

# CLS 2+1 flavor simulations at physical light- and strange-quark masses

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*Representing the CLS effort  
Together with Stefan Schaefer and Jakob Simeth*

## 1 Introduction

- The CLS 2+1 flavor ensembles – Key features
- Landscape of CLS ensembles

## 2 Towards the physical point

- Autocorrelation times towards the physical point
- Thermalization strategy
- Current status

## 3 Conclusions and Outlook

# The CLS 2+1 flavor ensembles – Key features

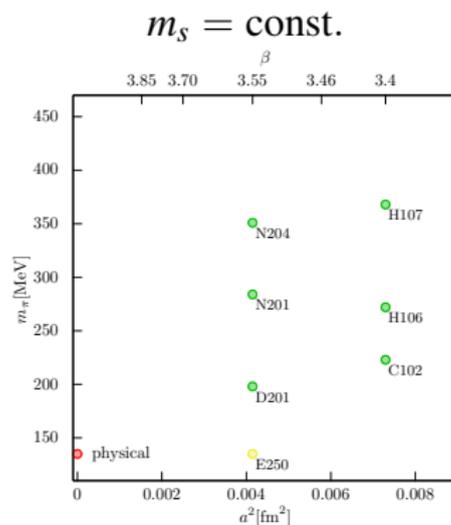
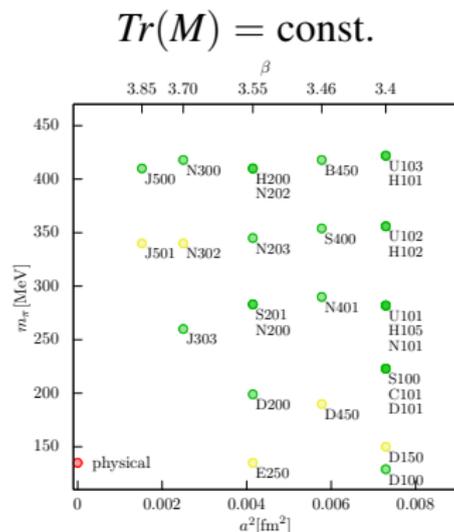
- Open boundary conditions to avoid topological freezing for  $a \rightarrow 0$
- Twisted mass reweighting (for the light quarks)
- Simulation along trajectory with fixed  $Tr(M)$
- Additional simulations along trajectories with fixed strange quark mass  $m_s = \text{const.}$  and with  $m_s = m_l$
- Flexible simulations with OpenQCD

<http://luscher.web.cern.ch/luscher/openQCD/>

- Nested hierarchical integrators
- Hasenbusch-style mass preconditioning with an arbitrary number of pseudofermion pairs
- Rational approximation (+ reweighting) for the strange quark
- Deflation acceleration and chronological solver
- A number of solvers

# CLS 2+1 flavor ensembles: Overview

Bruno *et al.* JHEP 1502 043 (2015); Bali *et al.* PRD 94 074501 (2016)

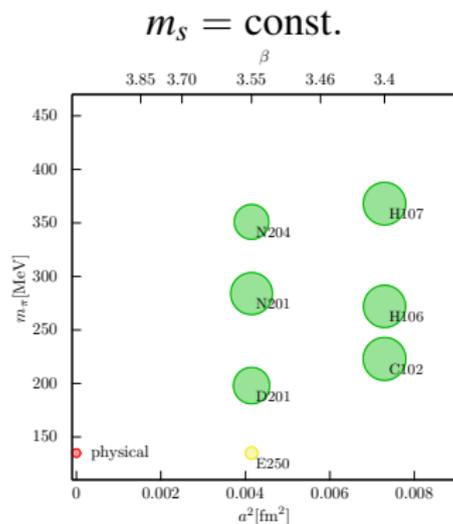
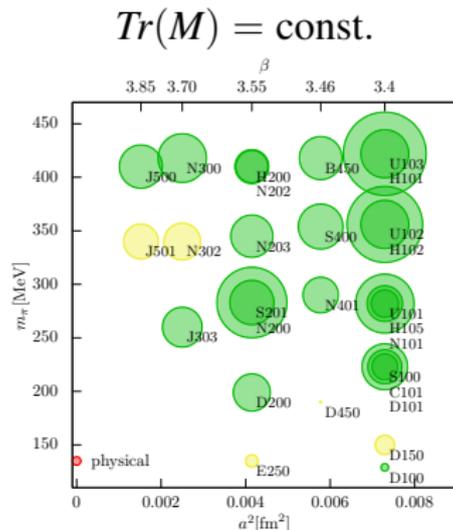


plots by Jakob Simeth, RQCD

- Letters in the name denote the aspect ratio  $T/L$ ; First digit encodes  $\beta$
- Ensembles at 5 lattice spacings and with a range of  $M_\pi \leq 420\text{MeV}$
- Ensembles to control (or exploit) finite volume effects

# CLS 2+1 flavor ensembles: Statistics – area $\propto$ MDU

Bruno *et al.* JHEP 1502 043 (2015); Bali *et al.* PRD 94 074501 (2016)

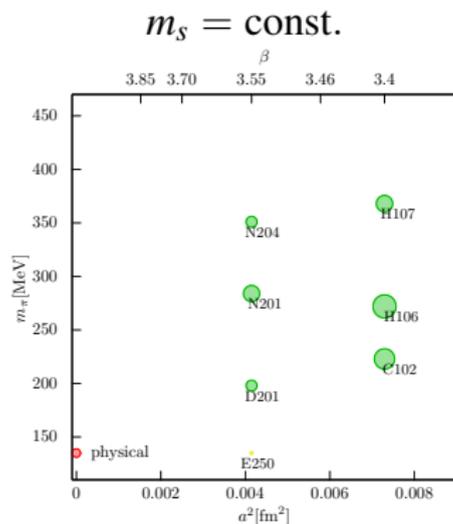
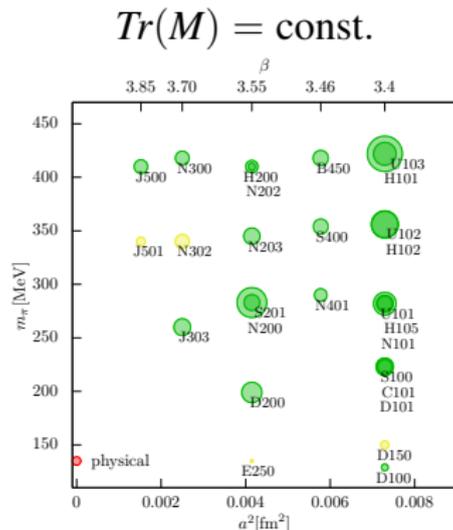


plots by Jakob Simeth, RQCD

- > 4000 MDU for many ensembles  
Typically save 1 configuration every 4 MDU
- target statistics chosen considering largest  $\tau_{int}$  (often YM action density)

# CLS 2+1 flavor ensembles: Statistics – $\text{area} \propto \text{MDU}/\tau_{\text{int}}$

Bruno *et al.* JHEP 1502 043 (2015); Bali *et al.* PRD 94 074501 (2016)



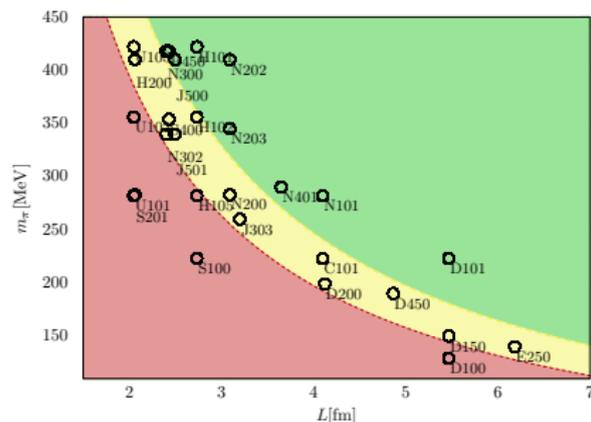
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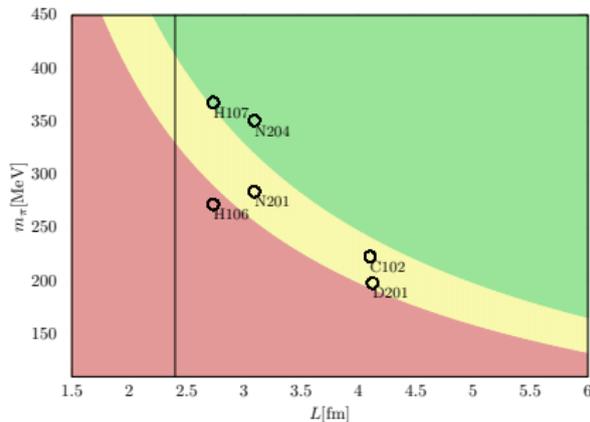
# CLS 2+1 flavor ensembles: Volumes used

Bruno *et al.* JHEP 1502 043 (2015); Bali *et al.* PRD 94 074501 (2016)

$Tr(M) = \text{const.}$



$m_s = \text{const.}$



plots by Jakob Simeth, RQCD

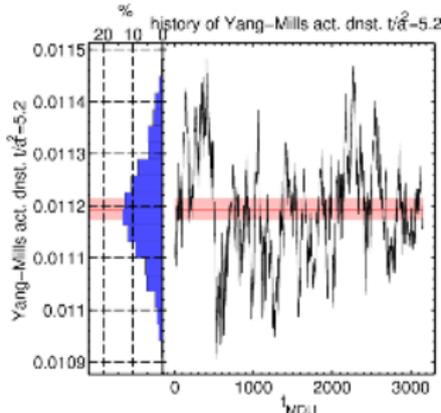
- red:  $m_\pi L \leq 4$ ; yellow:  $4 < m_\pi L \leq 5$ ; green  $5 < m_\pi L$
- Most ensembles with  $m_\pi L \geq 4$
- Some smaller volumes to check finite size effects

# Autocorrelation towards the continuum limit

Action density at  $t_0$  as defined by  $t^2\langle E \rangle = 0.3$

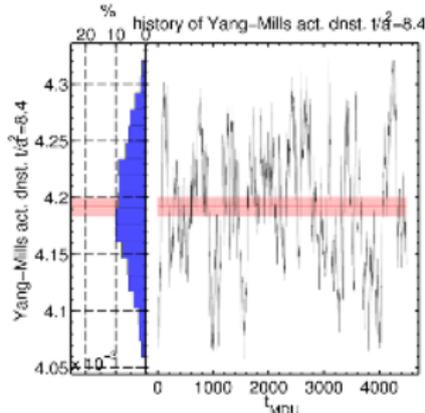
**N203**

$a \approx 0.064\text{fm}$



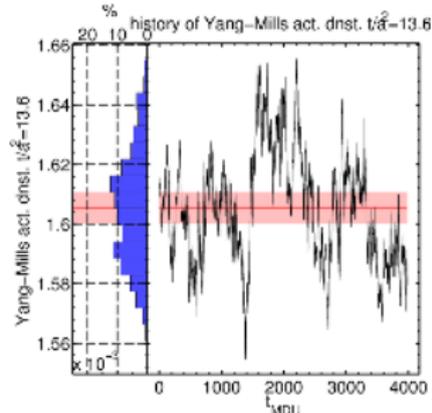
**N302**

$a \approx 0.050\text{fm}$



**J501**

$a \approx 0.039\text{fm}$



$\tau_{\text{int}} = 60(32)$  MDU

$\tau_{\text{int}} = 49(22)$  MDU

$\tau_{\text{int}} = 150(98)$  MDU

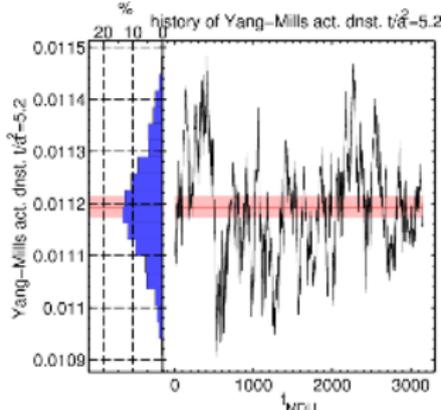
- Autocorrelation time is expected to increase significantly
- Uncertainty is still sizable

# Autocorrelation towards physical quark masses

Action density at  $t_0$  as defined by  $t^2 \langle E \rangle = 0.3$

**N203**

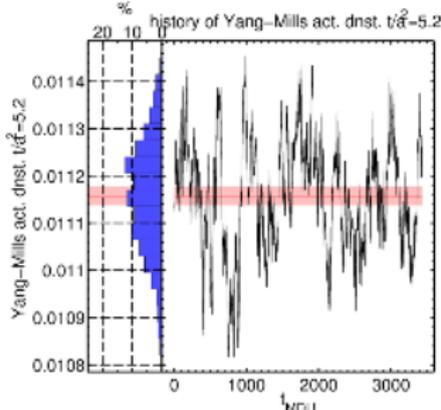
$m_\pi \approx 340$  MeV



$$\tau_{\text{int}} = 60(32) \text{ MDU}$$

**N200**

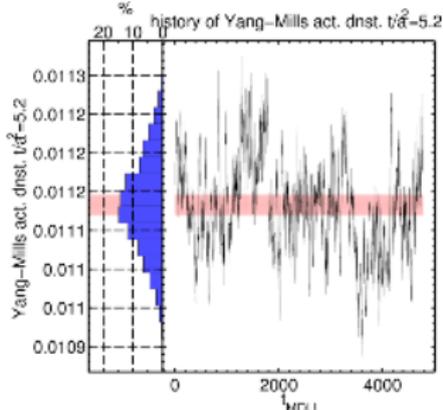
$m_\pi \approx 280$  MeV



$$\tau_{\text{int}} = 45(21) \text{ MDU}$$

**D200**

$m_\pi \approx 200$  MeV



$$\tau_{\text{int}} = 101(55) \text{ MDU}$$

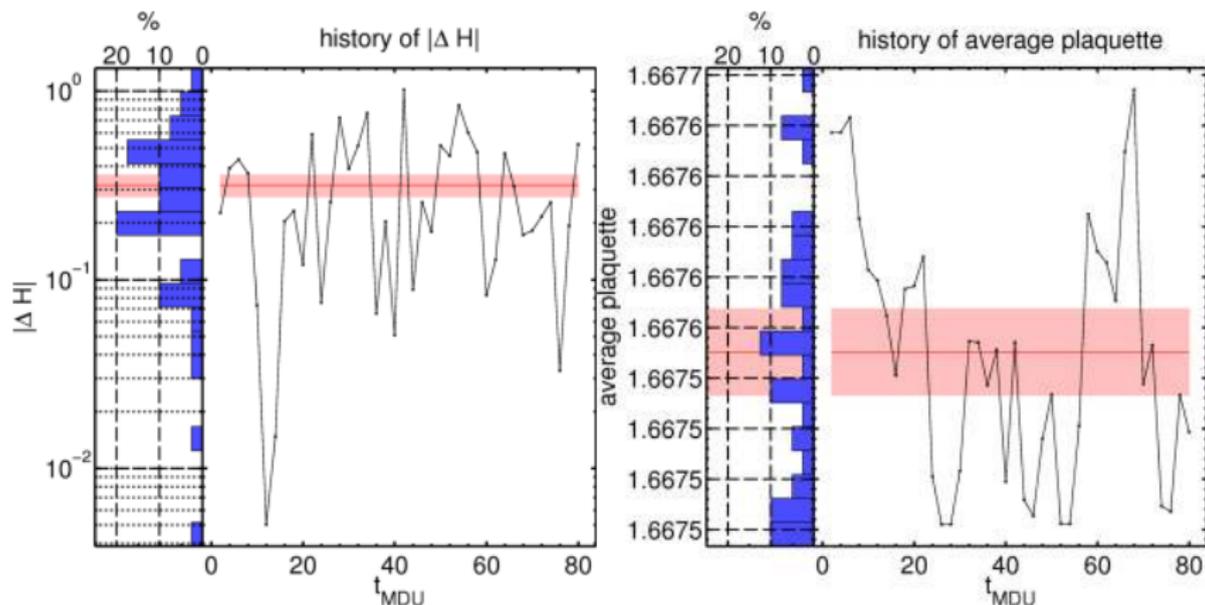
- Close to previously estimated  $\tau_{\text{exp}} = 14(3) \frac{t_0}{a^2}$

Bruno *et al.* JHEP 1502 043 (2015)

# “E250” –Description and thermalization strategy

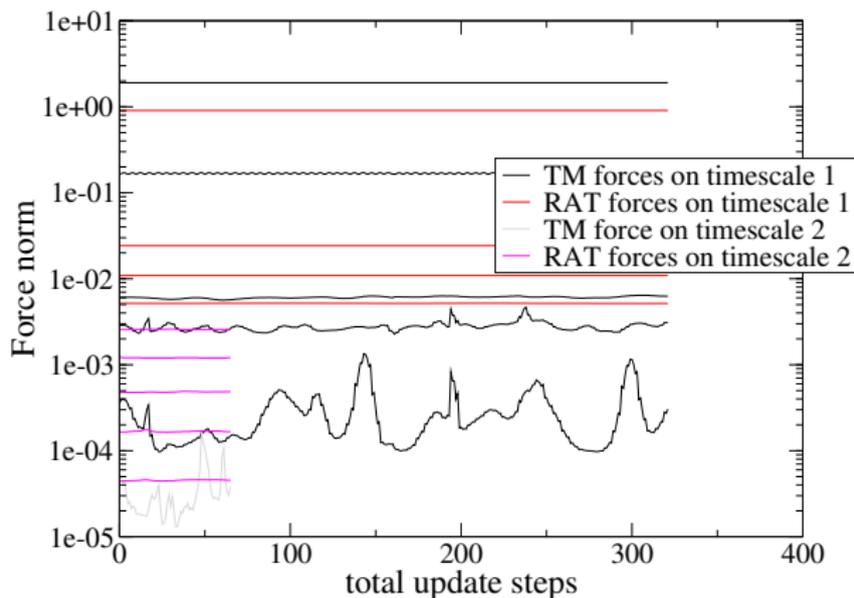
- At this lattice spacing periodic boundary conditions are chosen ( $\tau_{\text{exp}}$  not yet completely dominated by topology)
- Physical ud/s run at  $\beta = 3.55$  ( $a \approx 0.064$  fm)
- To keep  $m_{\pi}L \geq 4$ :  $L^3 \times T = 96^3 \times 192a^4$
- Thermalization strategy:
  - 1 Start from an  $SU(3)$  run with 3 light quarks and periodic boundary conditions
  - 2 Perform a number of runs to thermalize this small volume ( $L^3 \times T = 48^3 \times 64$ )
  - 3 Triple the time extent  $48^3 \times 64 \rightarrow 48^3 \times 192$
  - 4 Double the spatial extent  $48^3 \times 192 \rightarrow 96^3 \times 192$
- “Small volume” runs performed on JUQUEEN;  
large volume runs on MogonII (Mainz University)

# JUQUEEN → Cluster MOGON II (JGU Mainz)



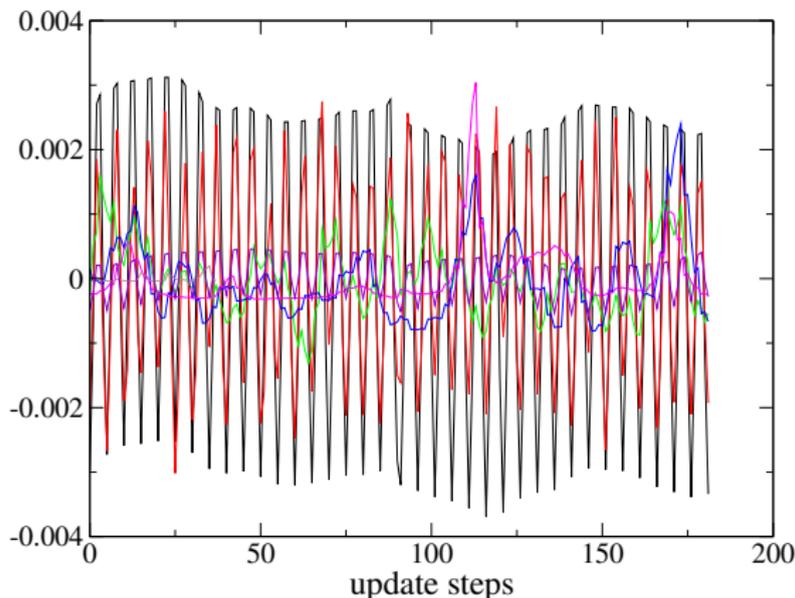
- First stable run – not yet fully thermalized
- Run uses local partition of size  $24 \times 8^3$  and 692 nodes/ 13824 cores
- Made possible by early usage time on Mogon II

## Some tuning: A look at the force norms



- Force terms for light quarks (black, grey) and strange (red, magenta)
- lvl 0 and lvl 1: 4th order Omelyan integrator;  
lvl 2: 2nd order Omelyan integrator
- lvl 2 forces are updated least often

## After some initial changes: A look at the norm fluctuations

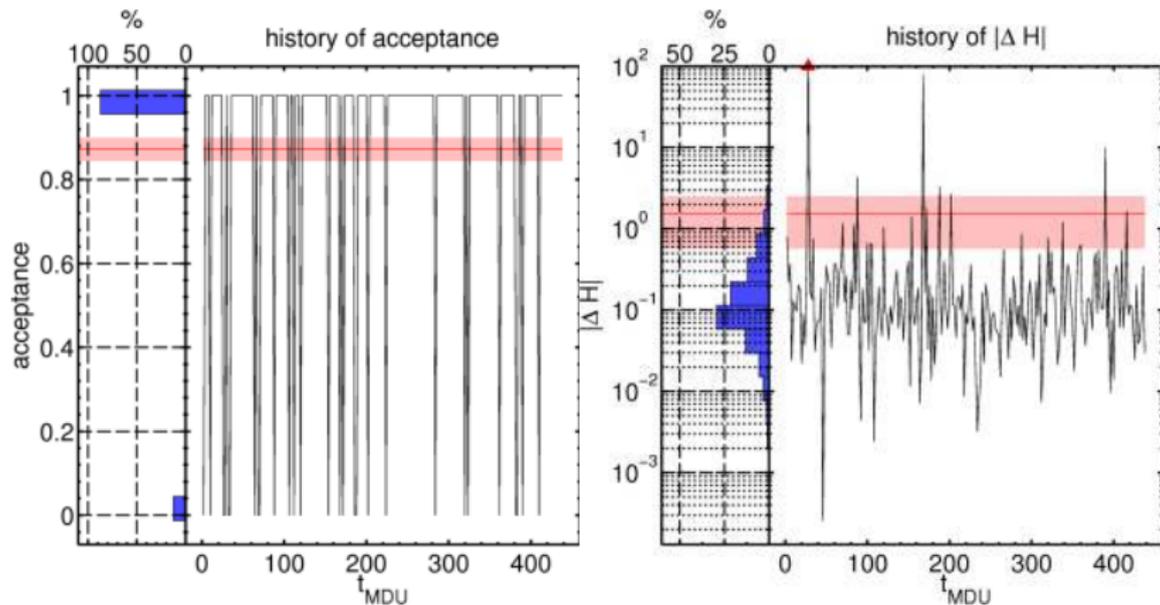


- after various tests  
(rearrangements of forces, further Hasenbusch masses, etc.)
- Observed dH seems largely driven by the force fluctuations

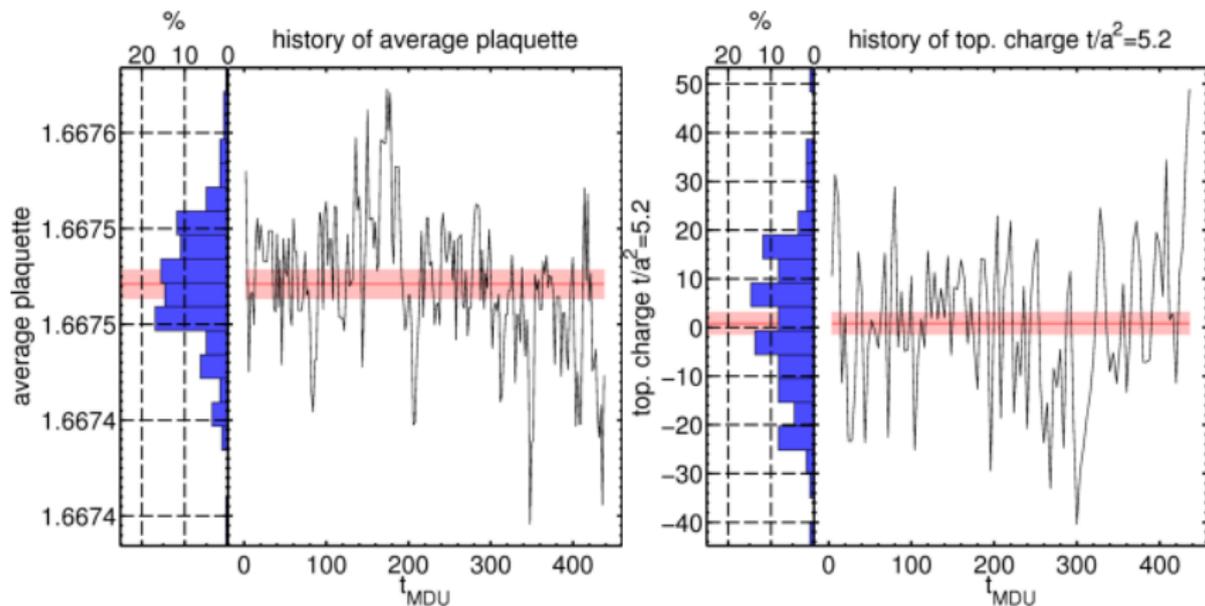
# Plots from the current run: dH

Acceptance: 0.872(27)

Shown: 436 MDU, 109 configurations

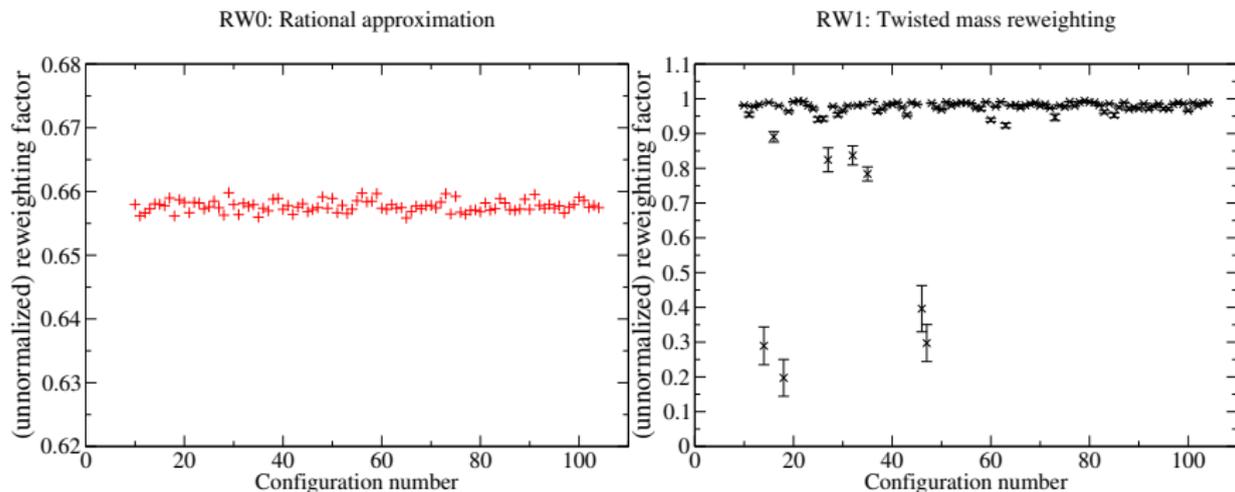


## Plots: average Plaquette & topological charge



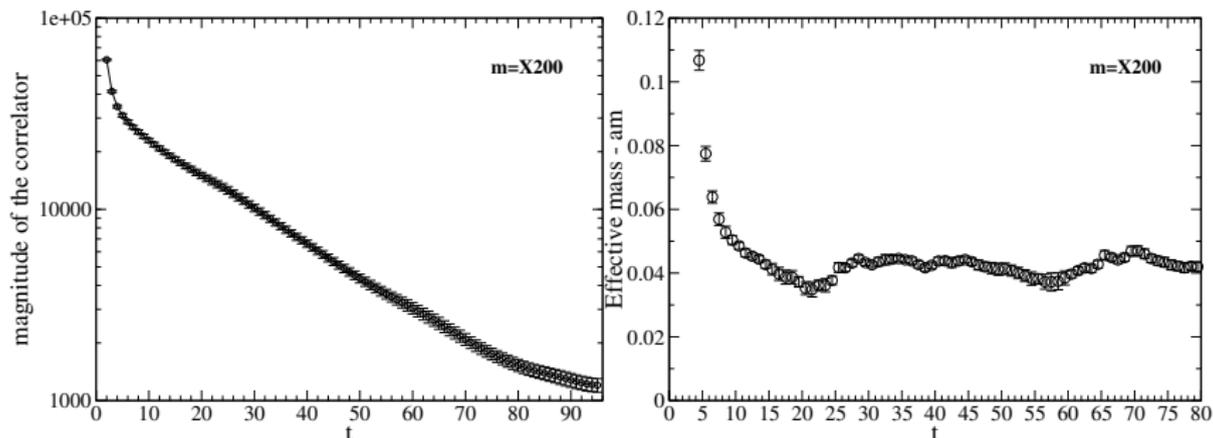
- Proper analysis will need a much longer chain
- Looks very promising

# A look at the reweighting factors



- Twisted mass reweighting estimated with 24 random sources and no intermediate twisted mass parameter  $\mu$
- Might have to improve estimate (see also pion)

# Pion correlator



- Results from 70 configs without averaging over (random) source locations
- Larger autocorrelation visible
- Currently results in  $m_\pi \approx 130(3)\text{MeV}$

# Challenges

- Runs with  $L^3 \times T = 48^3 \times 64$  proceeded smoothly
- Runs at intermediate volume needed various minor parameter adjustments (more frequent updates of the deflation subspace)
- Runs with  $L^3 \times T = 96^3 \times 192$ 
  - Large deflation blocksize was needed in order to maintain a manageable size of the little Dirac operator  
→ Iteration counts higher than desirable/ deflation not as efficient
  - Run only stable with large deflation blocksize  
 $6^4 \rightarrow 6 \times 4 \times 8^2 \rightarrow 8 \times 4 \times 8^2$
  - Indicates that a multigrid setup with 3 levels might be preferable for this lattice volume (but not obvious that it would pay off)
  - Even larger lattices would likely need further algorithmic improvements
- Fluctuation of twisted mass reweighting factor larger than desirable?

# Conclusions and Outlook

- Large library of CLS 2+1 flavor ensembles

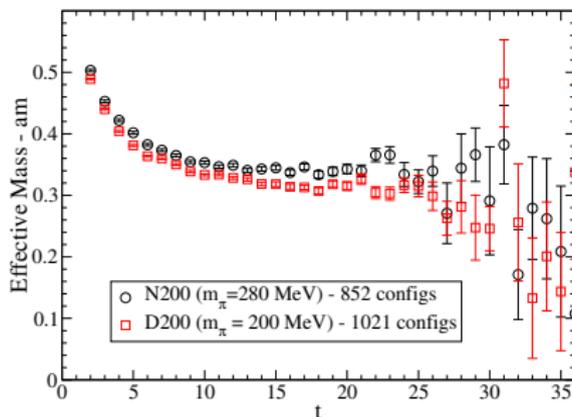
Bruno *et al.* JHEP 1502 043 (2015)

Bali *et al.* PRD 94 074501 (2016)

- Many physics studies started (and a number close to publication)
- Stable run at (very close to) physical  $m_l, m_s$  with  $a \approx 0.064$  fm
- Not enough statistics for a detailed study of autocorrelation, pion masses, nucleon masses, decay constants, . . .
- might profit from a 3 level multigrid setup at the current lattice volume
- Physical light-quark mass run will be crucial to reduce systematic uncertainties (examples focus on Mainz projects)
  - Hadronic vacuum polarization contribution to  $a_\mu$
  - Baryon structure calculations
  - Scale setting

Thank you!

# Nucleon effective masses

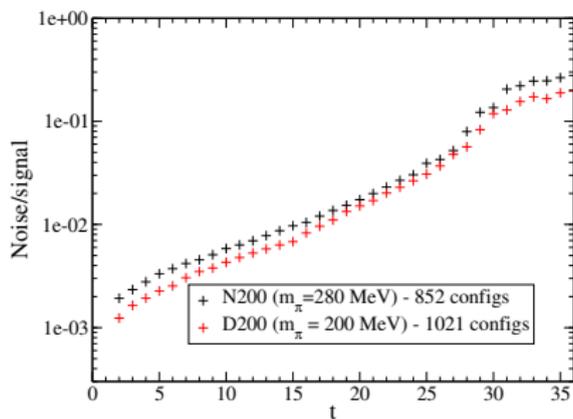


Data from Tim Harris, Konstantin Ottnad, Mainz

## Setup

- All-mode-averaging (AMA)  
12 ( $n_c \times n_D$ ) exact inversions and  $16 \times 12$  sloppy inversions
- Results from sources in a single timeslice
- Effective mass from the local-smearred correlator

# Nucleon noise/signal



Data from Tim Harris, Konstantin Ottnad, Mainz

- Slope in (most of) plateau region does not reach asymptotic value (given by  $m_N - \frac{3}{2}m_\pi$ )
- Suggests that in practice noise/signal scaling is not as severe
- Exponential growth qualitatively observed