

Studying how the particle spectra of GUTs emerge

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Motivation - Physical states

- Physics is gauge invariant:
Non-Abelian gauge theories \Rightarrow bound states
- Electroweak physics:
 - Elementary fields (Higgs, W/Z) treated as if they were observable in perturbation theory
 - But they are gauge dependent
 \Rightarrow non-observable objects
- Why does perturbation theory work at all?

FMS mechanism in the SM

[Fröhlich, Morcchio and Strocchi, PLB97 (1980) and NPB190 (1981)]

- Construct gauge-invariant operator:

$$O(x) = (\phi^\dagger \phi)(x)$$

- Expand correlator in fluctuations around vev and in conventional perturbation theory: $\phi(x) = v + h(x)$

$$\langle O(x) \bar{O}(y) \rangle = 4v^2 \langle h(x) h(y) \rangle_0 + \langle h(x) h(y) \rangle_0^2 + \dots$$

- Compare poles on both sides: Same mass
- Confirmed on the lattice (also for 1^- channel)

[Maas, MPL A28 (2013) / Maas and Mufti, JHEP (2014)]

- Works also for the rest of the SM
- Does it work for BSM theories?

GUT-like theory

- Same logic as in SM leads to a **conflict**
- GUT inspired theories:
 - Gauge group is larger than global symmetry group
- Consider $SU(N)$ gauge theory ($N > 2$) with one fundamental scalar ϕ
 - Global symmetry: $U(1)$ custodial symmetry
- Perturbative construction: $SU(N) \xrightarrow{\langle \phi \rangle} SU(N - 1)$
 - $2(N - 1) + 1$ massive and $N(N - 2)$ massless gauge bosons
 - 1 massive real scalar field h

Physical spectrum of the GUT-like theory

- 0^+ $U(1)$ -singlet channel: $O(x) = (\phi^\dagger \phi)(x)$

$$\langle O(x) \bar{O}(y) \rangle = 4v^2 \langle h(x) h(y) \rangle + \dots$$

- 1 massive state
- Mass of perturbative Higgs

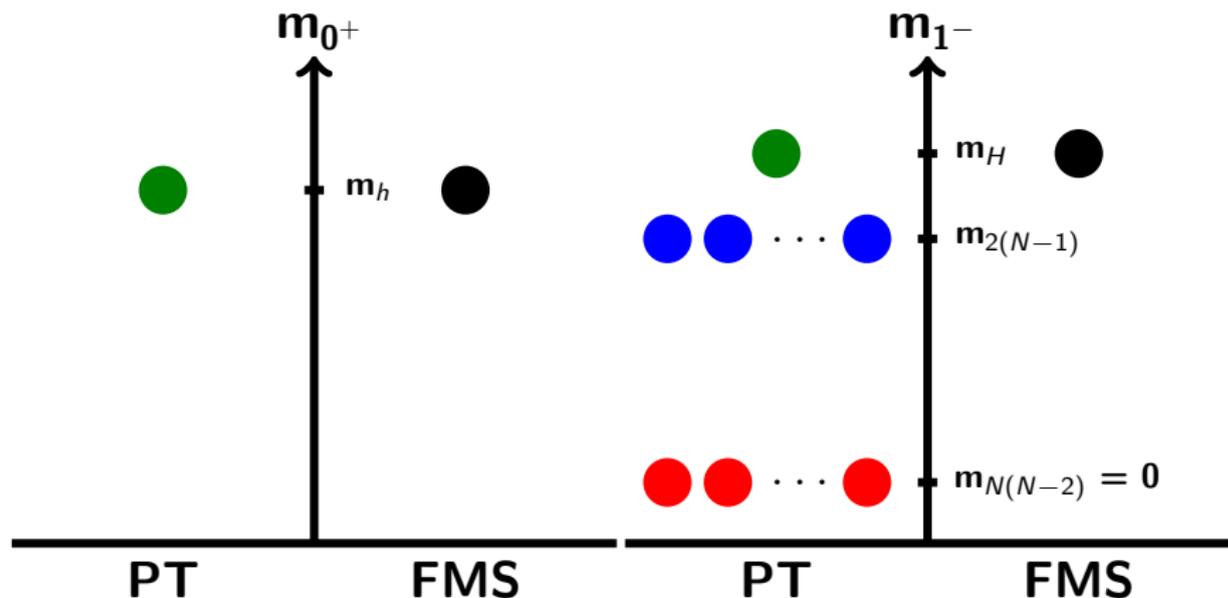
- 1^- $U(1)$ -singlet channel: $O_\mu(x) = i(\phi^\dagger D_\mu \phi)(x)$

$$\langle O_\mu(x) \bar{O}^\mu(y) \rangle = v^4 \langle W_\mu^H(x) W^{H \mu}(y) \rangle + \dots$$

- 1 massive state
- Mass of heaviest gauge boson W^H

Comparison between PT and FMS

- Contradiction in the singlet vector channel between physical and perturbative spectrum
- No contradiction in the singlet scalar channel



$SU(3)$ with a fundamental scalar - Lattice

[Maas and Törek, PRD95 (2017), 1607.05860]

■ Lattice action: $U_{x,\mu} = e^{iW_{x,\mu}} \in SU(3)$

$$S[U, \phi] = \frac{\beta}{3} \sum_{\square} \text{Re tr}[U_{\square}] + \sum_x \left[\phi_x^\dagger \phi_x + \lambda(\phi_x^\dagger \phi_x - 1)^2 - \kappa \sum_{\mu} (\phi_x^\dagger U_{x,\mu} \phi_{x+\hat{\mu}} + \text{c.c.}) \right]$$

■ Generating configurations: Multi-hit Metropolis

■ To study elementary fields: Gauge fixing required

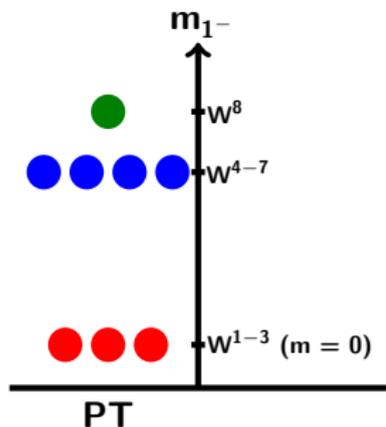
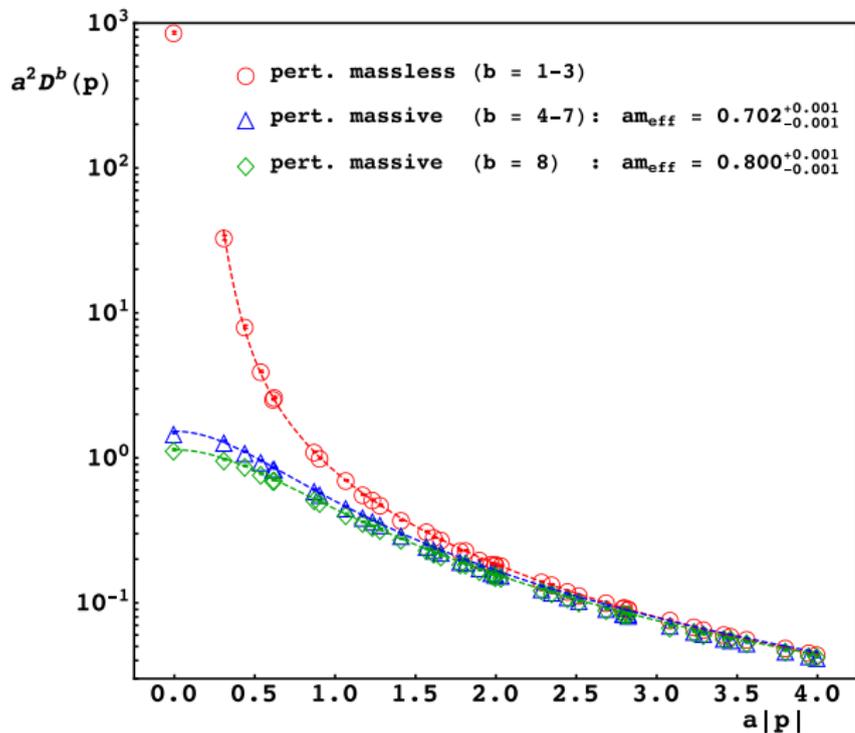
□ Local gauge fixing: Minimal Landau gauge

$$\partial_{\mu} W_{\mu}(x) = 0$$

□ Global gauge fixing: Rotate Higgs field into $\phi \propto (0, 0, 1)$

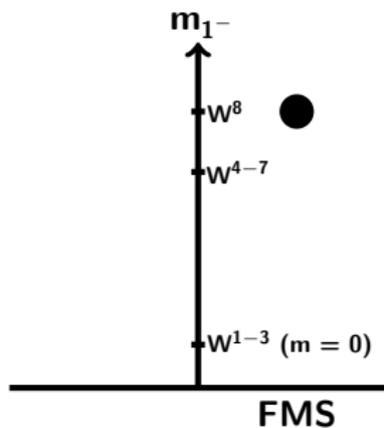
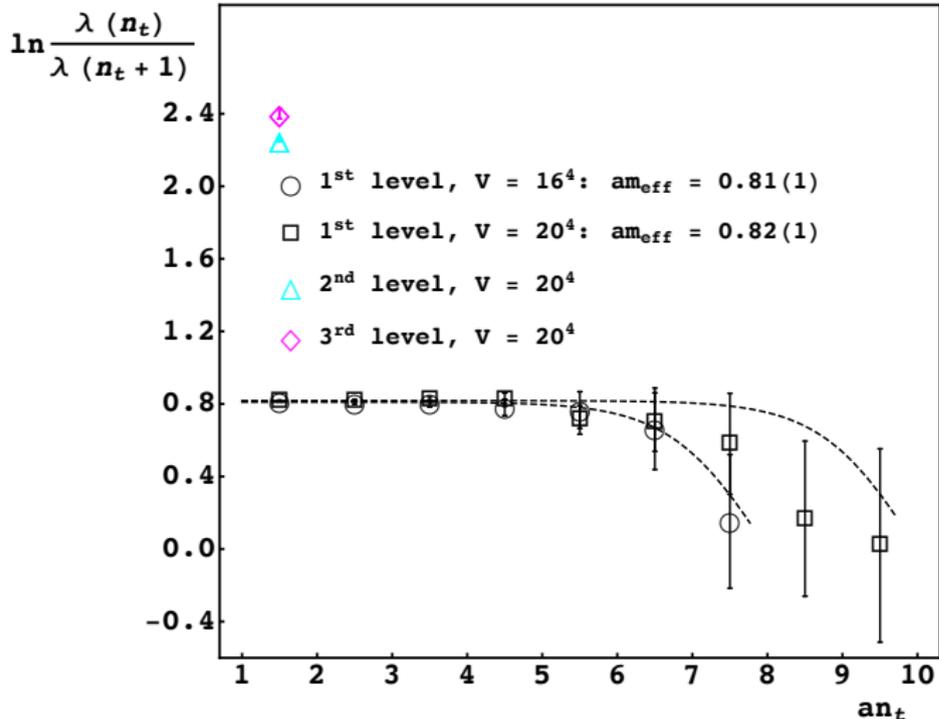
Masses from gauge-variant d.o.f.

$$V = 20^4, \beta = 9.59055, \kappa = 0.444462, \lambda = 0.4118$$



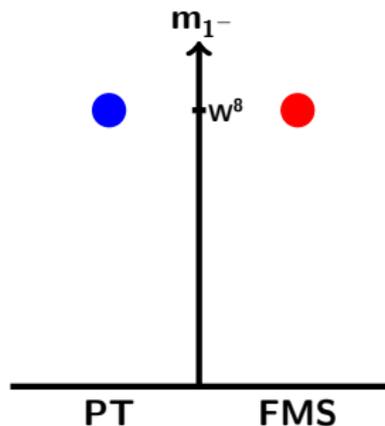
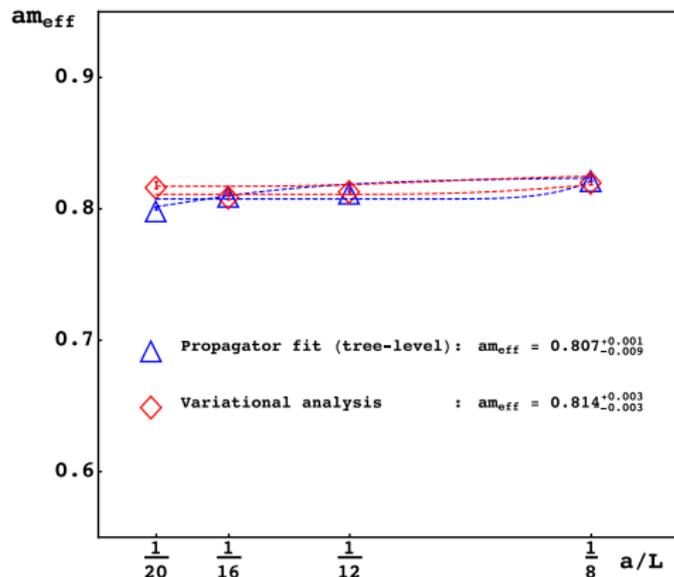
Masses from gauge-invariant d.o.f.

$V = 16^4, 20^4$, $\beta = 9.59055$, $\kappa = 0.444462$, $\lambda = 0.4118$



Volume dependency

$$\beta = 9.59055, \kappa = 0.444462, \lambda = 0.4118$$



- Single massive ground state with mass of W^8
- Exactly like FMS mechanism predicts
- Also confirmed for 0^+ channel

Open $U(1)$ states in the $SU(3)$ case

- There should be states with open $U(1)$ q-number:

$$\mathcal{O}^{0^+,1}(x) = \left[\epsilon_{ijk} \phi_i (D_\mu \phi)_j (D_\mu D_\nu D_\nu \phi)_k \right] (x)$$

$$\mathcal{O}^{0^+,-1}(x) = \mathcal{O}^{0^+,1}(x)^\dagger$$

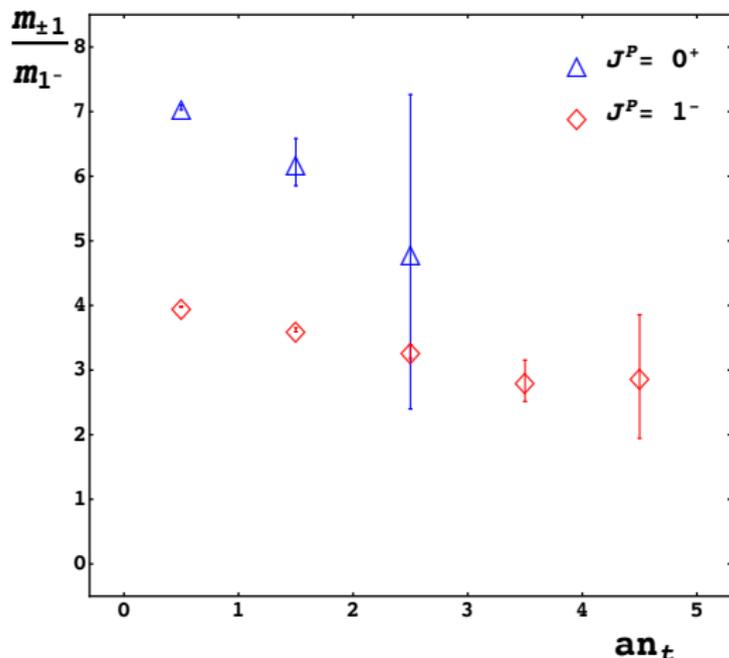
$$\mathcal{O}_\mu^{1^-,1}(x) = \left[\epsilon_{ijk} \phi_i (D_\mu \phi)_j (D_\nu D_\nu \phi)_k \right] (x)$$

$$\mathcal{O}_\mu^{1^-,-1}(x) = \mathcal{O}_\mu^{1^-,1}(x)^\dagger$$

- Should be stable (conserved q-number)
- Not predicted by perturbation theory
- Application of FMS leads to complicated pole structure: Under investigation

Effective masses of open $U(1)$ states

$V = 16^4, \beta = 6.85535, \kappa = 0.456074, \lambda = 2.3416, n_{\text{smear}} = 10$



■ Signals are very noisy

■ Masses are of the order of the cut-off

Summary and conclusions

- FMS applied to SM reproduces correct spectrum and it is based on gauge invariance

[Egger *et al.*, 1701.02881 / Törek and Maas, 1610.04188 /

Maas and Mufti, 1312.5579 / Maas, 1205.6625 /

Fröhlich *et al.*, PLB97 (1980) and NPB190 (1981)]

- $SU(N)$ gauge theory with one fundamental scalar

[Maas, Sondenheimer and Törek, to be published]

- FMS is supported by lattice results for $SU(3)$

[Maas and Törek, PRD95 (2017), 1607.05860

and PoS LATTICE2016, 1610.04188]

- Open $U(1)$ states need further investigations

Outlook

[Maas, Sondenheimer and Törek, to be published]

- Toy models on the market where further **conflicts** are expected:
 - $SU(N)$ with adjoint scalar field
 - $SU(N)$ with adjoint and fundamental scalars
- FMS predicts entirely different spectrum than perturbation theory
- Classes of **conflicts** are testable on the lattice
- Conventional GUTs seem to fail to reproduce low energy spectrum

Running coupling

