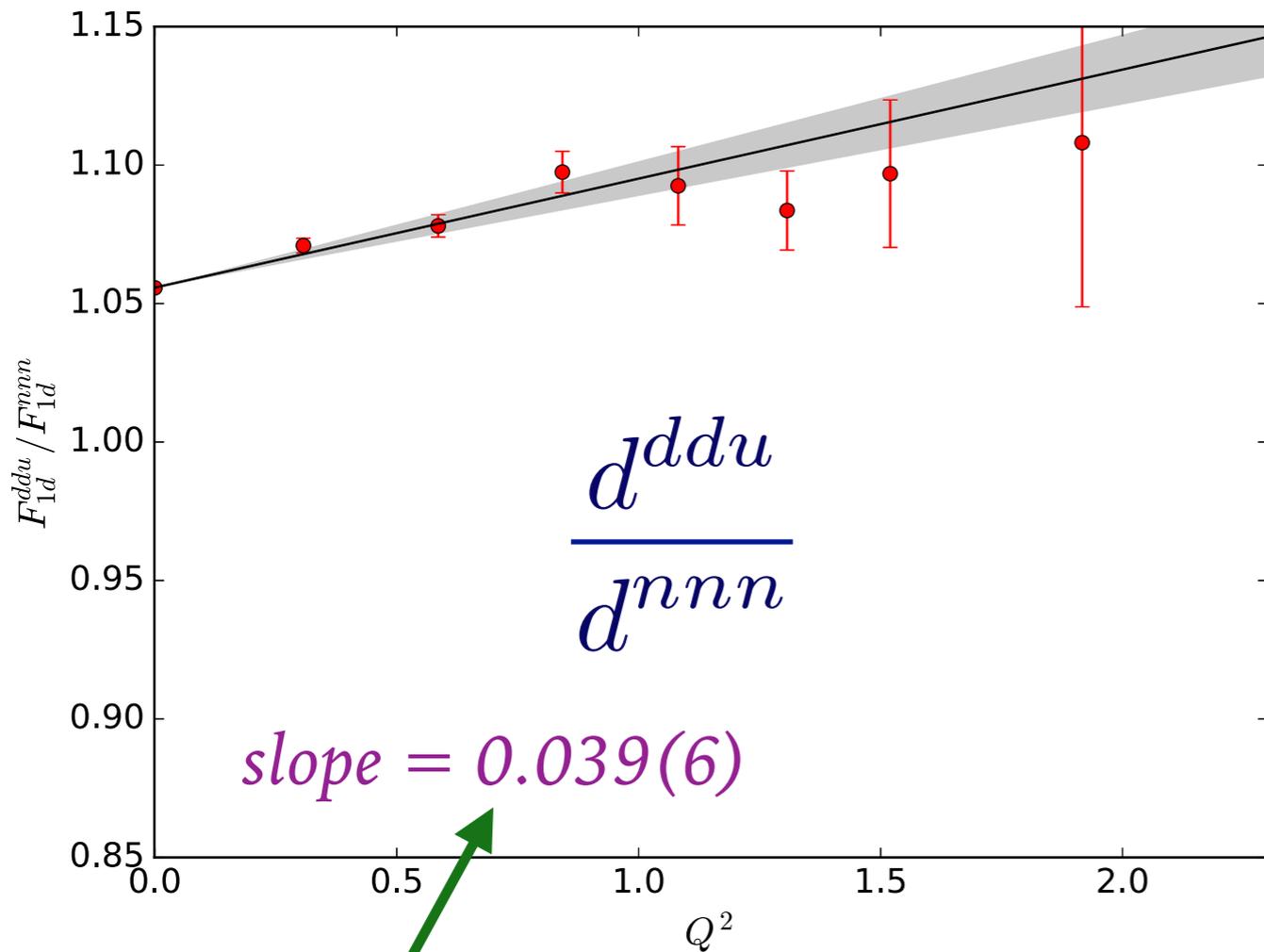
Counterintuitive? FV effect?



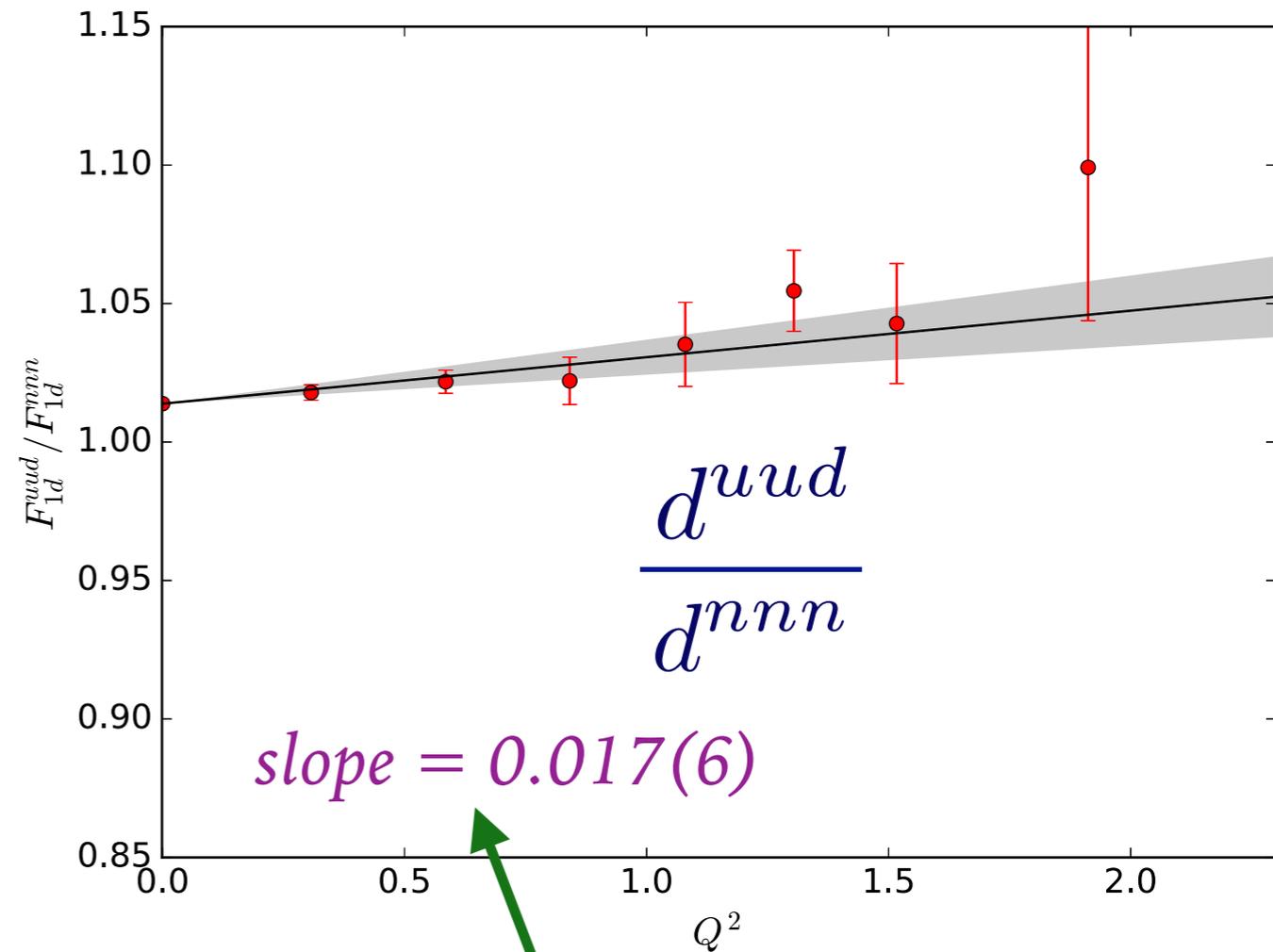
Competing effects? Perhaps ok?

FORM FACTORS – SINGLY REPRESENTED QUARK

- Coulomb attraction/repulsion, expect smaller/faster fall-off with Q^2



Signature for Coulomb attraction?

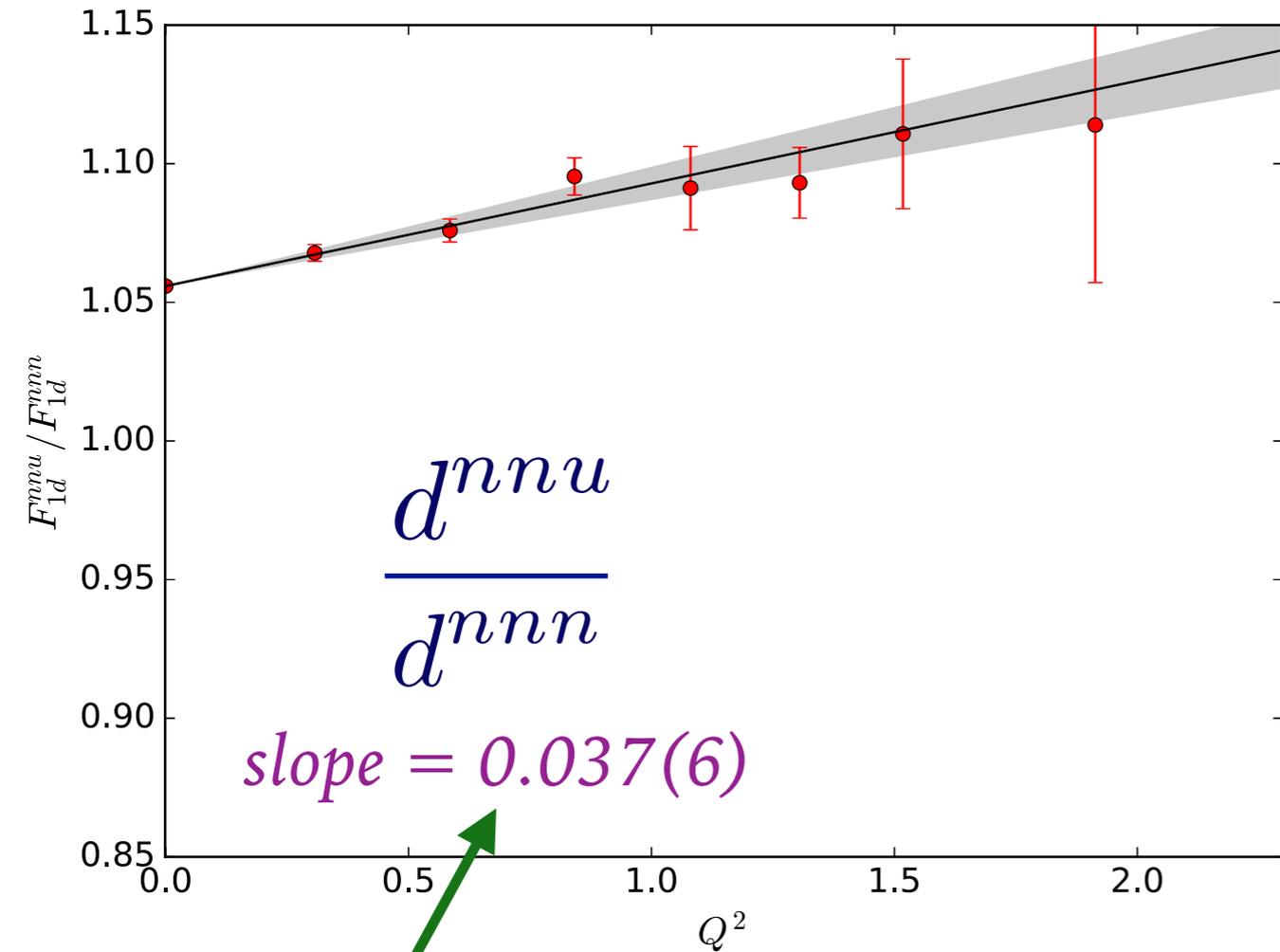


Expect similar Coulomb attraction.

FV effect due to $Q_{uud} = +1$?

FORM FACTORS

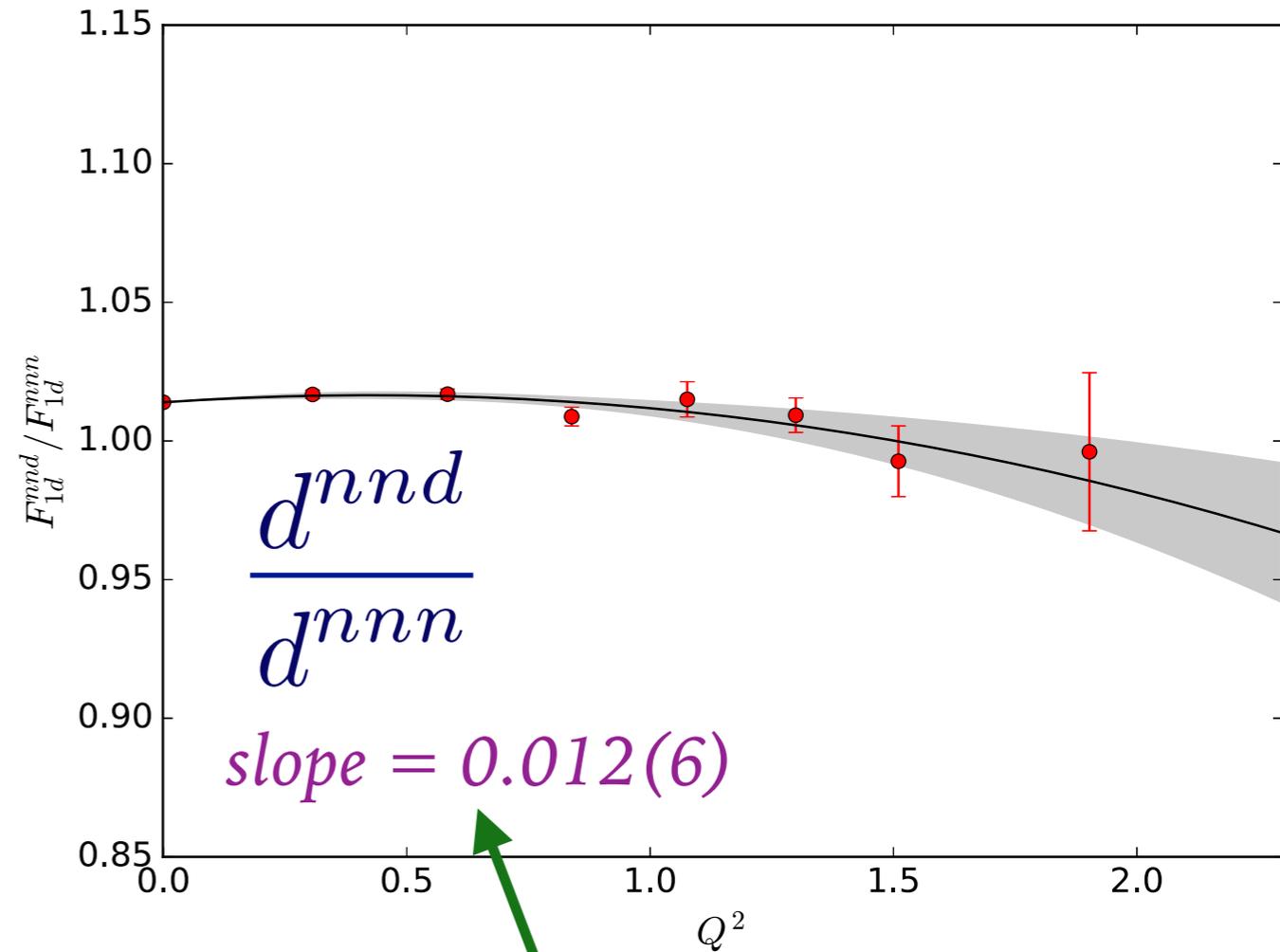
- Construct combination that should have no Coulomb effects (naive QM)



Umm..

Beyond QM?

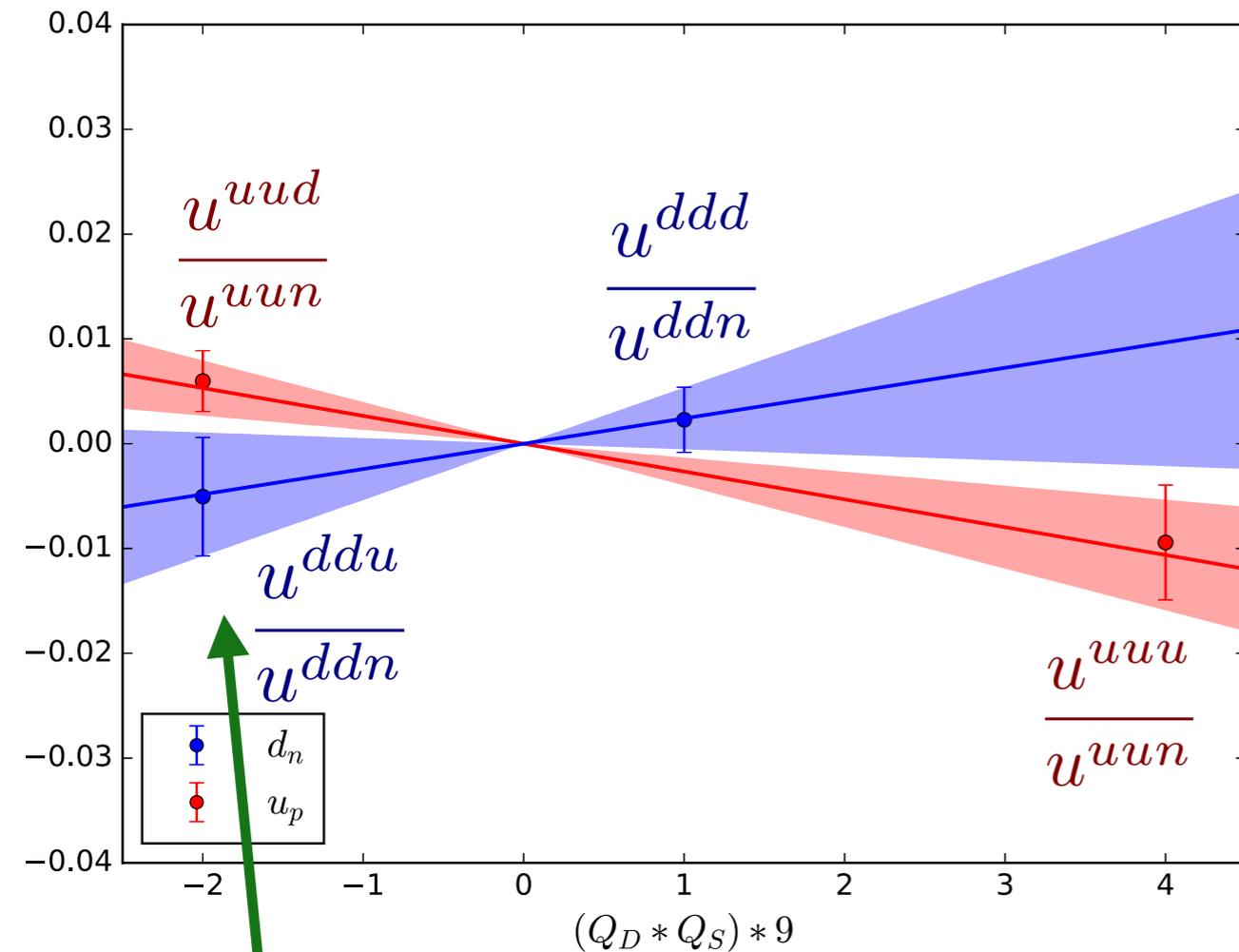
FV effect?



Similar effect, but smaller

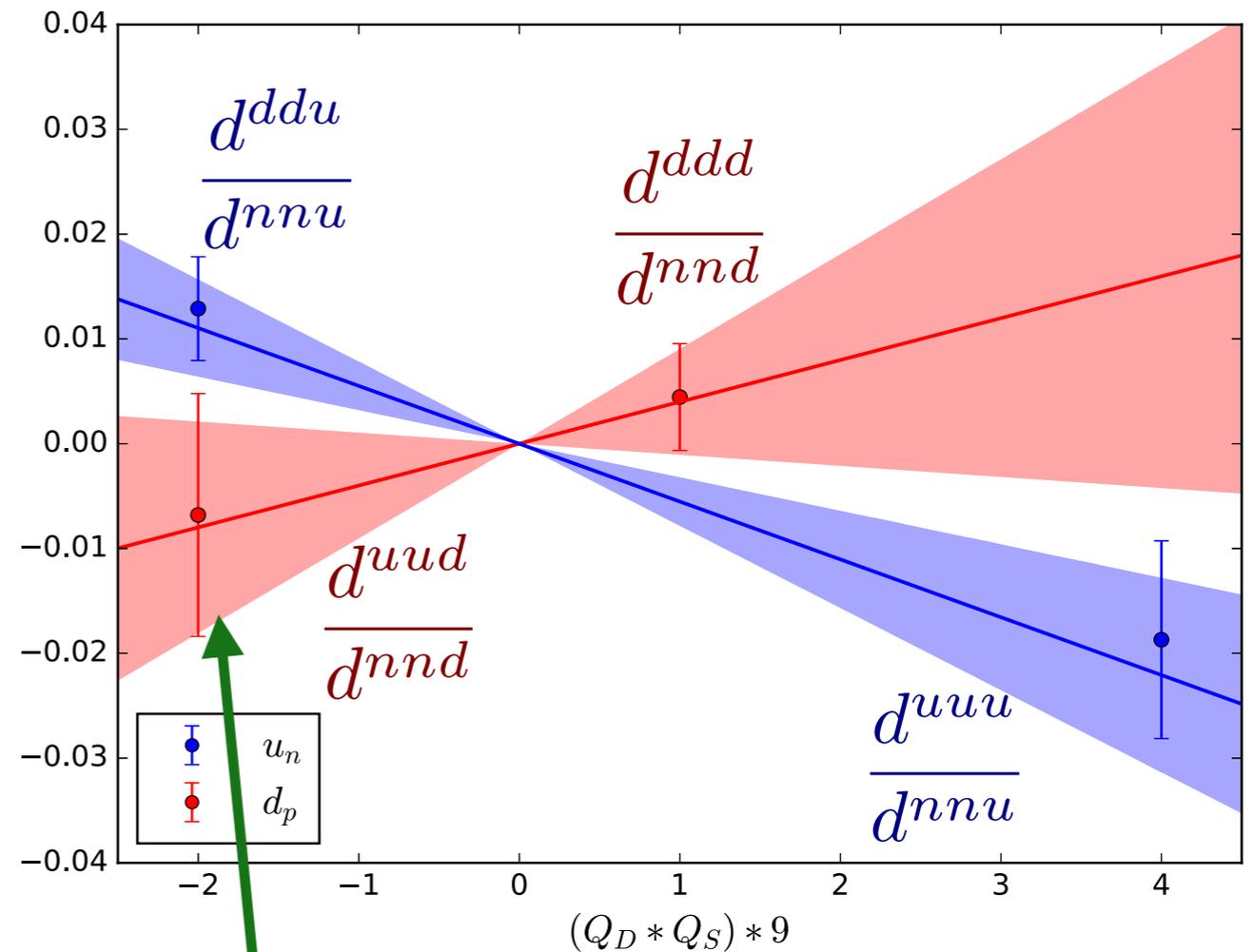
FORM FACTORS - CSV

- Attempt to gain insights into CSV through the following combinations



difference between these
2 points like

$$\delta u = u_p - d_n (\equiv u^{uud} - u^{ddu})$$



while difference here

$$\delta d = d_p - u_n (\equiv d^{uud} - d^{ddu})$$

AXIAL CHARGE

- To compute g_A , usual procedure is to assume isospin symmetry and compute

$$g_A = u^p - d^p \quad \text{i.e.} \quad \langle p | \bar{u} \gamma_3 \gamma_5 u - \bar{d} \gamma_3 \gamma_5 d | p \rangle$$

- Experimentally determined via $n \rightarrow p e^- \bar{\nu}$

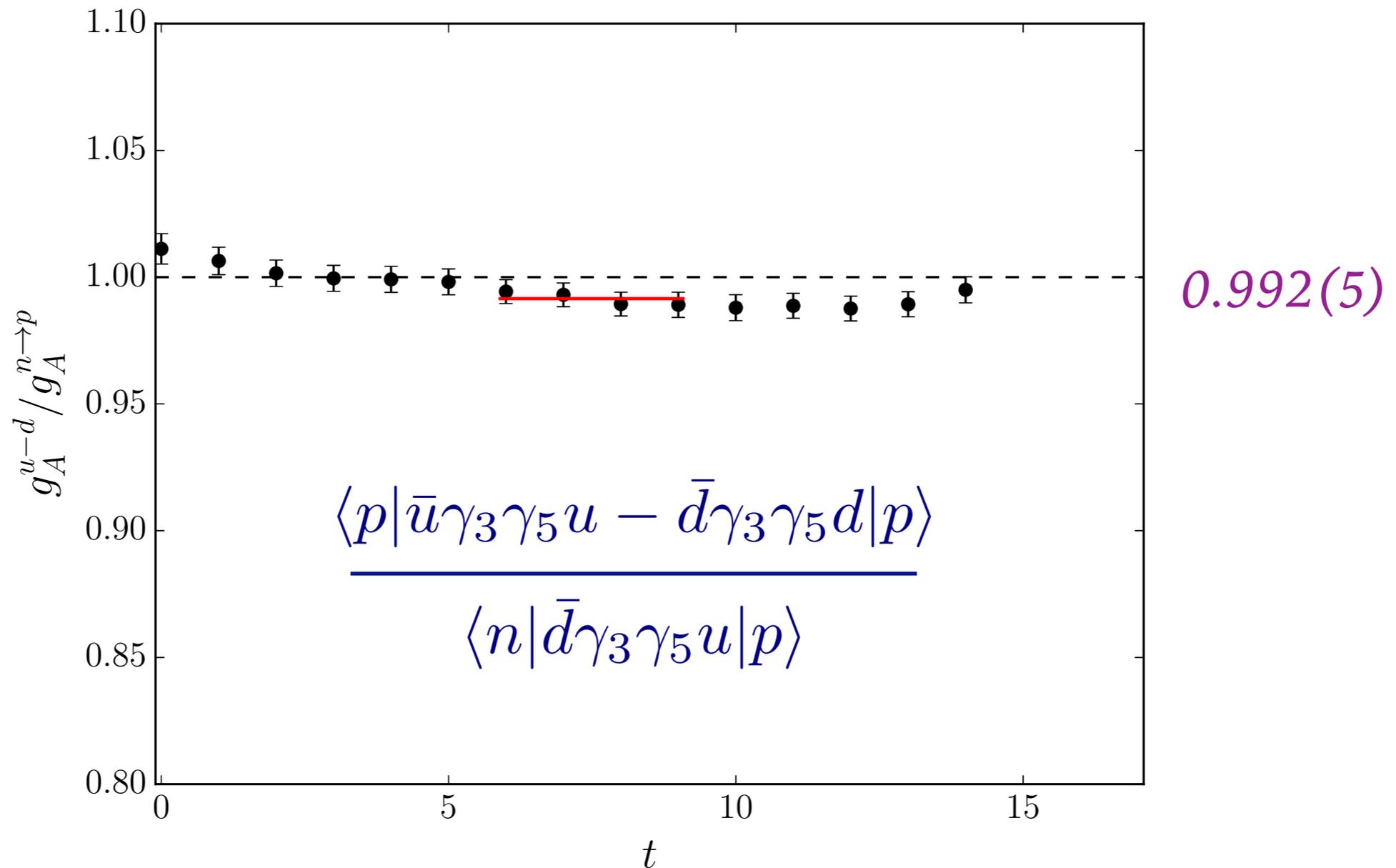
$$\text{i.e.} \quad \langle n | \bar{d} \gamma_3 \gamma_5 u | p \rangle$$

- Can we observe violations due to isospin breaking due to quark charges?

- Compute

$$\frac{\langle p | \bar{u} \gamma_3 \gamma_5 u - \bar{d} \gamma_3 \gamma_5 d | p \rangle}{\langle n | \bar{d} \gamma_3 \gamma_5 u | p \rangle}$$

AXIAL CHARGE

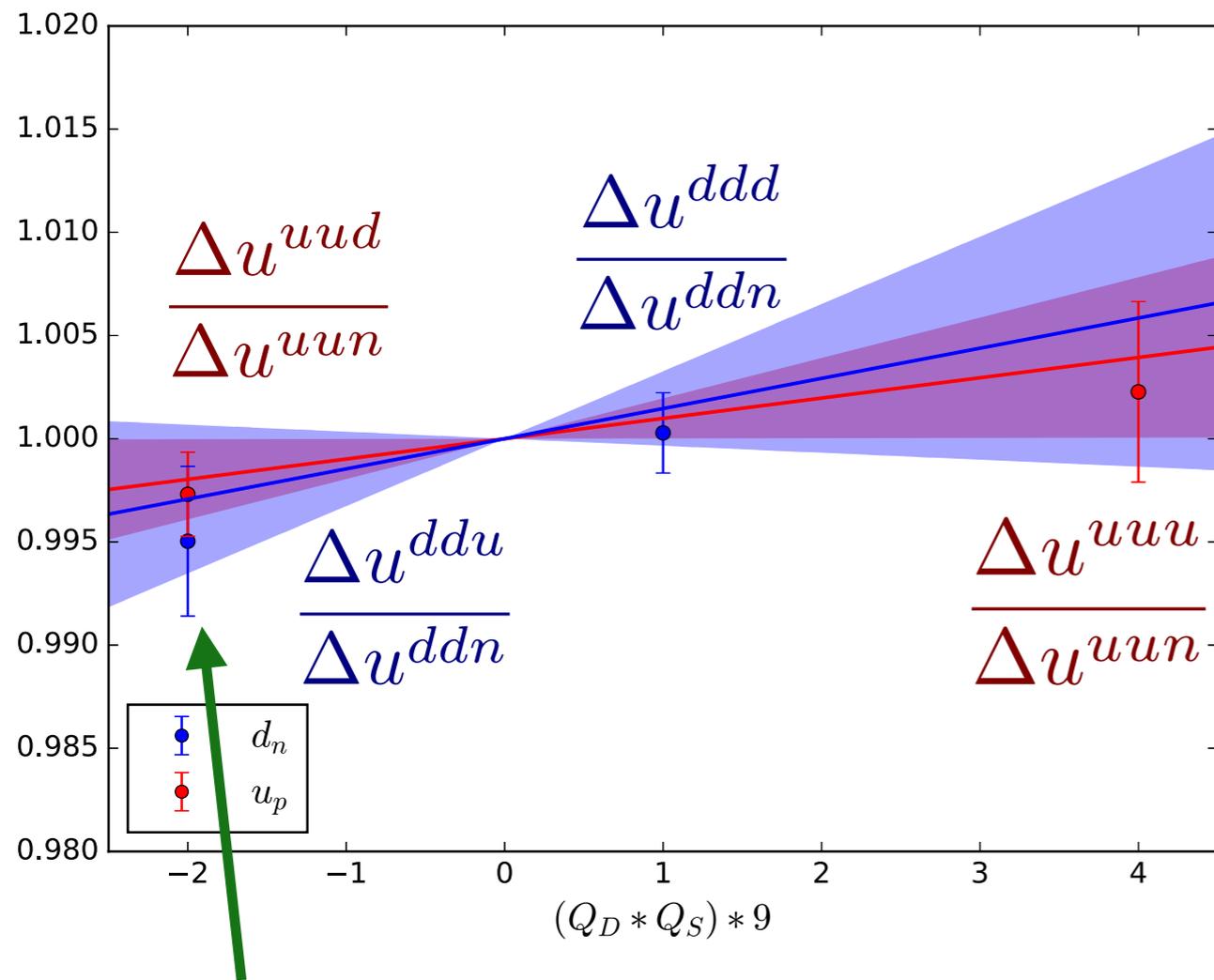


- Need better treatment of excited states
- Evidence for $\sim (0.5-1)/10$ % effect

CSV IN SPIN-DEPENDENT PDFs

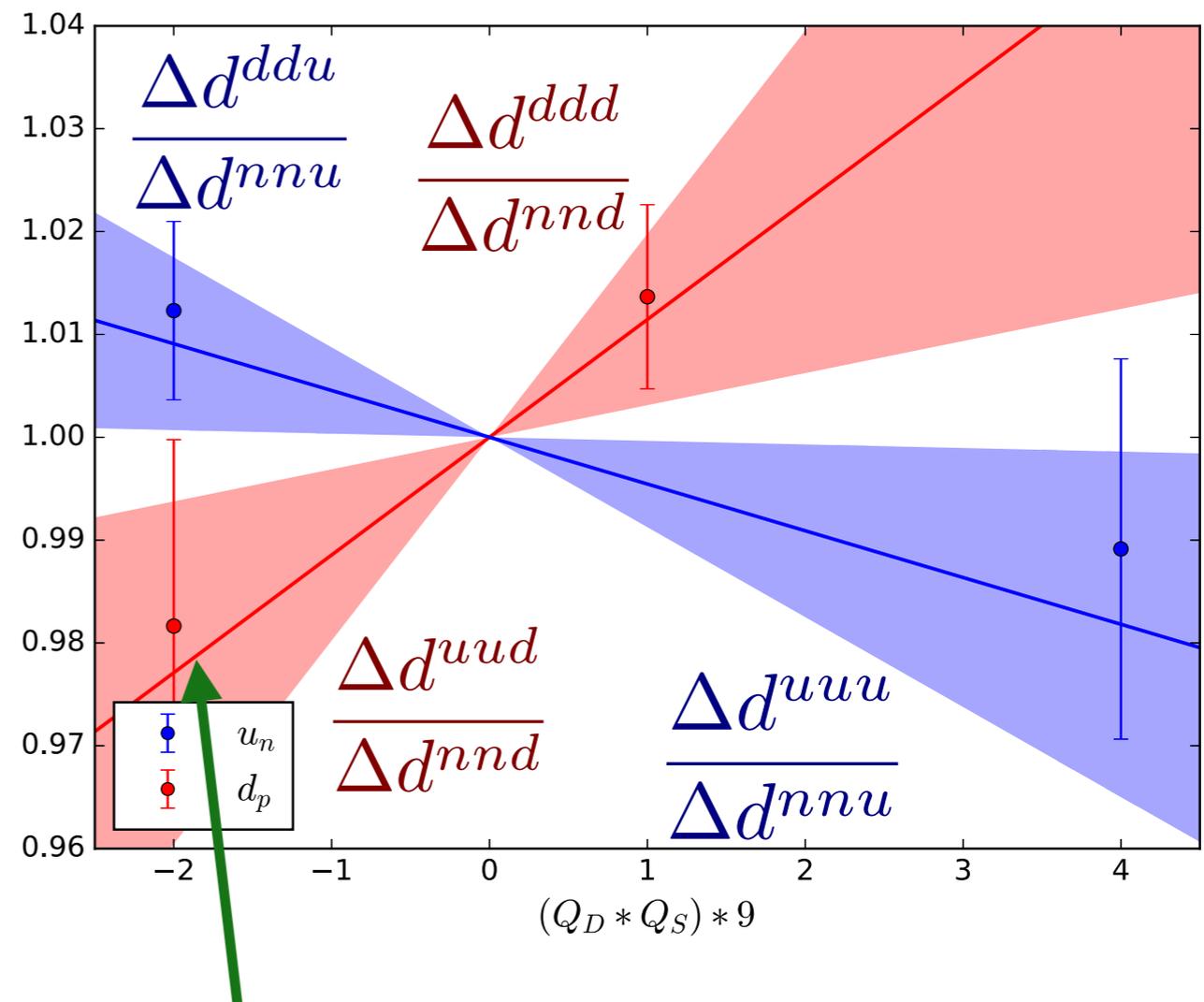
$\delta\Delta u$ $\delta\Delta d$

- To cancel potentially charge-dependent Z_A
- Construct ratios and compare charged quark sectors



difference gives $\delta\Delta u = \Delta u_p - \Delta d_n$

Consistent with zero



while here $\delta\Delta d = \Delta d_p - \Delta u_n$

Evidence for $\sim (3/10) \%$

SUMMARY AND OUTLOOK

- Had a first look at QED effects in nucleon matrix elements
- Form factors:
 - Evidence for Coulomb attraction for u quark in neutron
 - Hints at (small) CSV effects due to QED
- Axial charge:
 - Isospin-breaking effects due to quark charges appear to have $<1\%$ effect on $g_A = \Delta u - \Delta d$
 - Evidence for negligible $\text{CSV}^{\text{QED}} \delta\Delta u$
but non-zero $\delta\Delta d$
- Much work to be done on systematics, e.g. FV effects (including radiative corrections)