

Spectroscopy of the BSM sextet model

Outline

Challenges

Mixed Action

Preliminary results

Conclusion

Chik Him (Ricky) Wong

Lattice Higgs Collaboration (L_{at}HC):

Zoltán Fodor[§], *Kieran Holland*^{*},

Julius Kuti[†], *Dániel Nógrádi*⁻, *Chik Him Wong*[§]

† University of California, San Diego * University of the Pacific § University of Wuppertal - Eötvös University

LATTICE 2017

Outline

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

Outline

Challenges

Mixed Action

Preliminary results

Conclusion

- Challenges of lattice analysis of nearly conformal BSM model
- Mixed action analysis with application of gradient flow
- Preliminary results
- Conclusion

Challenges

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

Outline

Challenges

Mixed Action

Preliminary results

Conclusion

- Case study of nearly conformal model: Sextet model $SU(3)$ with $N_f = 2$ in two-index symmetric representation
- Focus of this talk: Hadron Spectroscopy study
- No IRFP is found despite small β function [more in Kieran Holland's talk]
⇒ still chirally broken
- Is χ PT applicable? Dynamics are very different from QCD
- A low-lying 0^{++} scalar exists
⇒ Linear- σ model or Dilaton-inspired extended theory? (Julius Kuti's talk)
- Expensive to get lower in m where 0^{++} scalar may decouple

Challenges

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

Outline

Challenges

Mixed Action

Preliminary results

Conclusion

- Case study of nearly conformal model: Sextet model $SU(3)$ with $N_f = 2$ in two-index symmetric representation
- Focus of this talk: Hadron Spectroscopy study
- No IRFP is found despite small β function [more in Kieran Holland's talk]
⇒ still chirally broken
- Is χ PT applicable? Dynamics are very different from QCD
- A low-lying 0^{++} scalar exists
⇒ Linear- σ model or Dilaton-inspired extended theory? (Julius Kuti's talk)
- Expensive to get lower in m where 0^{++} scalar may decouple

Challenges

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

Outline

Challenges

Mixed Action

Preliminary results

Conclusion

- Case study of nearly conformal model: Sextet model $SU(3)$ with $N_f = 2$ in two-index symmetric representation
- Focus of this talk: Hadron Spectroscopy study
- No IRFP is found despite small β function [more in Kieran Holland's talk]
⇒ still chirally broken
- Is χ PT applicable? Dynamics are very different from QCD
- A low-lying 0^{++} scalar exists
⇒ Linear- σ model or Dilaton-inspired extended theory? (Julius Kuti's talk)
- Expensive to get lower in m where 0^{++} scalar may decouple

Challenges

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

Outline

Challenges

Mixed Action

Preliminary results

Conclusion

- Case study of nearly conformal model: Sextet model $SU(3)$ with $N_f = 2$ in two-index symmetric representation
- Focus of this talk: Hadron Spectroscopy study
- No IRFP is found despite small β function [more in Kieran Holland's talk]
⇒ still chirally broken
- Is χ PT applicable? Dynamics are very different from QCD
- A low-lying 0^{++} scalar exists
⇒ Linear- σ model or Dilaton-inspired extended theory? (Julius Kuti's talk)
- Expensive to get lower in m where 0^{++} scalar may decouple

Challenges

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

Outline

Challenges

Mixed Action

Preliminary results

Conclusion

- Case study of nearly conformal model: Sextet model $SU(3)$ with $N_f = 2$ in two-index symmetric representation
- Focus of this talk: Hadron Spectroscopy study
- No IRFP is found despite small β function [more in Kieran Holland's talk]
⇒ still chirally broken
- Is χ PT applicable? Dynamics are very different from QCD
- A low-lying 0^{++} scalar exists
⇒ Linear- σ model or Dilaton-inspired extended theory? (Julius Kuti's talk)
- Expensive to get lower in m where 0^{++} scalar may decouple

Challenges

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

Outline

Challenges

Mixed Action

Preliminary results

Conclusion

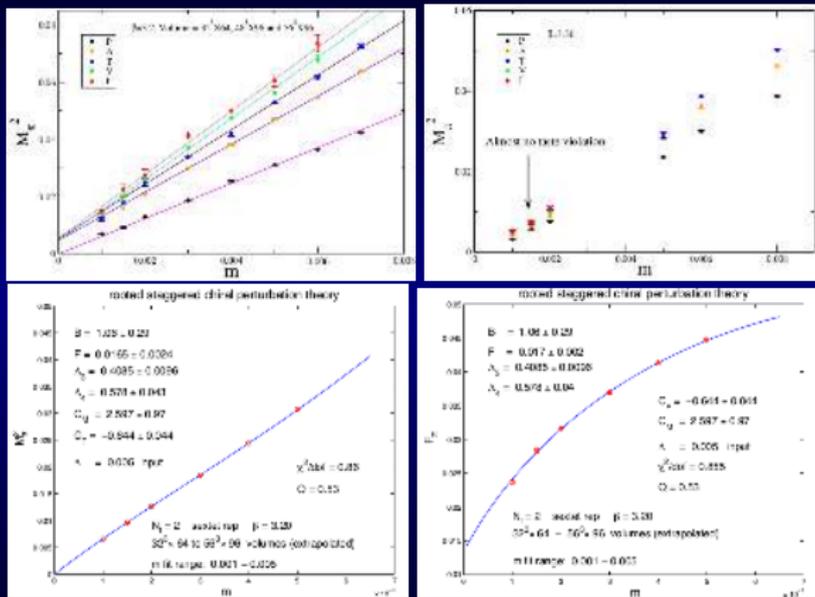
- Case study of nearly conformal model: Sextet model $SU(3)$ with $N_f = 2$ in two-index symmetric representation
- Focus of this talk: Hadron Spectroscopy study
- No IRFP is found despite small β function [more in Kieran Holland's talk]
 \Rightarrow still chirally broken
- Is χ PT applicable? Dynamics are very different from QCD
- A low-lying 0^{++} scalar exists
 \Rightarrow Linear- σ model or Dilaton-inspired extended theory? (Julius Kuti's talk)
- Expensive to get lower in m where 0^{++} scalar may decouple

Challenges

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

- Staggered formalism:
Taste breaking structure is different from QCD



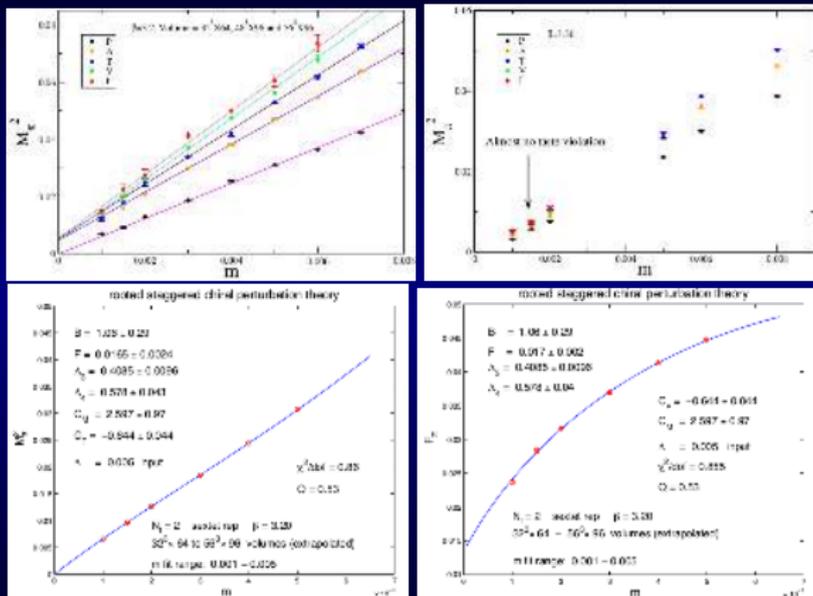
- Analysis on full dataset with Rooted staggered χ PT becomes difficult
- Goal: Ease the analysis by isolating taste breaking effects
 \Rightarrow Mixed action analysis

Challenges

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

- Staggered formalism:
Taste breaking structure is different from QCD



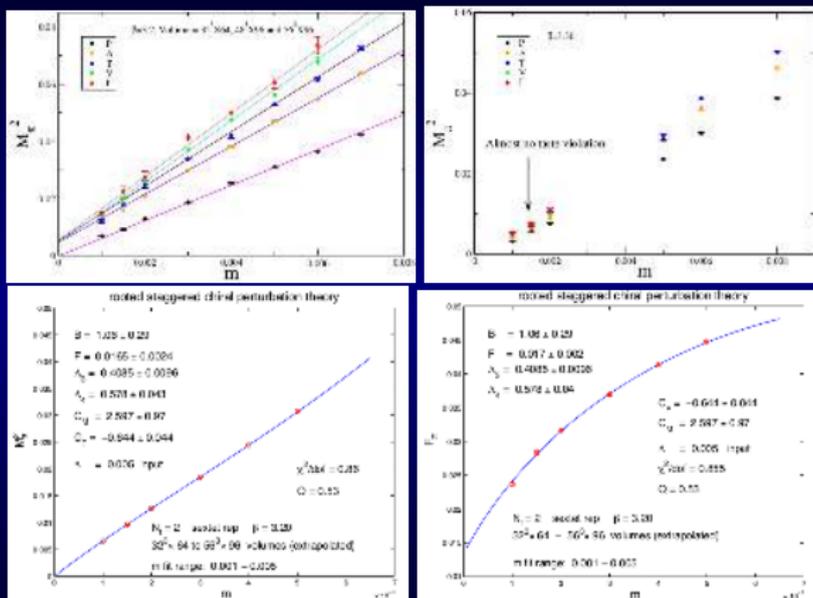
- Analysis on full dataset with Rooted staggered χ PT becomes difficult
- Goal: Ease the analysis by isolating taste breaking effects
 \Rightarrow Mixed action analysis

Challenges

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

- Staggered formalism:
Taste breaking structure is different from QCD



- Analysis on full dataset with Rooted staggered χ PT becomes difficult
- Goal: Ease the analysis by isolating taste breaking effects
 \Rightarrow Mixed action analysis

Mixed action analysis

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

Outline

Challenges

Mixed Action

Preliminary results

Conclusion

- **Mixed action setup: Valence fermion action is different from sea fermion action**
- χ PT \Rightarrow MA χ PT
- If the valence fermion action (almost) respects taste symmetry,
 - The valence Goldstone spectrum $M_{\pi, V}$ has no detectable taste splitting
 - Taste breaking effect from the sea fermion action is messaged in the mixed meson $M_{\pi, SV}$
- Flowed action as the valence action :
 - Apply a large number of small stout smearing steps to the original links, equivalent to a Wilson flow of $t_0 a^2$
 - Staggered action defined by the “flowed” links with a valence quark mass m_V

Mixed action analysis

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

Outline

Challenges

Mixed Action

Preliminary results

Conclusion

- Mixed action setup: Valence fermion action is different from sea fermion action
- χ PT \Rightarrow MA χ PT
- If the valence fermion action (almost) respects taste symmetry,
 - The valence Goldstone spectrum $M_{\pi, V}$ has no detectable taste splitting
 - Taste breaking effect from the sea fermion action is messaged in the mixed meson $M_{\pi, S}$
- Flowed action as the valence action :
 - Apply a large number of small stout smearing steps to the original links, equivalent to a Wilson flow of $t_0 a^2$
 - Staggered action defined by the “flowed” links with a valence quark mass m_V

Mixed action analysis

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

Outline

Challenges

Mixed Action

Preliminary results

Conclusion

- Mixed action setup: Valence fermion action is different from sea fermion action
- χ PT \Rightarrow MA χ PT
- If the valence fermion action (almost) respects taste symmetry,
 - The valence Goldstone spectrum $M_{\pi,VV}$ has no detectable taste splitting
 - Taste breaking effect from the sea fermion action is messaged in the mixed meson $M_{\pi,VS}$
- Flowed action as the valence action :
 - Apply a large number of small stout smearing steps to the original links, equivalent to a Wilson flow of $t_0 a^2$
 - Staggered action defined by the “flowed” links with a valence quark mass m_V

Mixed action analysis

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

Outline

Challenges

Mixed Action

Preliminary results

Conclusion

- Mixed action setup: Valence fermion action is different from sea fermion action
- χ PT \Rightarrow MA χ PT
- If the valence fermion action (almost) respects taste symmetry,
 - The valence Goldstone spectrum $M_{\pi, vV}$ has no detectable taste splitting
 - Taste breaking effect from the sea fermion action is messaged in the mixed meson $M_{\pi, vS}$
- Flowed action as the valence action :
 - Apply a large number of small stout smearing steps to the original links, equivalent to a Wilson flow of $t_0 a^2$
 - Staggered action defined by the “flowed” links with a valence quark mass m_V

Mixed action analysis

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

Outline

Challenges

Mixed Action

Preliminary results

Conclusion

- Mixed action setup: Valence fermion action is different from sea fermion action
- χ PT \Rightarrow MA χ PT
- If the valence fermion action (almost) respects taste symmetry,
 - The valence Goldstone spectrum $M_{\pi, vV}$ has no detectable taste splitting
 - Taste breaking effect from the sea fermion action is messaged in the mixed meson $M_{\pi, vS}$
- Flowed action as the valence action :
 - Apply a large number of small stout smearing steps to the original links, equivalent to a Wilson flow of $t_0 a^2$
 - Staggered action defined by the “flowed” links with a valence quark mass m_V

Mixed action analysis

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

Outline

Challenges

Mixed Action

Preliminary results

Conclusion

- Mixed action setup: Valence fermion action is different from sea fermion action
- χ PT \Rightarrow MA χ PT
- If the valence fermion action (almost) respects taste symmetry,
 - The valence Goldstone spectrum $M_{\pi, vV}$ has no detectable taste splitting
 - Taste breaking effect from the sea fermion action is messaged in the mixed meson $M_{\pi, vS}$
- Flowed action as the valence action :
 - Apply a large number of small stout smearing steps to the original links, equivalent to a Wilson flow of $t_f a^2$
 - Staggered action defined by the “flowed” links with a valence quark mass m_v

Mixed action analysis

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

Outline

Challenges

Mixed Action

Preliminary results

Conclusion

- Mixed action setup: Valence fermion action is different from sea fermion action
- χ PT \Rightarrow MA χ PT
- If the valence fermion action (almost) respects taste symmetry,
 - The valence Goldstone spectrum $M_{\pi, vV}$ has no detectable taste splitting
 - Taste breaking effect from the sea fermion action is messaged in the mixed meson $M_{\pi, vS}$
- Flowed action as the valence action :
 - Apply a large number of small stout smearing steps to the original links, equivalent to a Wilson flow of $t_f a^2$
 - Staggered action defined by the “flowed” links with a valence quark mass m_v

Mixed action analysis

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

Outline

Challenges

Mixed Action

Preliminary results

Conclusion

- Mixed action setup: Valence fermion action is different from sea fermion action
- χ PT \Rightarrow MA χ PT
- If the valence fermion action (almost) respects taste symmetry,
 - The valence Goldstone spectrum $M_{\pi, vV}$ has no detectable taste splitting
 - Taste breaking effect from the sea fermion action is messaged in the mixed meson $M_{\pi, vS}$
- Flowed action as the valence action :
 - Apply a large number of small stout smearing steps to the original links, equivalent to a Wilson flow of $t_f a^2$
 - Staggered action defined by the “flowed” links with a valence quark mass m_v

Mixed action analysis

Spectroscopy of the BSM sextet model

Chik Him (Ricky) Wong

Outline

Challenges

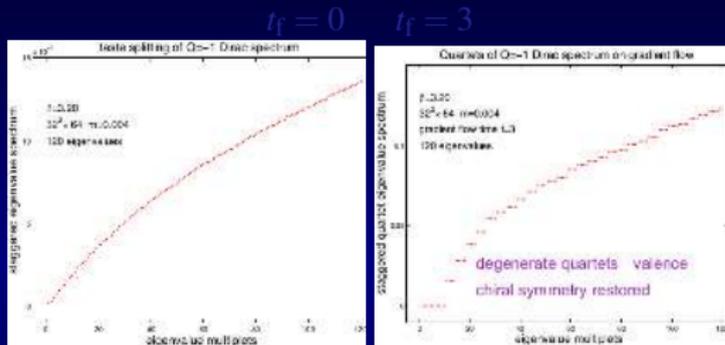
Mixed Action

Preliminary results

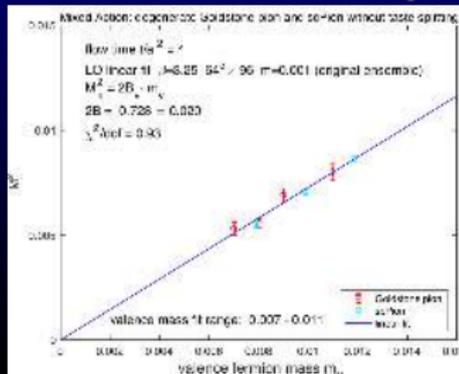
Conclusion

• Flowed action as the valence action :

- Wilson flow reduces cutoff effects, approximately restores the taste symmetry



- Valence Goldstone and valence non-Goldstone pions degenerate



Mixed action analysis

Spectroscopy of the BSM sextet model

Chik Him (Ricky) Wong

Outline

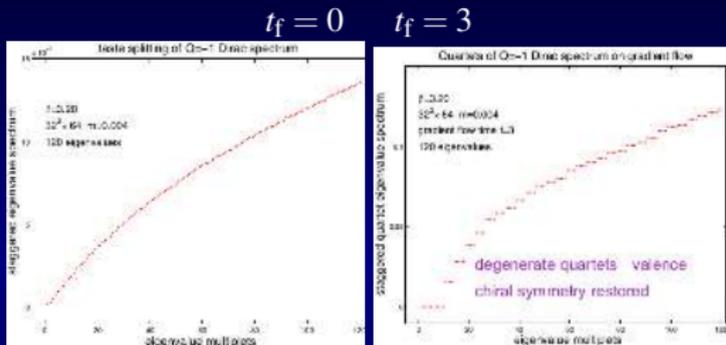
Challenges

Mixed Action

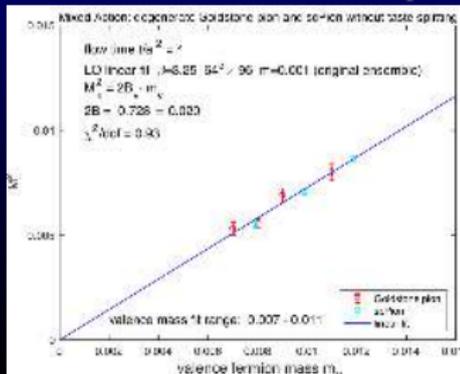
Preliminary results

Conclusion

- Flowed action as the valence action :
 - Wilson flow reduces cutoff effects, approximately restores the taste symmetry



- Valence Goldstone and valence non-Goldstone pions degenerate



Mixed action analysis

Spectroscopy of the BSM sextet model

Chik Him (Ricky) Wong

Outline

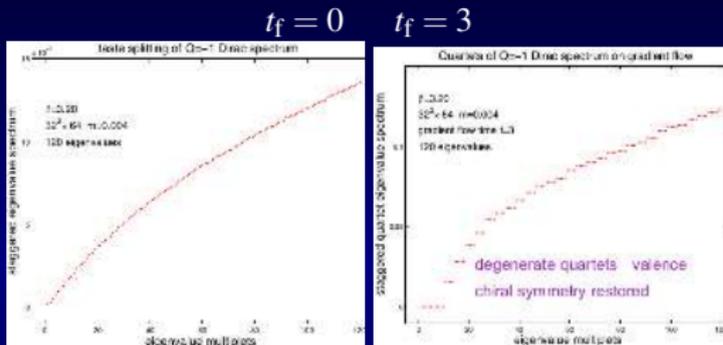
Challenges

Mixed Action

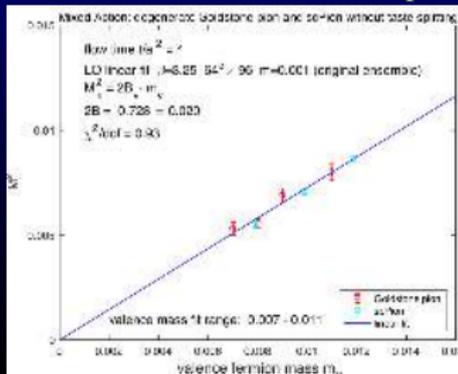
Preliminary results

Conclusion

- Flowed action as the valence action :
 - Wilson flow reduces cutoff effects, approximately restores the taste symmetry



- Valence Goldstone and valence non-Goldstone pions degenerate



Mixed action analysis

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

Outline

Challenges

Mixed Action

Preliminary results

Conclusion

- **Additional advantage:**
 - Wilson flow smoothens the links \Rightarrow Faster inversions
 - Hadron correlators, especially 0^{++} scalar, becomes more affordable
 - Going lower in m_V is easier

Mixed action analysis

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

Outline

Challenges

Mixed Action

Preliminary results

Conclusion

- **Additional advantage:**
 - Wilson flow smoothens the links \Rightarrow Faster inversions
 - Hadron correlators, especially 0^{++} scalar, becomes more affordable
 - Going lower in m_V is easier

Mixed action analysis

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

Outline

Challenges

Mixed Action

Preliminary results

Conclusion

- Additional advantage:
 - Wilson flow smoothens the links \Rightarrow Faster inversions
 - Hadron correlators, especially 0^{++} scalar, becomes more affordable
 - Going lower in m_V is easier

Mixed action analysis

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

Outline

Challenges

Mixed Action

Preliminary results

Conclusion

- Additional advantage:
 - Wilson flow smoothens the links \Rightarrow Faster inversions
 - Hadron correlators, especially 0^{++} scalar, becomes more affordable
 - Going lower in m_V is easier

Preliminary results

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

Outline

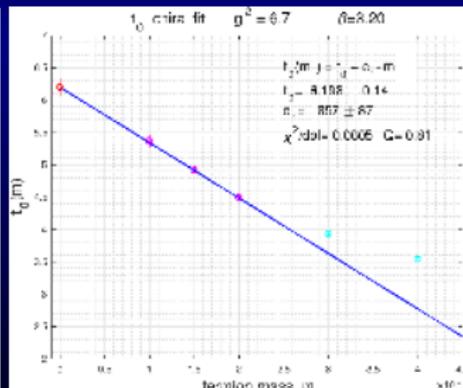
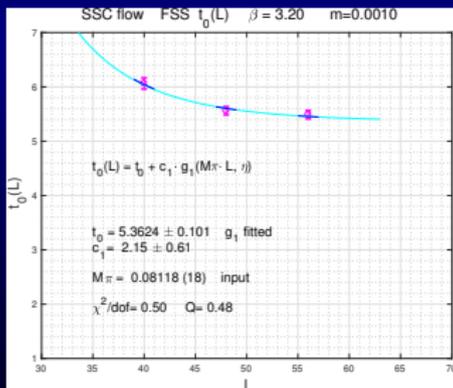
Challenges

Mixed Action

Preliminary results

Conclusion

- Measure quantities X , e.g. F_π , M_X on gradient flowed links. $\sqrt{8t_f} M_\pi \ll 1$ is required, and p -regime is assumed.
- Define a scale $t_0 : g^2|_{t_0} = c$ (6.7 here)
- Determine the chiral limit of the infinite volume extrapolated t_0 at each β [Kieran Holland's talk]



Preliminary results

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

Outline

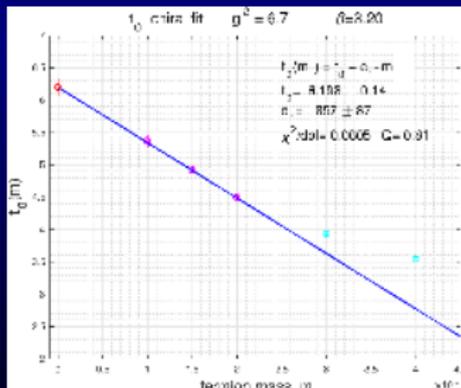
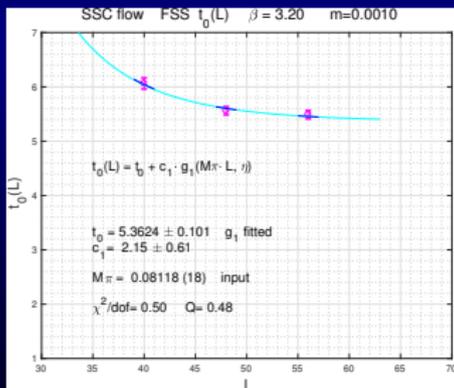
Challenges

Mixed Action

Preliminary results

Conclusion

- Measure quantities X , e.g. F_π , M_X on gradient flowed links. $\sqrt{8t_f} M_\pi \ll 1$ is required, and p -regime is assumed.
- Define a scale $t_0 : g^2|_{t_0} = c$ (6.7 here)
- Determine the chiral limit of the infinite volume extrapolated t_0 at each β [Kieran Holland's talk]



Preliminary results

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

Outline

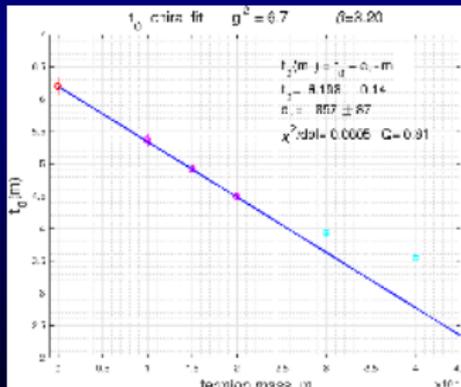
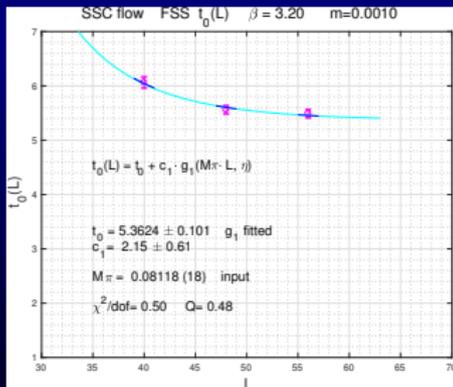
Challenges

Mixed Action

Preliminary results

Conclusion

- Measure quantities X , e.g. F_π , M_X on gradient flowed links.
 $\sqrt{8t_f} M_\pi \ll 1$ is required, and p -regime is assumed.
- Define a scale t_0 : $g^2|_{t_0} = c$ (6.7 here)
- Determine the chiral limit of the infinite volume extrapolated t_0 at each β [Kieran Holland's talk]



Preliminary results

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

Outline

Challenges

Mixed Action

Preliminary results

Conclusion

- Assuming MA χ PT, the relation between X_{NLO} and X_{LO} in the infinite-volume limit can be worked out. E.g.

$$\frac{M_{\pi,vv,\text{NLO}}^2}{M_{\pi,vv,\text{LO}}^2} = \left(1 + \frac{1}{32\pi^2 F_\pi^2} \left[(M_{\pi,vv,\text{LO}}^2 - M_{\pi,ss,\text{LO}}^2) \right. \right. \\ \left. \left. + (2M_{\pi,vv,\text{LO}}^2 - M_{\pi,ss,\text{LO}}^2) \ln \frac{M_{\pi,vv,\text{LO}}^2}{\mu^2} \right] \right. \\ \left. - \frac{8}{F_\pi} \left[(L_5 - 2L_8)M_{\pi,vv,\text{LO}}^2 + 2(L_4 - 2L_6)M_{\pi,ss,\text{LO}}^2 \right] + C a^2 \right), \\ \frac{F_{\pi,vv,\text{NLO}}^2}{F_\pi} = \left(1 - \frac{M_{\pi,vs,\text{LO}}^2}{16\pi^2 F_\pi^2} \ln \frac{M_{\pi,vs,\text{LO}}^2}{\mu^2} + \frac{4}{F_\pi^2} \left[L_5 M_{\pi,vv,\text{LO}}^2 + 2L_4 M_{\pi,ss,\text{LO}}^2 \right] \right. \\ \left. + D a^2 \right),$$

where $M_{\pi,vv,\text{LO}}^2 = 2Bm_v$, $M_{\pi,ss,\text{LO}}^2 = 2Bm_s$, $M_{\pi,vs,\text{LO}}^2 = B(m_v + m_s)$

- Scaling with t_0 to obtain dimensionless quantities $\bar{y} \equiv \sqrt{t_0} y$, these relations can be parameterized as

$$\bar{M}_{\pi, \nu \nu, \text{NLO}}^2 = \bar{m}_\nu \left(2\bar{B} + b_1 \bar{m}_\nu + b_2 \bar{m}_s + b_3 (2\bar{m}_\nu - \bar{m}_s) \ln \bar{m}_\nu + b_4 t_0^{-1} a^2 \right)$$

$$\bar{F}_{\pi, \nu \nu, \text{NLO}} = \bar{F}_\pi + c_1 \bar{m}_\nu + c_2 \bar{m}_s + c_3 (\bar{m}_\nu + \bar{m}_s) \ln \bar{m}_\nu + c_4 t_0^{-1} a^2$$

- In Mixed action, chiral limit and continuum limit cannot be separated
 - \Rightarrow Simultaneous fit of all available $L^3 \times T$'s, β 's (with corresponding t_0 's), m_s and m_ν 's to obtain \bar{X} 's in the infinite-volume, chiral and continuum limit
- \bar{F}_π is the t_f -independent, infinite-volume, continuum and chiral limit of $\sqrt{t_0} F_\pi$, which sets the scale of M_X via $\bar{M}_X / \bar{F}_\pi = M_X / F_\pi$

- Scaling with t_0 to obtain dimensionless quantities $\bar{y} \equiv \sqrt{t_0} y$, these relations can be parameterized as

$$\bar{M}_{\pi, \nu\nu, \text{NLO}}^2 = \bar{m}_\nu \left(2\bar{B} + b_1 \bar{m}_\nu + b_2 \bar{m}_s + b_3 (2\bar{m}_\nu - \bar{m}_s) \ln \bar{m}_\nu + b_4 t_0^{-1} a^2 \right)$$

$$\bar{F}_{\pi, \nu\nu, \text{NLO}} = \bar{F}_\pi + c_1 \bar{m}_\nu + c_2 \bar{m}_s + c_3 (\bar{m}_\nu + \bar{m}_s) \ln \bar{m}_\nu + c_4 t_0^{-1} a^2$$

- In Mixed action, chiral limit and continuum limit cannot be separated
 \Rightarrow Simultaneous fit of all available $L^3 \times T$'s, β 's (with corresponding t_0 's), m_s and m_ν 's to obtain \bar{X} 's in the infinite-volume, chiral and continuum limit
- \bar{F}_π is the t_f -independent, infinite-volume, continuum and chiral limit of $\sqrt{t_0} F_\pi$, which sets the scale of M_X via $\bar{M}_X / \bar{F}_\pi = M_X / F_\pi$

- Scaling with t_0 to obtain dimensionless quantities $\bar{y} \equiv \sqrt{t_0} y$, these relations can be parameterized as

$$\bar{M}_{\pi, \nu\nu, \text{NLO}}^2 = \bar{m}_\nu \left(2\bar{B} + b_1 \bar{m}_\nu + b_2 \bar{m}_s + b_3 (2\bar{m}_\nu - \bar{m}_s) \ln \bar{m}_\nu + b_4 t_0^{-1} a^2 \right)$$

$$\bar{F}_{\pi, \nu\nu, \text{NLO}} = \bar{F}_\pi + c_1 \bar{m}_\nu + c_2 \bar{m}_s + c_3 (\bar{m}_\nu + \bar{m}_s) \ln \bar{m}_\nu + c_4 t_0^{-1} a^2$$

- In Mixed action, chiral limit and continuum limit cannot be separated
 \Rightarrow Simultaneous fit of all available $L^3 \times T$'s, β 's (with corresponding t_0 's), m_s and m_ν 's to obtain \bar{X} 's in the infinite-volume, chiral and continuum limit
- \bar{F}_π is the t_f -independent, infinite-volume, continuum and chiral limit of $\sqrt{t_0} F_\pi$, which sets the scale of M_X via $\bar{M}_X / \bar{F}_\pi = M_X / F_\pi$

Preliminary results

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

Outline

Challenges

Mixed Action

Preliminary results

Conclusion

- **Sea Action:**
Tree-level Symanzik-Improved gauge action with 2-step $\rho = 0.15$ stout-smearred Staggered $N_f = 2$ SU(3) Sextet fermion, sea mass m_s
- **Valence Action:**
Staggered fermion action with $t_f = 4$ (80 steps of $\rho = 0.05$ stout smeared) gauge, valence mass m_v
- **Available data:**

β	m_s	m_v	$L^3 \times T$
3.20	0.001	0.006,0.008,0.010	$40^3 \times 80, 48^3 \times 96, 56^3 \times 96$
	0.0015	0.006,0.008,0.010	$56^3 \times 96$
	0.002	0.006,0.008,0.010	$56^3 \times 96$
3.25	0.001	0.006,0.008,0.010	$48^3 \times 96, 56^3 \times 96, 64^3 \times 96$
3.30	0.001	0.006,0.008,0.010	$48^3 \times 96, 56^3 \times 96, 64^3 \times 96$

Preliminary results

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

Outline

Challenges

Mixed Action

Preliminary results

Conclusion

- **Sea Action:**
Tree-level Symanzik-Improved gauge action with 2-step $\rho = 0.15$ stout-smearred Staggered $N_f = 2$ SU(3) Sextet fermion, sea mass m_s
- **Valence Action:**
Staggered fermion action with $t_f = 4$ (80 steps of $\rho = 0.05$ stout smeared) gauge, valence mass m_v
- **Available data:**

β	m_s	m_v	$L^3 \times T$
3.20	0.001	0.006,0.008,0.010	$40^3 \times 80, 48^3 \times 96, 56^3 \times 96$
	0.0015	0.006,0.008,0.010	$56^3 \times 96$
	0.002	0.006,0.008,0.010	$56^3 \times 96$
3.25	0.001	0.006,0.008,0.010	$48^3 \times 96, 56^3 \times 96, 64^3 \times 96$
3.30	0.001	0.006,0.008,0.010	$48^3 \times 96, 56^3 \times 96, 64^3 \times 96$

Preliminary results

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

Outline

Challenges

Mixed Action

Preliminary results

Conclusion

- **Sea Action:**
Tree-level Symanzik-Improved gauge action with 2-step $\rho = 0.15$ stout-smearred Staggered $N_f = 2$ SU(3) Sextet fermion, sea mass m_s
- **Valence Action:**
Staggered fermion action with $t_f = 4$ (80 steps of $\rho = 0.05$ stout smeared) gauge, valence mass m_v
- **Available data:**

β	m_s	m_v	$L^3 \times T$
3.20	0.001	0.006,0.008,0.010	$40^3 \times 80, 48^3 \times 96, 56^3 \times 96$
	0.0015	0.006,0.008,0.010	$56^3 \times 96$
	0.002	0.006,0.008,0.010	$56^3 \times 96$
3.25	0.001	0.006,0.008,0.010	$48^3 \times 96, 56^3 \times 96, 64^3 \times 96$
3.30	0.001	0.006,0.008,0.010	$48^3 \times 96, 56^3 \times 96, 64^3 \times 96$

Preliminary results

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

Outline

Challenges

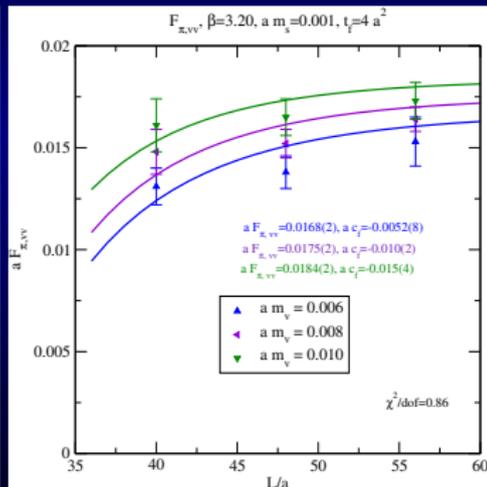
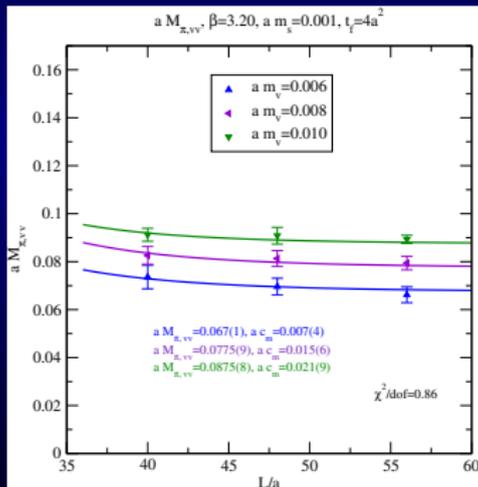
Mixed Action

Preliminary results

Conclusion

- Preliminary results of global fit: Finite Size Scaling part

$$M_{\pi, \nu\nu}(L) = M_{\pi, \nu\nu} + c_m g_1(M_{\pi, \nu\nu} L), \quad F_{\pi, \nu\nu}(L) = F_{\pi, \nu\nu} + c_f g_1(M_{\pi, \nu\nu} L)$$



Preliminary results

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

Outline

Challenges

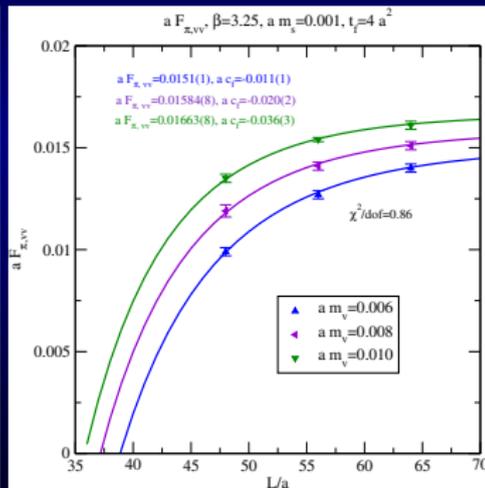
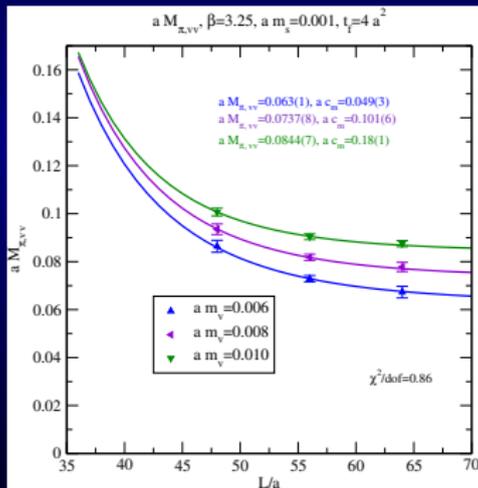
Mixed Action

Preliminary results

Conclusion

- Preliminary results of global fit: Finite Size Scaling part

$$M_{\pi, \nu\nu}(L) = M_{\pi, \nu\nu} + c_m g_1(M_{\pi, \nu\nu} L), \quad F_{\pi, \nu\nu}(L) = F_{\pi, \nu\nu} + c_f g_1(M_{\pi, \nu\nu} L)$$



Preliminary results

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

Outline

Challenges

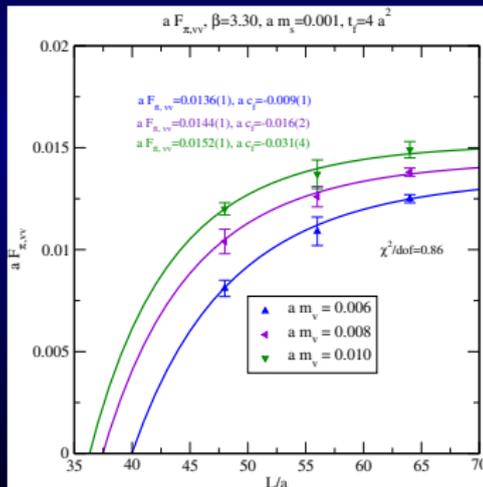
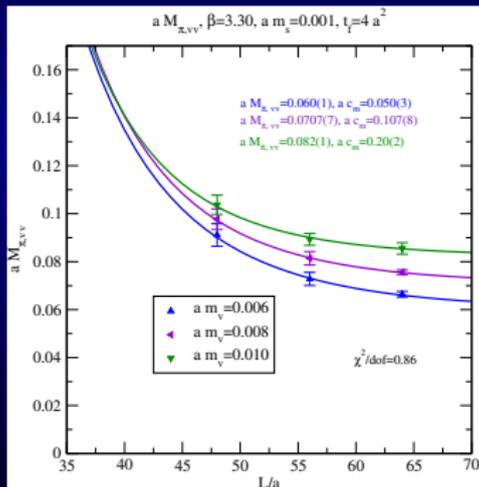
Mixed Action

Preliminary results

Conclusion

- Preliminary results of global fit: Finite Size Scaling part

$$M_{\pi, \nu \nu}(L) = M_{\pi, \nu \nu} + c_m g_1(M_{\pi, \nu \nu} L), \quad F_{\pi, \nu \nu}(L) = F_{\pi, \nu \nu} + c_f g_1(M_{\pi, \nu \nu} L)$$



Preliminary results

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

Outline

Challenges

Mixed Action

Preliminary results

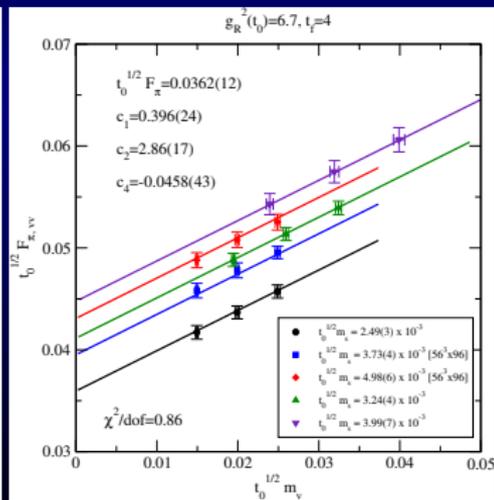
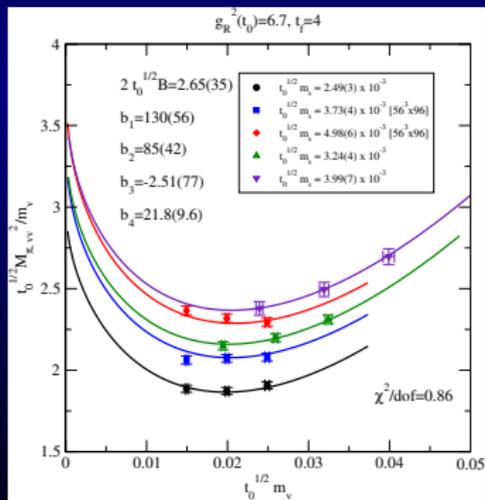
Conclusion

- Preliminary results of global fit:

$$\bar{M}_{\pi, vv, \text{NLO}}^2 = \bar{m}_v (2\bar{B} + b_1 \bar{m}_v + b_2 \bar{m}_s + b_3 (2\bar{m}_v - \bar{m}_s) \ln \bar{m}_v + b_4 t_0^{-1} a^2)$$

$$\bar{F}_{\pi, vv, \text{NLO}} = \bar{F}_{\pi} + c_1 \bar{m}_v + c_2 \bar{m}_s + c_3 (\bar{m}_v + \bar{m}_s) \ln \bar{m}_v + c_4 t_0^{-1} a^2$$

(c_3 is not detectable, hence omitted in the fit)



Conclusion

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

Outline

Challenges

Mixed Action

Preliminary results

Conclusion

- **Hadron Spectroscopy on nearly conformal models is challenging**
 - Low-lying 0^{++} scalar interacts with pion dynamics \Rightarrow χ PT needs modification
 - Taste breaking structure for Staggered simulations is different from QCD
- **Mixed action analysis is explored**
 - Wilson-flowed links used as the valence action
 - Flowed action restores taste symmetry and allows cheaper inversions
 - Preliminary results is promising, demonstrating the viability of the approach
- **More comprehensive analysis is needed. E.g. Errors of t_0 , Non-unitarity effects, the effects of low-lying 0^{++} scalar**

Conclusion

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

Outline

Challenges

Mixed Action

Preliminary results

Conclusion

- Hadron Spectroscopy on nearly conformal models is challenging
 - Low-lying 0^{++} scalar interacts with pion dynamics \Rightarrow χ PT needs modification
 - Taste breaking structure for Staggered simulations is different from QCD
- Mixed action analysis is explored
 - Wilson-flowed links used as the valence action
 - Flowed action restores taste symmetry and allows cheaper inversions
 - Preliminary results is promising, demonstrating the viability of the approach
- More comprehensive analysis is needed. E.g. Errors of t_0 , Non-unitarity effects, the effects of low-lying 0^{++} scalar

Conclusion

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

Outline

Challenges

Mixed Action

Preliminary results

Conclusion

- Hadron Spectroscopy on nearly conformal models is challenging
 - Low-lying 0^{++} scalar interacts with pion dynamics \Rightarrow χ PT needs modification
 - Taste breaking structure for Staggered simulations is different from QCD
- Mixed action analysis is explored
 - Wilson-flowed links used as the valence action
 - Flowed action restores taste symmetry and allows cheaper inversions
 - Preliminary results is promising, demonstrating the viability of the approach
- More comprehensive analysis is needed. E.g. Errors of t_0 , Non-unitarity effects, the effects of low-lying 0^{++} scalar

Conclusion

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

Outline

Challenges

Mixed Action

Preliminary results

Conclusion

- Hadron Spectroscopy on nearly conformal models is challenging
 - Low-lying 0^{++} scalar interacts with pion dynamics \Rightarrow χ PT needs modification
 - Taste breaking structure for Staggered simulations is different from QCD
- Mixed action analysis is explored
 - Wilson-flowed links used as the valence action
 - Flowed action restores taste symmetry and allows cheaper inversions
 - Preliminary results is promising, demonstrating the viability of the approach
- More comprehensive analysis is needed. E.g. Errors of t_0 , Non-unitarity effects, the effects of low-lying 0^{++} scalar

Conclusion

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

Outline

Challenges

Mixed Action

Preliminary results

Conclusion

- Hadron Spectroscopy on nearly conformal models is challenging
 - Low-lying 0^{++} scalar interacts with pion dynamics \Rightarrow χ PT needs modification
 - Taste breaking structure for Staggered simulations is different from QCD
- Mixed action analysis is explored
 - Wilson-flowed links used as the valence action
 - Flowed action restores taste symmetry and allows cheaper inversions
 - Preliminary results is promising, demonstrating the viability of the approach
- More comprehensive analysis is needed. E.g. Errors of t_0 , Non-unitarity effects, the effects of low-lying 0^{++} scalar

Conclusion

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

Outline

Challenges

Mixed Action

Preliminary results

Conclusion

- Hadron Spectroscopy on nearly conformal models is challenging
 - Low-lying 0^{++} scalar interacts with pion dynamics \Rightarrow χ PT needs modification
 - Taste breaking structure for Staggered simulations is different from QCD
- Mixed action analysis is explored
 - Wilson-flowed links used as the valence action
 - Flowed action restores taste symmetry and allows cheaper inversions
 - Preliminary results is promising, demonstrating the viability of the approach
- More comprehensive analysis is needed. E.g. Errors of t_0 , Non-unitarity effects, the effects of low-lying 0^{++} scalar

Conclusion

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

Outline

Challenges

Mixed Action

Preliminary results

Conclusion

- Hadron Spectroscopy on nearly conformal models is challenging
 - Low-lying 0^{++} scalar interacts with pion dynamics \Rightarrow χ PT needs modification
 - Taste breaking structure for Staggered simulations is different from QCD
- Mixed action analysis is explored
 - Wilson-flowed links used as the valence action
 - Flowed action restores taste symmetry and allows cheaper inversions
 - Preliminary results is promising, demonstrating the viability of the approach
- More comprehensive analysis is needed. E.g. Errors of t_0 , Non-unitarity effects, the effects of low-lying 0^{++} scalar

Conclusion

Spectroscopy of
the BSM sextet
model

Chik Him (Ricky)
Wong

Outline

Challenges

Mixed Action

Preliminary results

Conclusion

- Hadron Spectroscopy on nearly conformal models is challenging
 - Low-lying 0^{++} scalar interacts with pion dynamics \Rightarrow χ PT needs modification
 - Taste breaking structure for Staggered simulations is different from QCD
- Mixed action analysis is explored
 - Wilson-flowed links used as the valence action
 - Flowed action restores taste symmetry and allows cheaper inversions
 - Preliminary results is promising, demonstrating the viability of the approach
- More comprehensive analysis is needed. E.g. Errors of t_0 , Non-unitarity effects, the effects of low-lying 0^{++} scalar